

I. Summary

Paschen's law underlies our understand of scaling properties of electric discharges. It describes non-thermal, self-sustained discharges occurring in high voltage, low current, and low-pressure conditions between two parallel plate electrodes (Raizer et al., 1991). Originally established experimentally for various gas mixtures, Townsend (1915) developed a formal theory that relies on an exponential fit of the primary ionization coefficient $\alpha_{\text{eff}} \approx A \exp(-Bp/E)$ and the poorly understood secondary electron emission (γ). Raizer et al. (1991 p.75) states that "The data on γ are incomplete and often contradictory." The commonly used A, B, γ constants do not traditionally consider electrodes' geometries and materials. Rioussset et al. (2022) proposed a new formalism suitable for non-planar geometries using the reduced effective ionization coefficient α_{eff}/p and mobility μp . The new model accounts for volume and drift velocity changes along the avalanche path via a power law approximation of μp . We propose to use this new formalism and explicitly characterize the constants A and B in the effective ionization α_{eff} . In addition, we develop an experimental setup for their validation. The discharges are produced in Embry-Riddle Aeronautical University's Lightning Plasma Chamber (LPC). The initiation voltage (V_{cr}) is measured at specific pressures p and distances d in air. Distances and pressure can be adjusted using a linear feedthrough (LFT) and mass flow controller (MFC), respectively. In addition, we seek to establish how γ depends on the nature of the electrode, its geometry, surface condition, and the gas of the environment. We show that the v. Engel-Steenbeck equation (Fridman & Kennedy, 2004) and the assumed value of γ does not adequately characterize the critical voltage under non-planar geometries. We propose a χ^2 -analysis to assess the dependencies of γ on the environmental parameters and obtain accurate values for A and B. These variations may prove especially important for the initiation of Transient Luminous Events occurring near the ionosphere at low pressures.

II. Introduction

Paschen's Law & Townsend Theory

$V \geq V_{\text{cr}} \Rightarrow$ Collision e-N (N: neutral gas) \Rightarrow Ionization of neutrals \Rightarrow 1 ion / 2 free electrons \Rightarrow Avalanche (Townsend, 1915).

Secondary Electron Emission S.E.E. (γ)

Experimental.

- Depends on metallicity, pressure, distance, geometry, and gas mixture (Ellion, 1965).

Paschen's Law: State of the Art

- Main formalism for Townsend's theory.
- Model of infinite parallel plates.
- Not applicable to non-uniform geometries.
- Left of minimum is ill-defined (Knaster et al., 2012).
- A and B coefficients are defined by Stoletov point.

Objectives

- Definition of a new system of equations accounting for (1) distance between cathode and anode (2) S.E.E. (γ).
- Comparison with experimental data collected in the LPC chamber.
- A and B coefficients defined based on LSQ fit of either:
 - Plot of E/N vs α_{eff}
 - Plot of pd vs. $V_{\text{cr}} = Bpd/\ln(Apd - \ln(1/\gamma + 1))$
- Estimates of S.E.E. (γ) using theory.

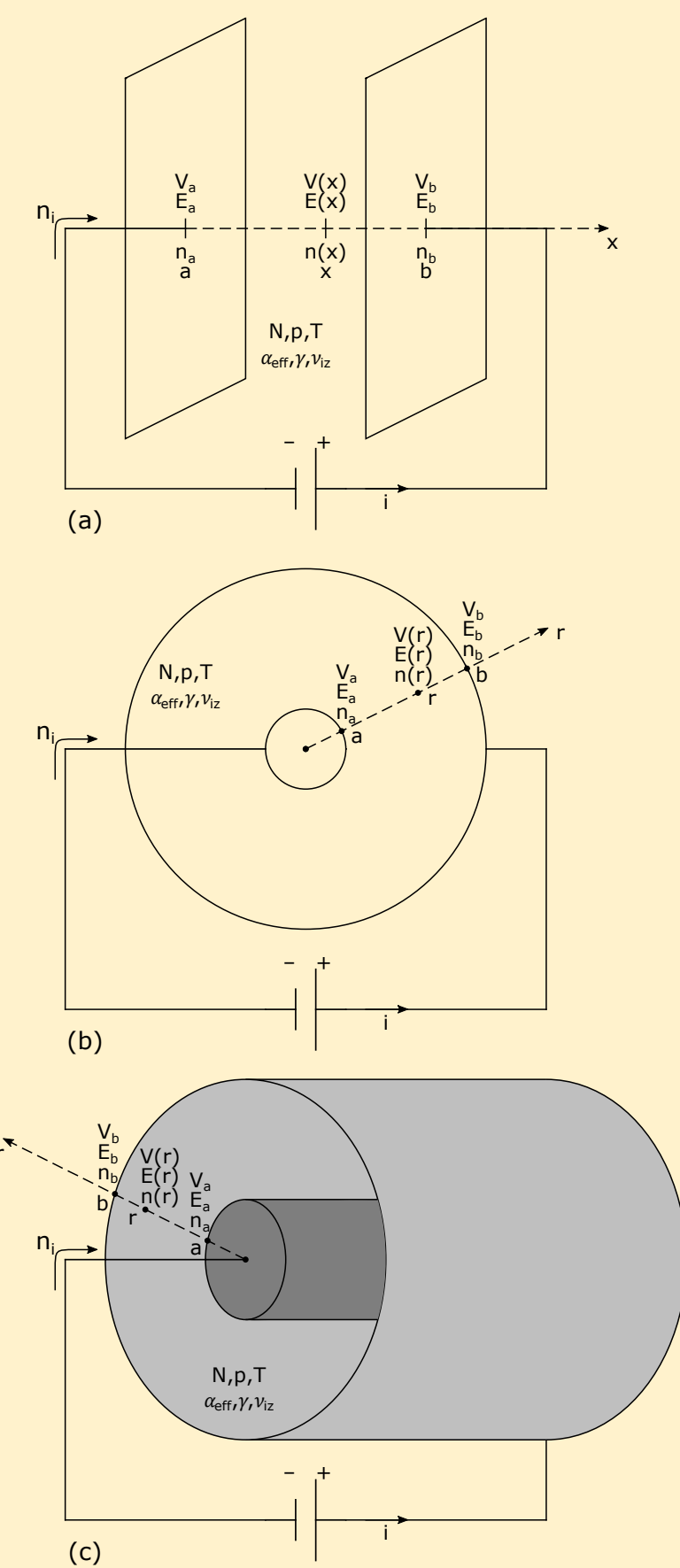


Figure 1. Geometries: (a) Parallel plates; (b) Coaxial cylinders; (c) Concentric spheres.

III. Methods & Models

a) Experimental setup

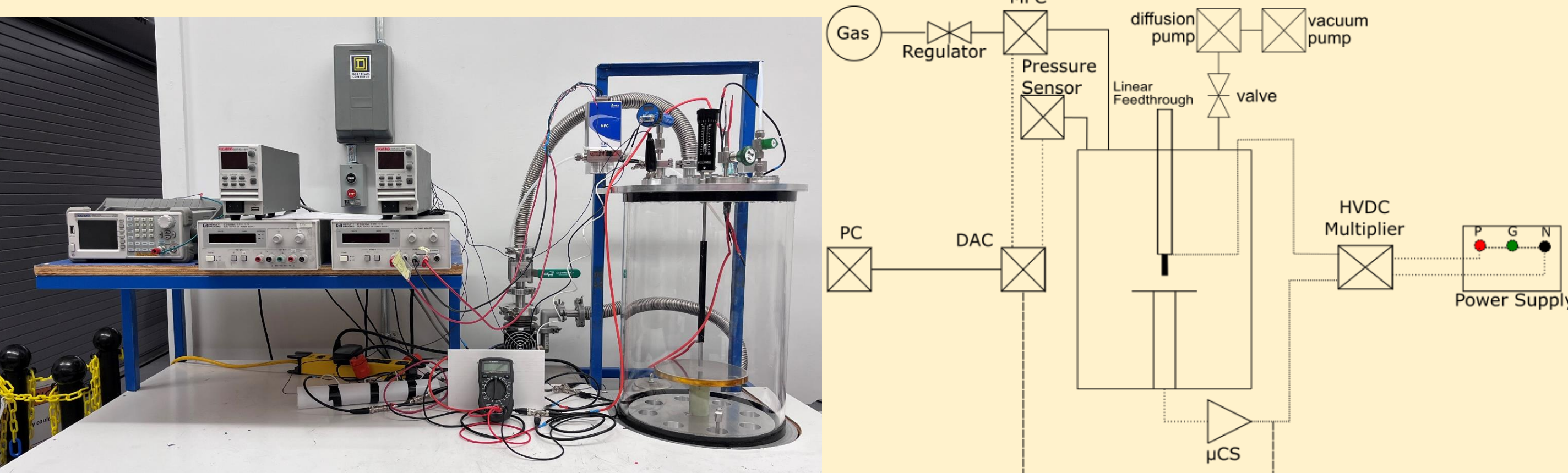


Figure 2. Experimental setup for initiating electrical dischargers in various environments. HVDC multiplied input voltage amplifies 0-25V to 10-3000V. Left: Experimental setup. Right: Schematic of the experiment.

III. Methods & Models (cont.)

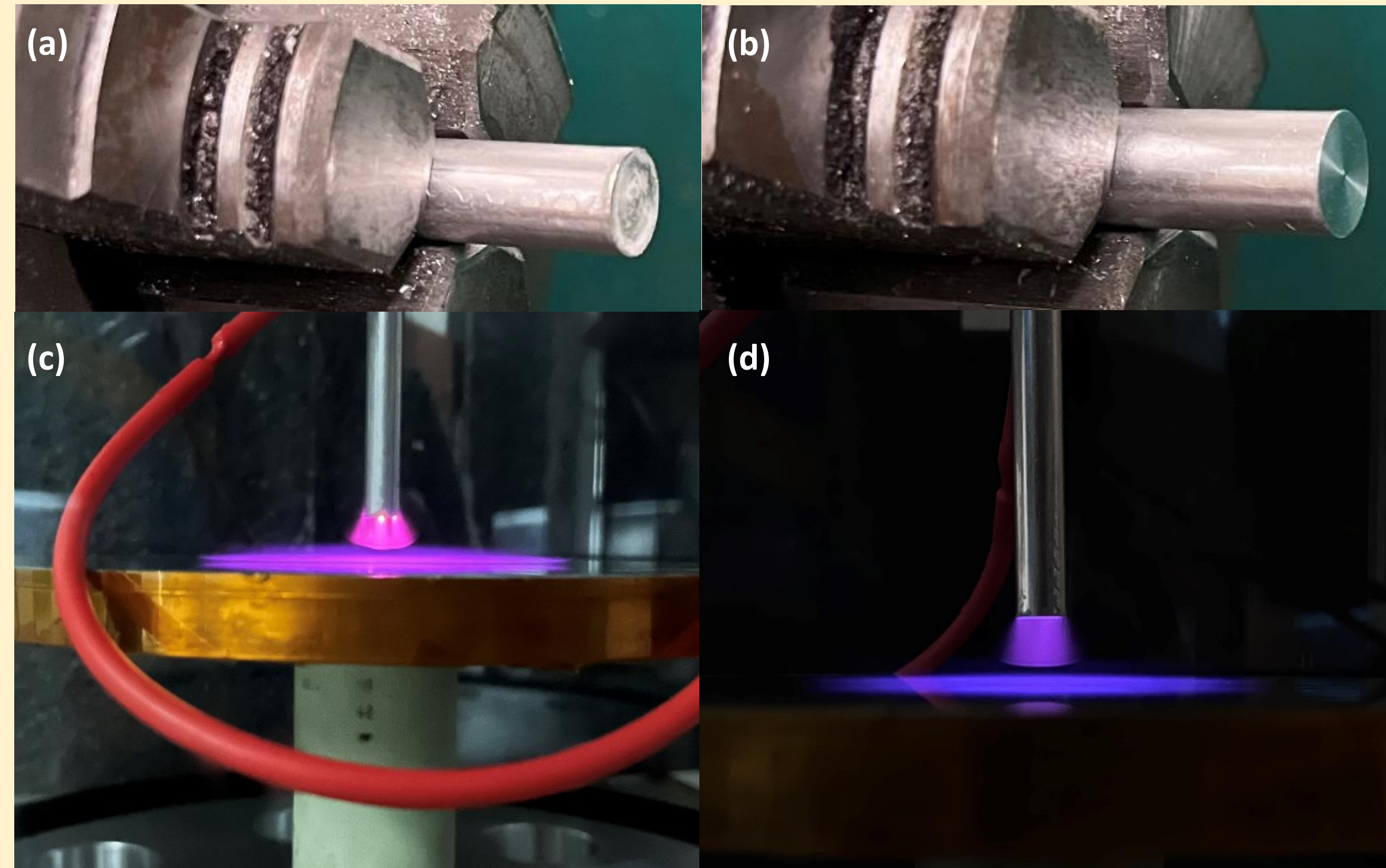


Figure 3. (a) Rough surface electrode from previous discharges; (b) Smooth surface electrode; (c) Glow discharge from rough surface, $\gamma=0.0029$; (d) Glow discharge from smooth electrode, $\gamma=0.0049$.

b) Theory

- Plasma relationships:
 - $\nabla \cdot \vec{E} = 0$ (1)
 - $v_{iz} = \alpha v_d$ where $\frac{\alpha}{N} = Ae^{-\frac{B}{E/N}}$ (2)
 - $v_d = \mu E$ where $\mu N = C \left(\frac{E}{N}\right)^D$ (3)
 - $\frac{\partial n}{\partial t} + \nabla \cdot (n \vec{v}_d) = v_{iz} n$ (4)
- Constitutive relationships between charge densities at a and b from primary secondary ionization and electronic currents:
 - $n_a = n_\gamma + n_i$ (5)
 - $n_\gamma = \gamma(n_b - n_a)$ (6)
 - $n_b = A_p n_a$ (7)
- Gauss' law $\nabla \cdot \vec{E} = 0 \Rightarrow E(r)/N$
- Breakdown equation $\Rightarrow \frac{E}{N} \Big|_a$
 - $\delta = 0$: Cartesian \Rightarrow v. Engel-Steenbeck
 - $\delta = 1$: Cylindrical (8)
 - $\delta = 2$: Spherical
- $\vec{E} = -\nabla V(r) \Rightarrow V_{\text{cr}}$

IV. Results

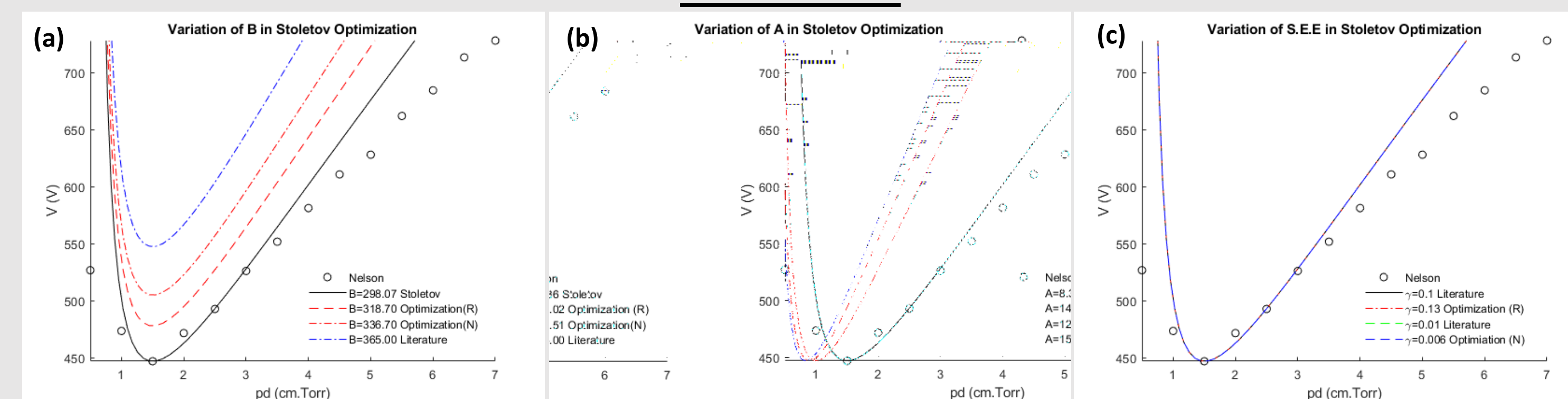


Figure 4. (a) Role of variable B in Paschen curves; (b) Role of variable A in Paschen curves; (c) Role of γ in Paschen curves. $B = V_{\text{min}}/pd_{\text{min}}$ $A = \bar{e} \ln\left(\frac{1}{\gamma} + 1\right)/pd_{\text{min}}$ (Fridman & Kennedy, 2004, p.210).

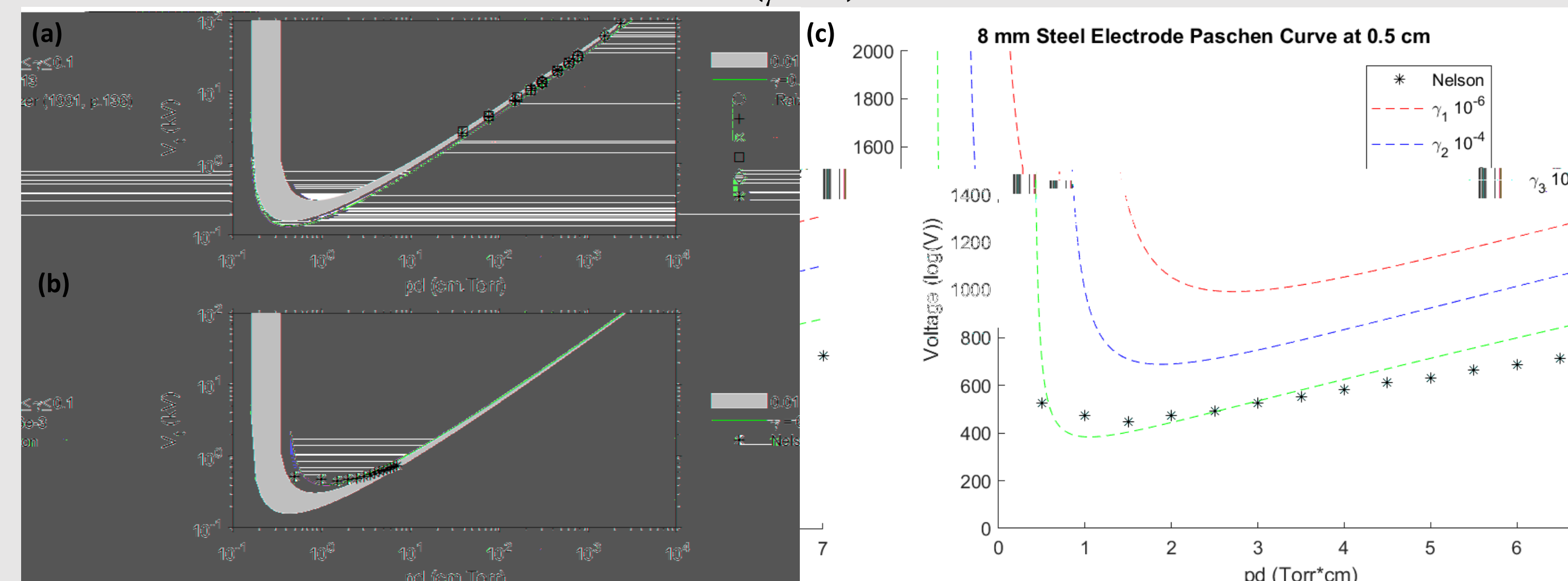


Figure 5. (a) Comparison of 'acceptable range' for Raizer et al. (1991) data; (b) Comparison of 'acceptable range' for Nelson data; (c) Discrepancy of Paschen curves in air from v. Engel-Steenbeck equation.

IV. Results (cont.)

Table 1. Case studies for air. Raizer et al. (1991, Tab.4.1) suggests that $A = 15/(\text{cm} \cdot \text{Torr})$, $B=365 \text{ V}/(\text{cm} \cdot \text{Torr})$, $\gamma = 10^{-2}$. All optimizations based on best fit equation.

V. Discussion

Role of previous ionization path:

- Unpurged chamber \Rightarrow Presence of free ions/electrons \Rightarrow Easier breakdown \Rightarrow Lower V_{cr} .
- Purged chamber \Rightarrow Little/no free charges \Rightarrow Stricter conditions \Rightarrow Higher V_{cr} .
- Improper grounding \Rightarrow Easier breakdown \Rightarrow Lower V_{cr} .

Roles of primary α_{eff} and secondary electron emission γ :

- Discrepancy between experiments and theory when A, B calculated from Stoletov's points.
- Impossible to calculate A & γ separately based on v. Engel-Steenbeck equation \Rightarrow Discrepancies when LSQ fit is used.
- Surface conditions of electrode \Rightarrow accrued errors in discharge parameters.

VI. Conclusions

The principal results and contributions from this work can be summarized as follows:

- We developed a new experimental setup to create self-sustained electrical discharges in air.
- We performed the first tests of scalability for the newly revised formalism for Paschen's law (Rioussset et al., 2022, under review).
- We found discrepancies between theoretical calculations of critical voltage and experiments.
- We compared the estimates of A and B obtained from Stoletov's point to a LSQ fit and showed that the accepted gas constants and secondary electron emission only hold true at minimum critical voltage.
- We demonstrated that adopting the v. Engel-Steenbeck equation as a standard description of the Paschen curves does NOT let us calculate A and γ separately.
- We experimentally showed that rough surface conditions of electrode decreases the secondary electron emission.

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