



Mapping Solar Wind Flows with PUNCH

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University

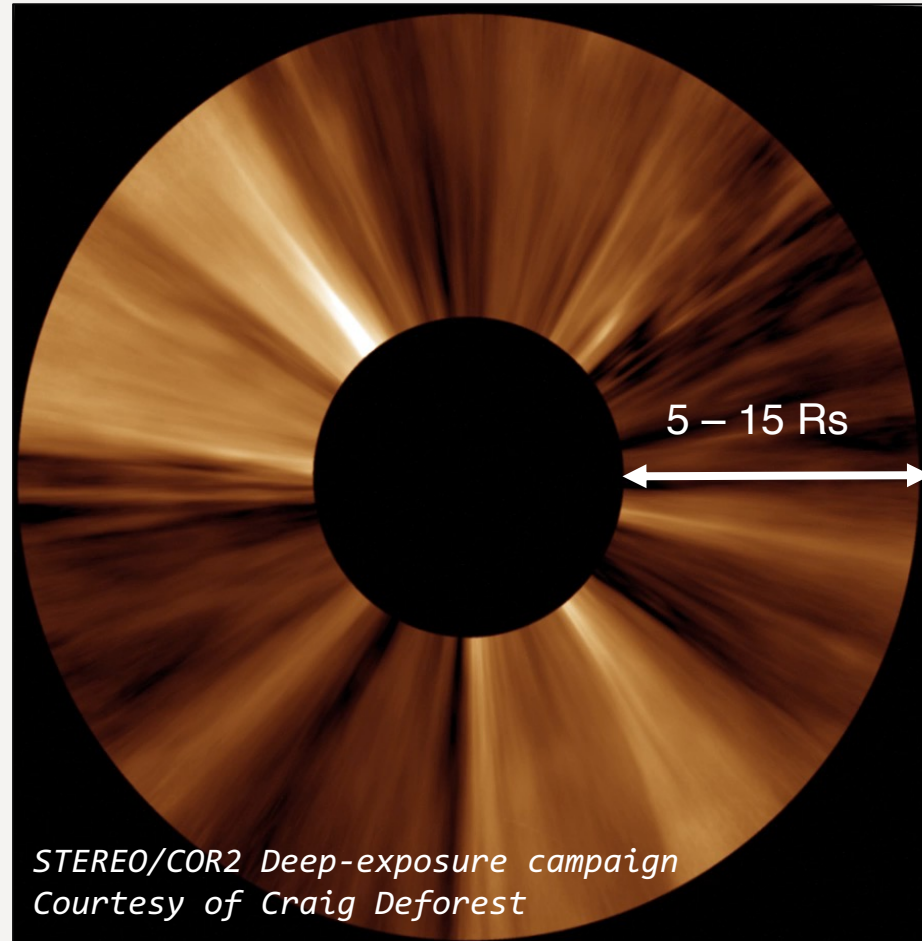
PUNCH 4 July 6th,
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Team:
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Valmir Moraes Filho
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Bea Gallardo-Lacourt
Elena Provornikova
Anna Malanushenko

MAPPING SOLAR WIND FLOWS: WHY?

- Understand the interplay between the corona and planetary environments
- By expanding as the SW flows outward, relatively small changes near the sun's surface feed planet-wide space weather effects. Measuring that flow is necessary to relate the dynamics in the environment of Earth and the other planets to what has happened upstream.
- Critical lack of flow maps in the solar wind, addressed by delivering solar wind flow fields with quantifiable uncertainties

MAPPING SOLAR WIND FLOWS: HOW?



HOW DO WE TRACK PLASMA FLOWS?

- Optical flow
- Physics-based
- Neural Networks
- Ball-tracking

HOW DO WE TRACK PLASMA FLOWS?

- **Optical flow**

Definition (qualitative): quantify the motion of brightness patterns across a time series of images in a sparse or dense flow field.

- Physics-based

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HOW DO WE TRACK PLASMA FLOWS?

○ Optical flow

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Methods:

- **Differential**
- **Feature matching**
- **Frequency based**

○ Physics-based

○ Neural Networks

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$$\partial_x I u + \partial_y I v + \partial_t I = 0$$

$I(x,y,t)$: Brightness (Image intensity)
(u,v): (x,y)-component of the 2D velocity vector in the image plane

○ Physics-based

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○ Physics-based

- 1 optical flow equation
 - 2 unknowns (u,v)
 - In reality: noise \Rightarrow optical flow equation \Rightarrow error term
- \Rightarrow Need additional constraints: e.g. smoothness constraints (no sharp transitions)
- \Rightarrow Minimization problem

○ Neural Networks

Horn & Schunk (1981)

$$\epsilon_b = \partial_x I u + \partial_y I v + I_t$$

$$\epsilon_s = \partial_x u^2 + \partial_y u^2 + \partial_x v^2 + \partial_y v^2$$

○ Ball-tracking

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$$\partial_x I u + \partial_y I v + \partial_t I = 0$$

○ Physics-based

Caveat



**Apparent motion:
upward** ↑

○ Neural Networks

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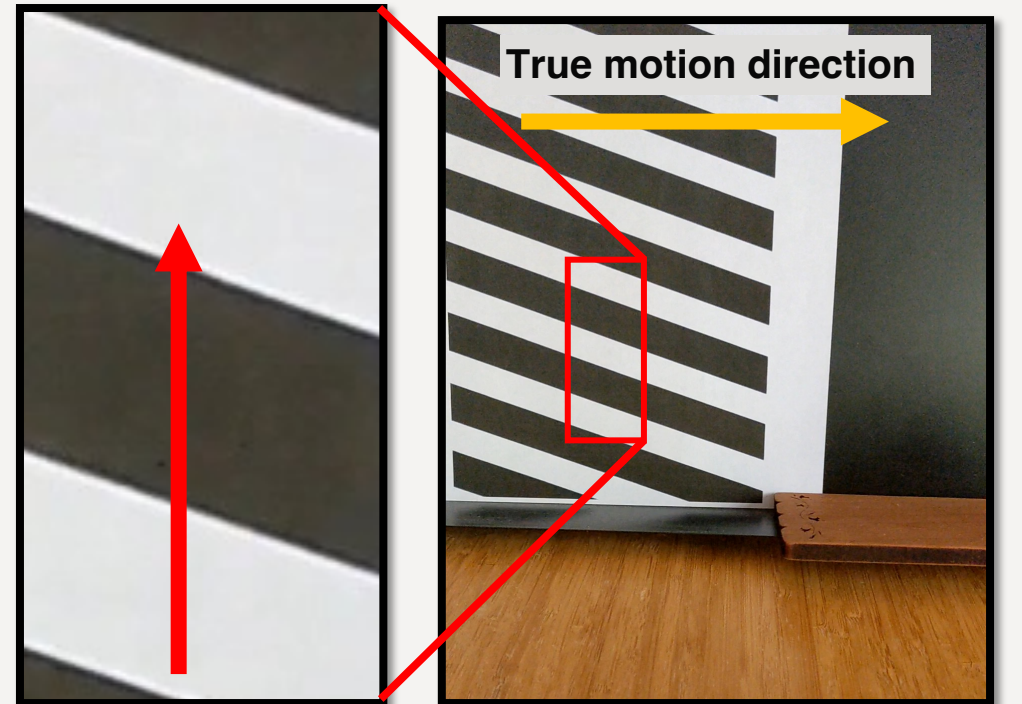
$$\partial_x I u + \partial_y I v + \partial_t I = 0$$

○ Physics-based

○ Neural Networks

○ Ball-tracking

Caveat



Apparent motion:
upward ↑

True motion: purely horizontal
left to right

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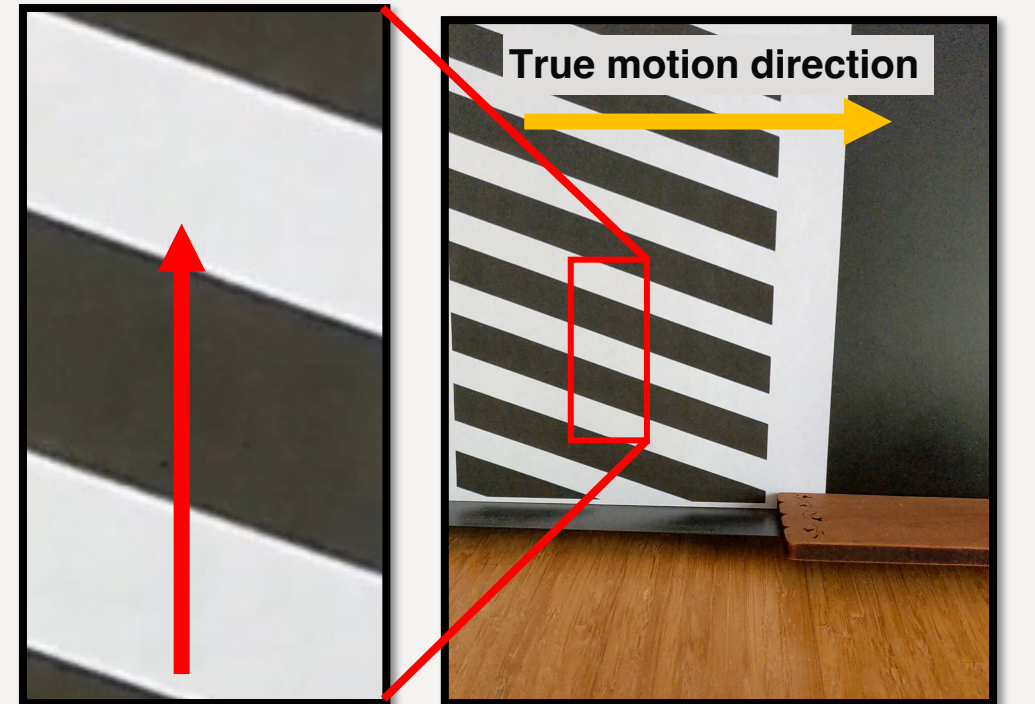
Caveat

When the image has locally no gradient in either or both direction, the motion vector cannot be determined

➤ Aperture problem

○ Neural Networks

○ Ball-tracking



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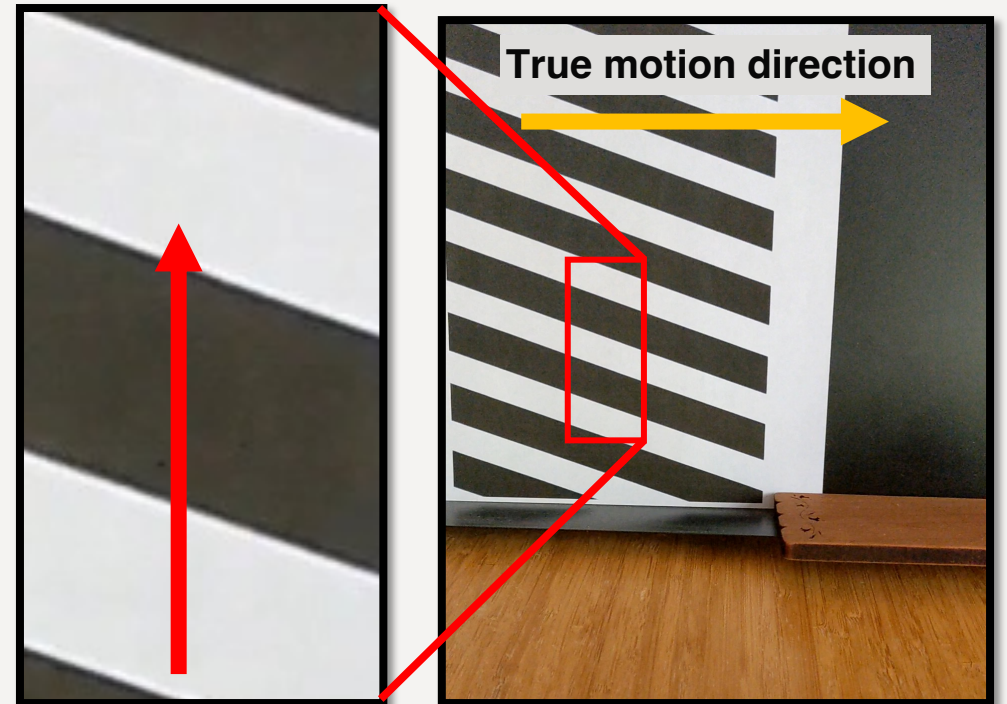
Some implementations can circumvent this problem:

- ✓ Numerical schemes fill in the gap
- ✓ Hierarchical/pyramidal processing

But... not tested yet for PUNCH

○ Neural Networks

○ Ball-tracking



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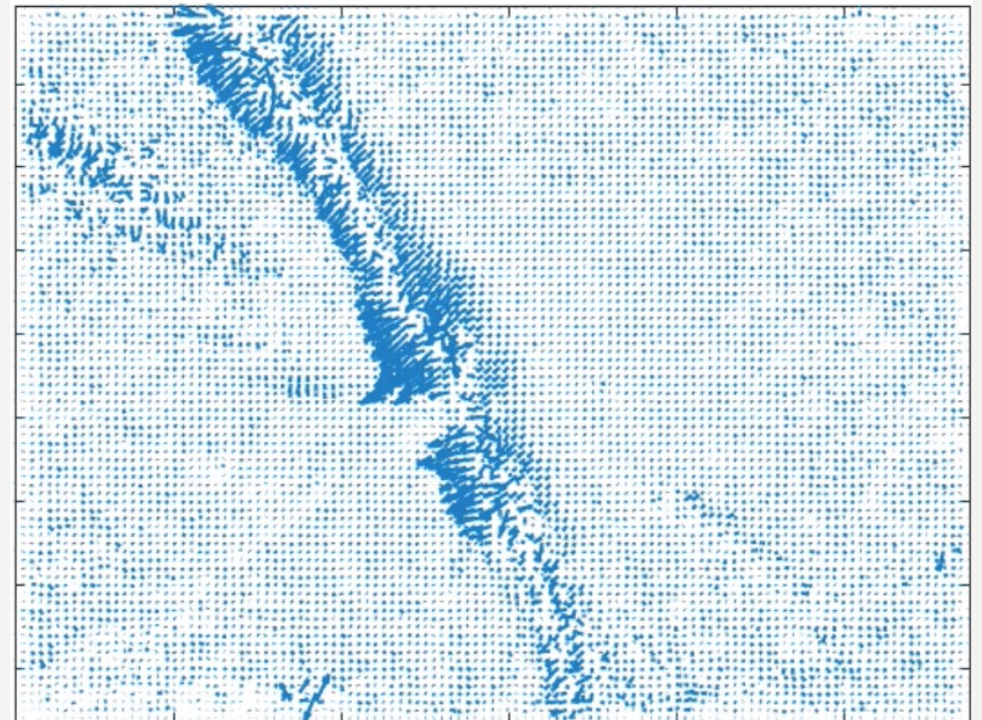
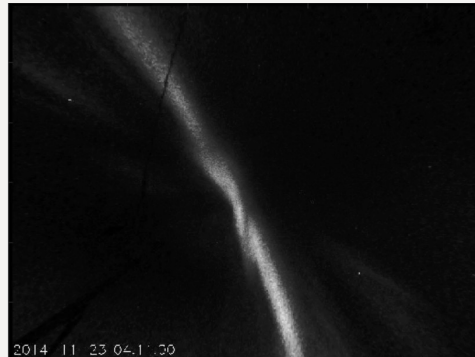
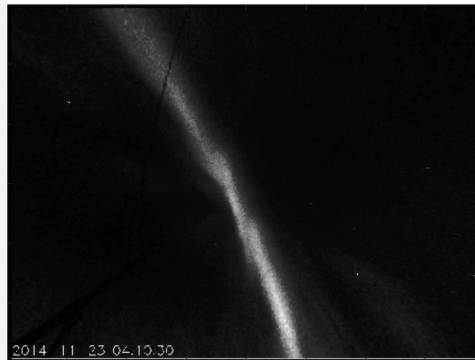
Application of differential method by **Bea Gallardo-Lacourt** for tracking auroras:

○ Physics-based

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○ Ball-tracking

Dense optical flow



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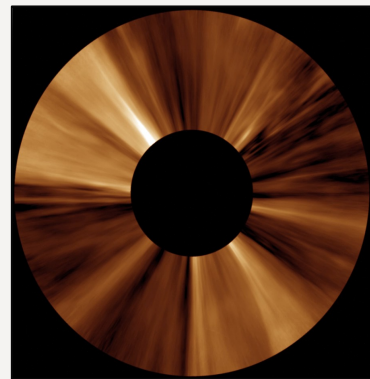
$$\partial_x I u + \partial_y I v + \partial_t I = 0$$

- 1 optical flow equation
 - 2 unknowns (u,v)
- ⇒ Need additional constraints

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Unwrapped view (polar transform): $v \Rightarrow$ radial component of the velocity. Purely radial flow: u vanishes.

Azimuth axis [0 – 360 deg]

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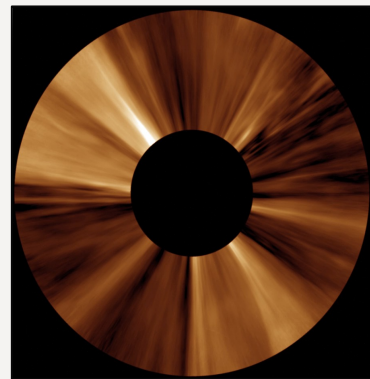
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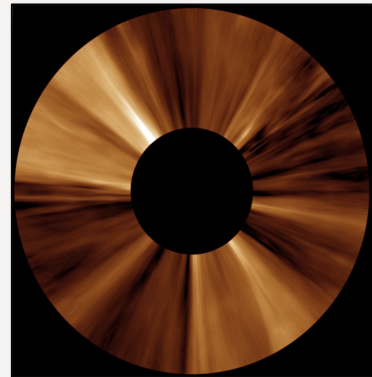
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⇒ Differential methods are worth a shot

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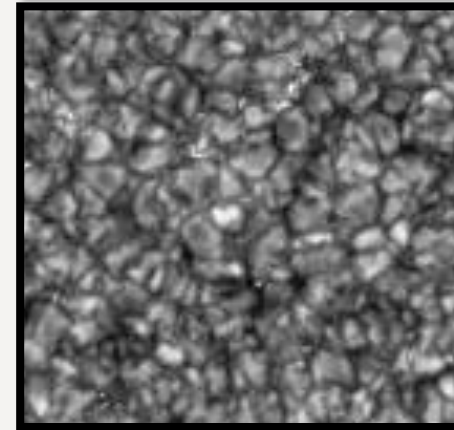
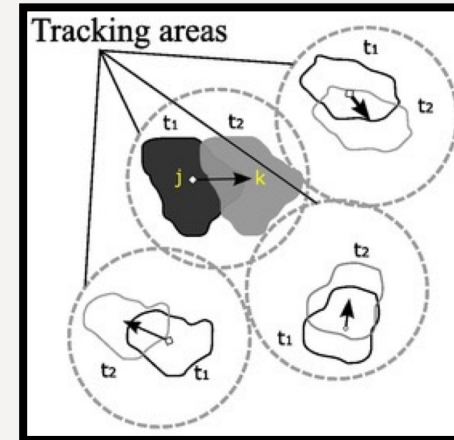
○ Ball-tracking

Metric of similarity: correlation

$$\sigma_{X^f} = \sqrt{\frac{1}{N-1} \sum_{i=1}^N (X_i^f - \bar{X}^f)^2}$$

$$R(k) = \frac{\sigma_{X^1 X^2}}{\sigma_{X^1} \sigma_{X^2}}$$

Local Correlation tracking:
optical flow based on
“correlation” similarity metric,
telling how much two tracking
areas in consecutive images are
similar. The position of
maximum correlation yields the
local motion vector.



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$$I(\mathbf{x}, t) = I_0(\mathbf{x})\delta(\mathbf{x} - \mathbf{v}t)$$

Initial brightness

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Initial brightness

$$I(\mathbf{x}, t) = I_0(\mathbf{x})\delta(\mathbf{x} - \mathbf{v}t)$$

$$\hat{I}(\mathbf{k}, \omega) = \hat{I}_0(\mathbf{k}, \omega)\delta(\mathbf{k} \cdot \mathbf{v} + \omega)$$

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- No practical implementation in place for heliospheric imagery
- Makes sense for tracking **periodic** density structures

HOW DO WE TRACK PLASMA FLOWS?

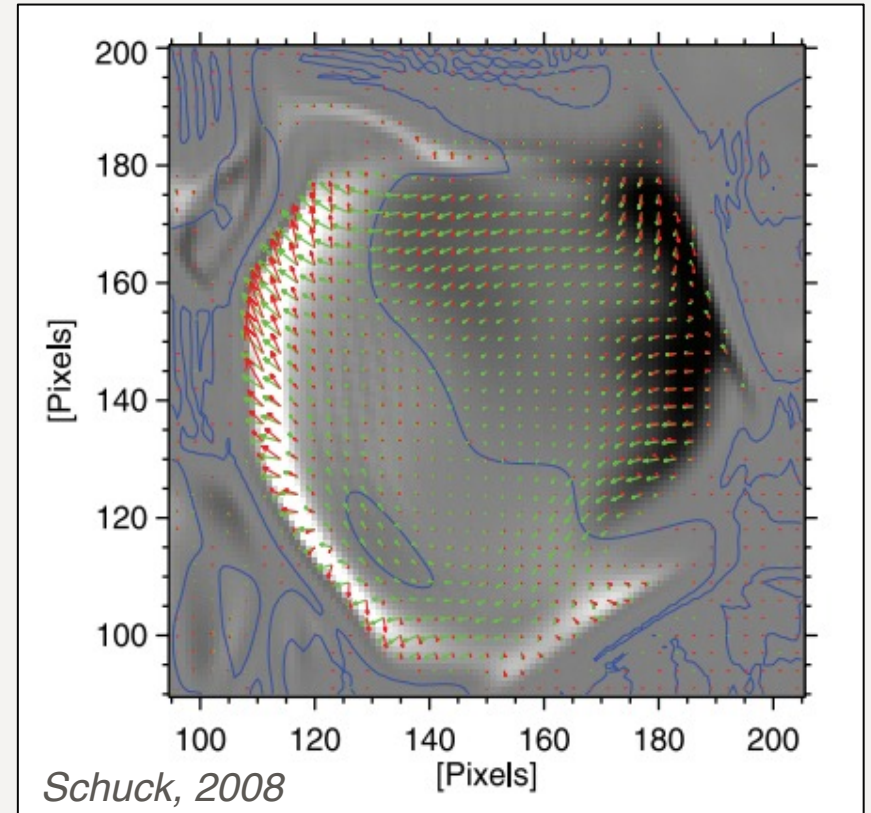
○ Optical flow

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- **Affine velocity estimators:**
DAVE & DAVE4VM (Schuck, 2006, 2008)
Using magnetic field measurements, account for magnetic induction equation to track the velocity of magnetic footpoints in the photosphere.
- More accurate results than correlation-based methods



HOW DO WE TRACK PLASMA FLOWS?

- Optical flow

- **Physics-based**

- **PUNCH:** polarized brightness
- **Physics:** Thompson scattering
- **Optical flow:** additional physical constraints should be investigated to minimize the uncertainty when relying solely on the displacements of brightness patterns.

- Neural Networks

- Ball-tracking

HOW DO WE TRACK PLASMA FLOWS?

○ Optical flow

Supervised Neural Nets are trained with [MHD] simulations, where a network is presented input observations (synthetic granulation) and an output ground truth (flow field), and the neural net creates a mapping functions between the input and output.

○ Physics-based

○ Neural Networks

- CNN: supervised
- PiNNs: unsupervised

○ Ball-tracking

HOW DO WE TRACK PLASMA FLOWS?

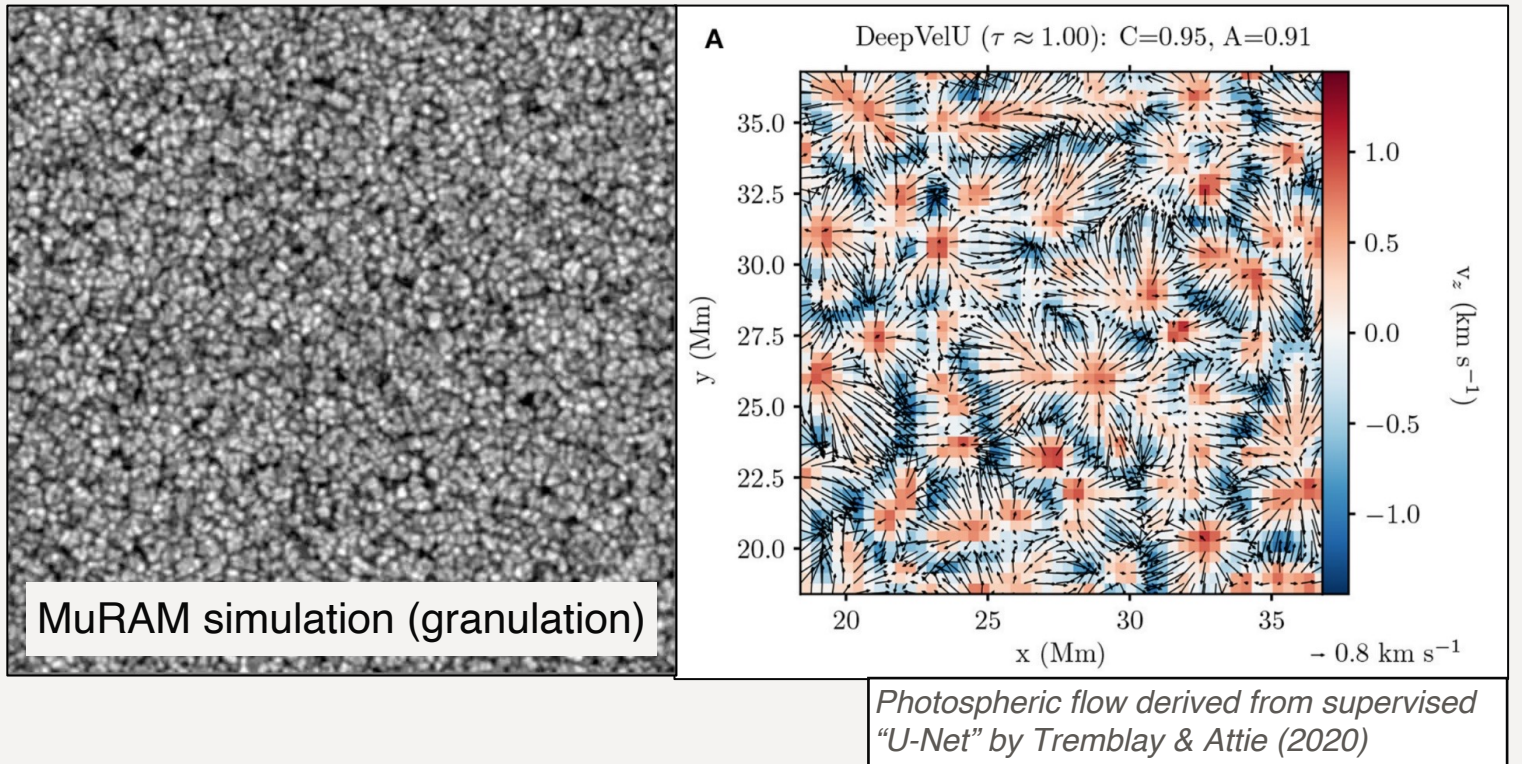
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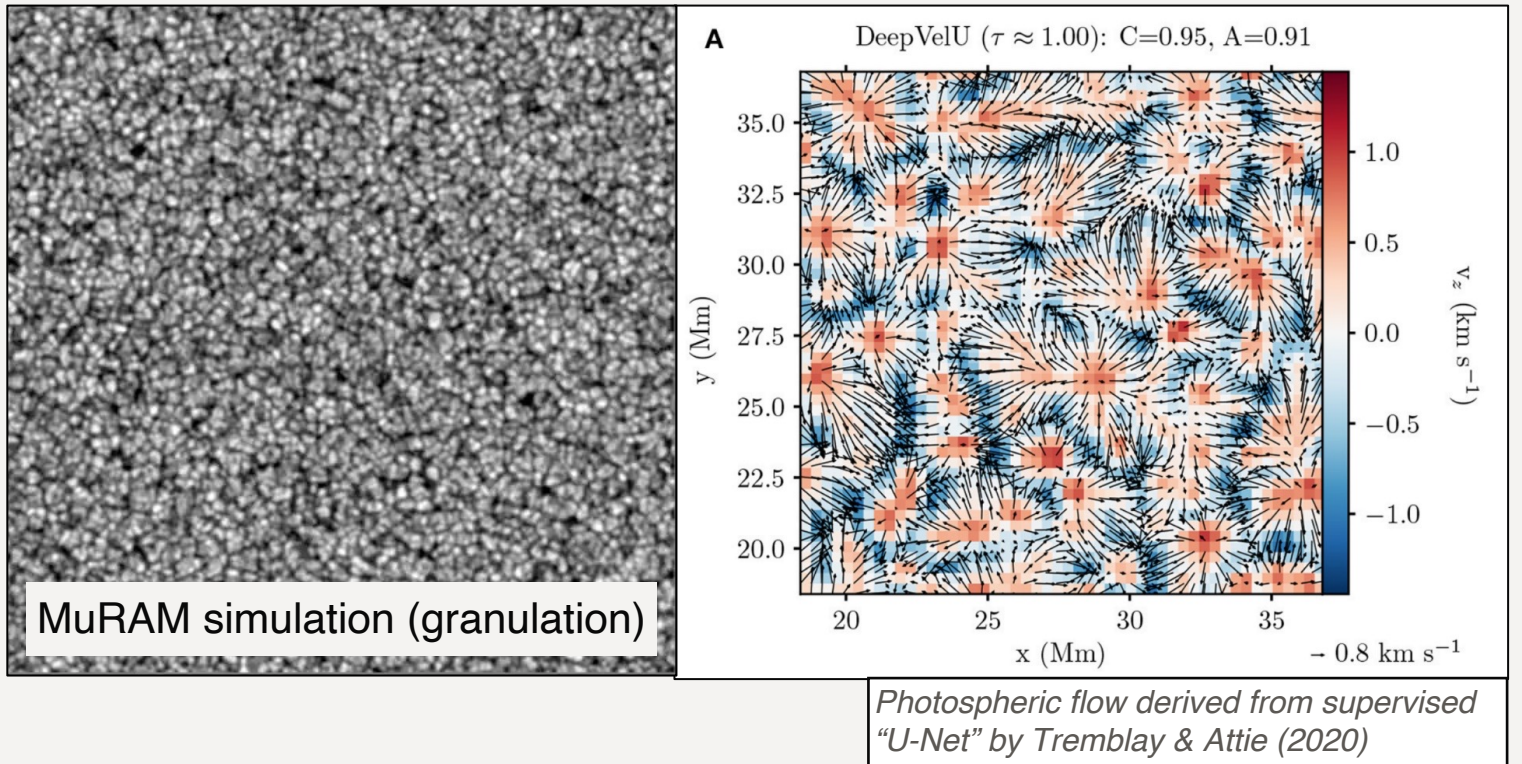
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Caveat: may not generalize well enough if systematics, or the lack of simulated physics make the real observations and simulations deviate from each other.

○ Ball-tracking

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PiNNs are Unsupervised Physics-informed Neural Nets: The forward propagation is using observations as input, but instead of a ground truth flow field at the output, the forward/backprop minimization is driven by physics equations that describe the mechanisms that **we believe** are at play.

Advantages:

➤ Efficient PDE solvers that can learn non-linear relationships

Disadvantages:

➤ Carry the uncertainty on to what extent the physics equations describe the observations, which is a human-based choice, restrict discovery space

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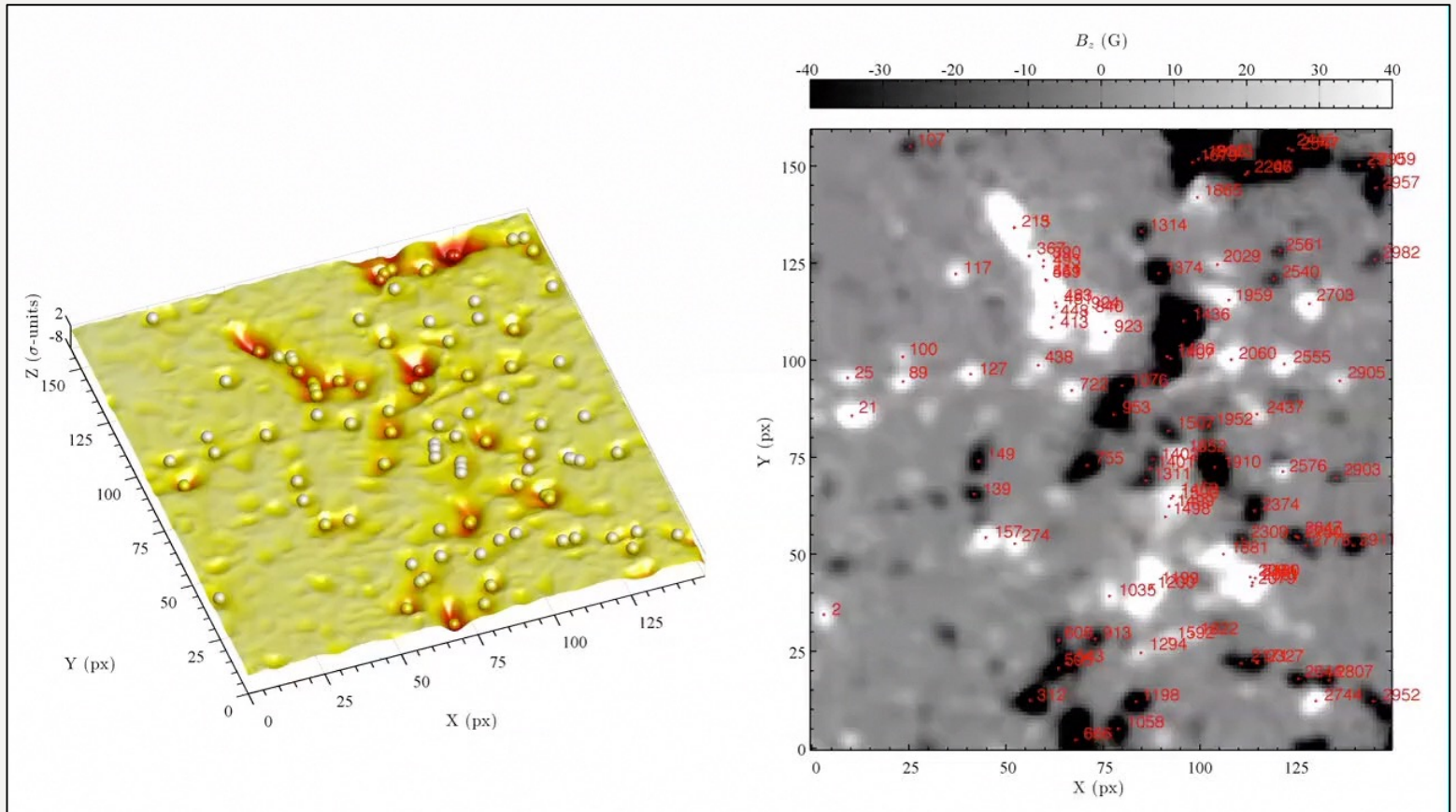
Magnetic Balltracking (*Attie & Innes, 2015*): Tracking in the **Lagrange** reference frame of moving magnetic features.

Output a “sparse” flow field, motion vectors for a set of moving objects (here, magnetic moving fragments in magnetograms), and feature characteristics (lifetimes, sizes, etc...)

○ Physics-based

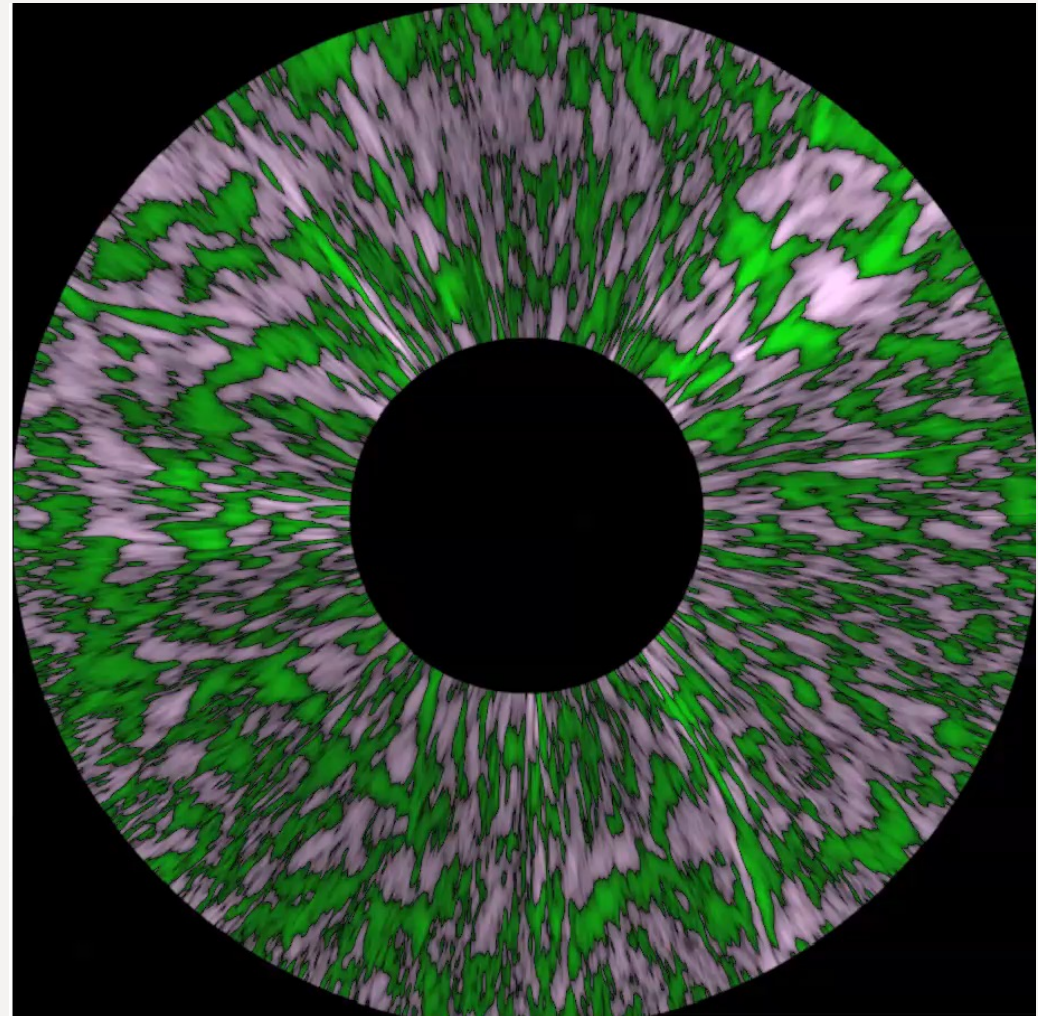
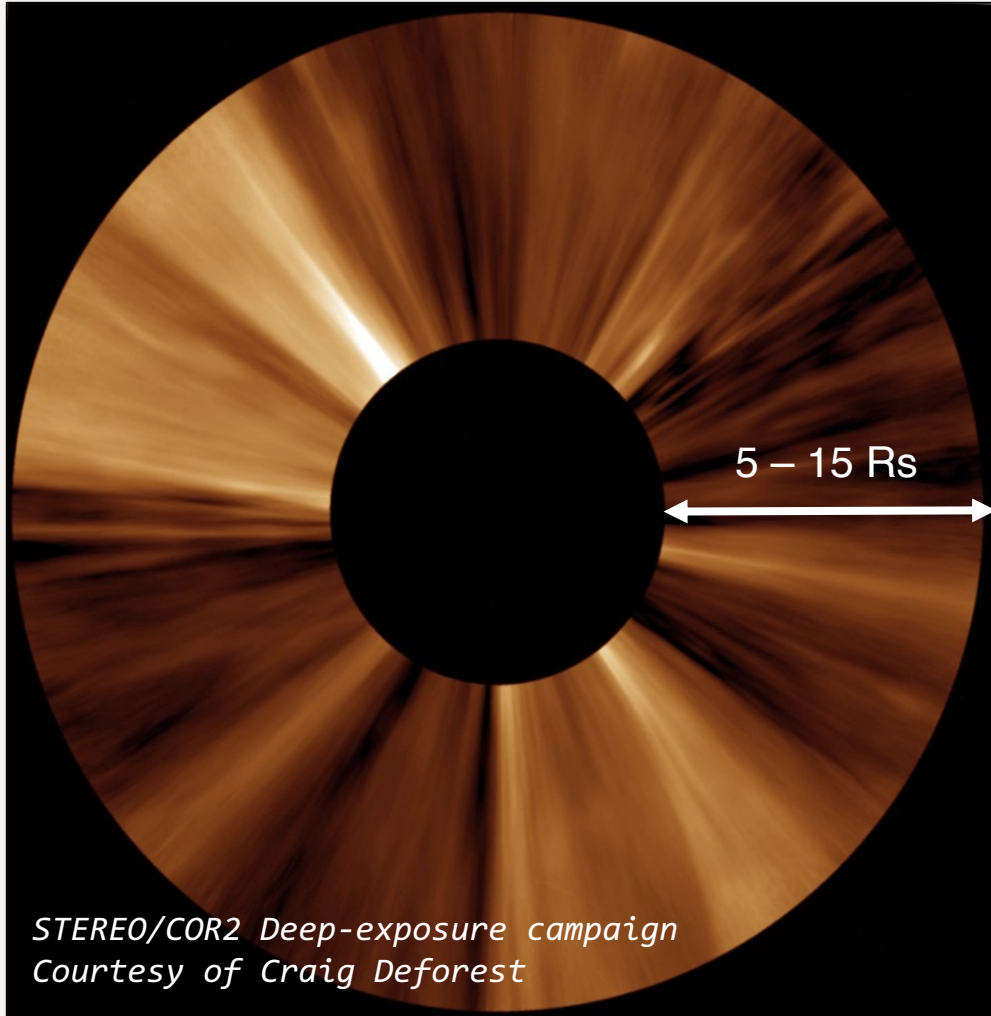
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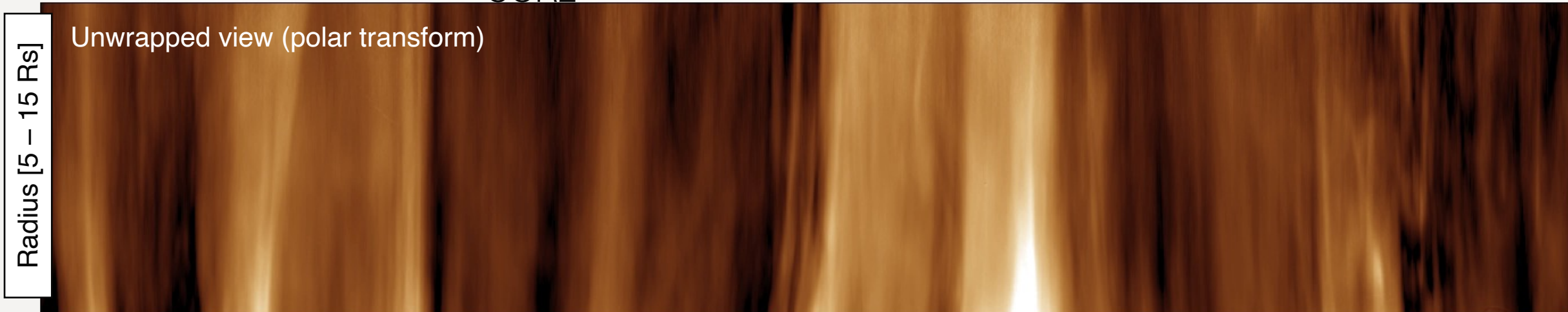


BALLTRACKING APPLIED TO STEREO/COR2

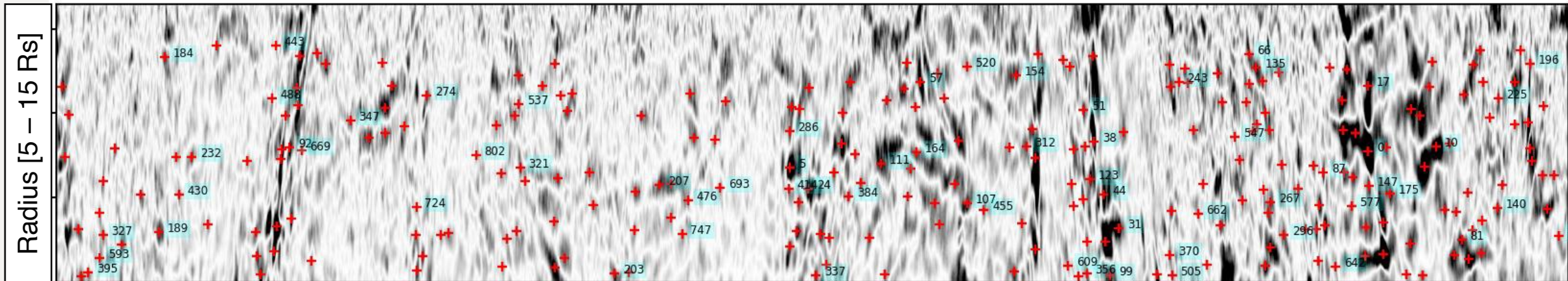
Temporal-unsharp masked (by Craig Deforest)



BALLTRACKING APPLIED TO STEREO COR2

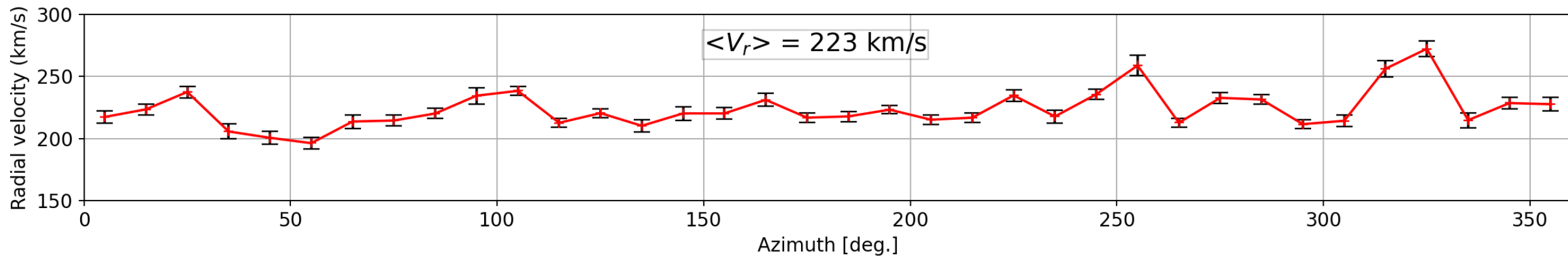


Tracking of PDS subset on L7 TUM - 2014-04-14T02:46:00 - Frame #0

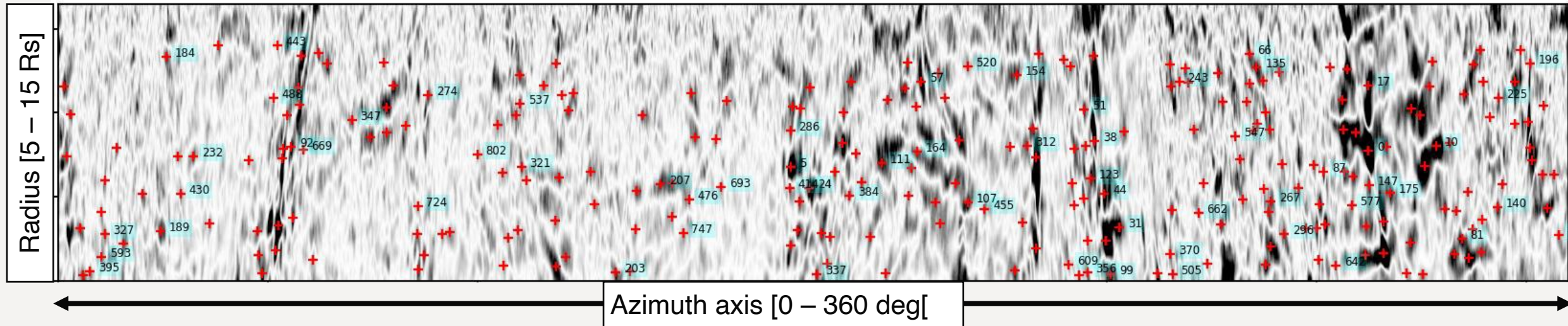


Magnetic Balltracking applied to plasma density structures in the solar wind

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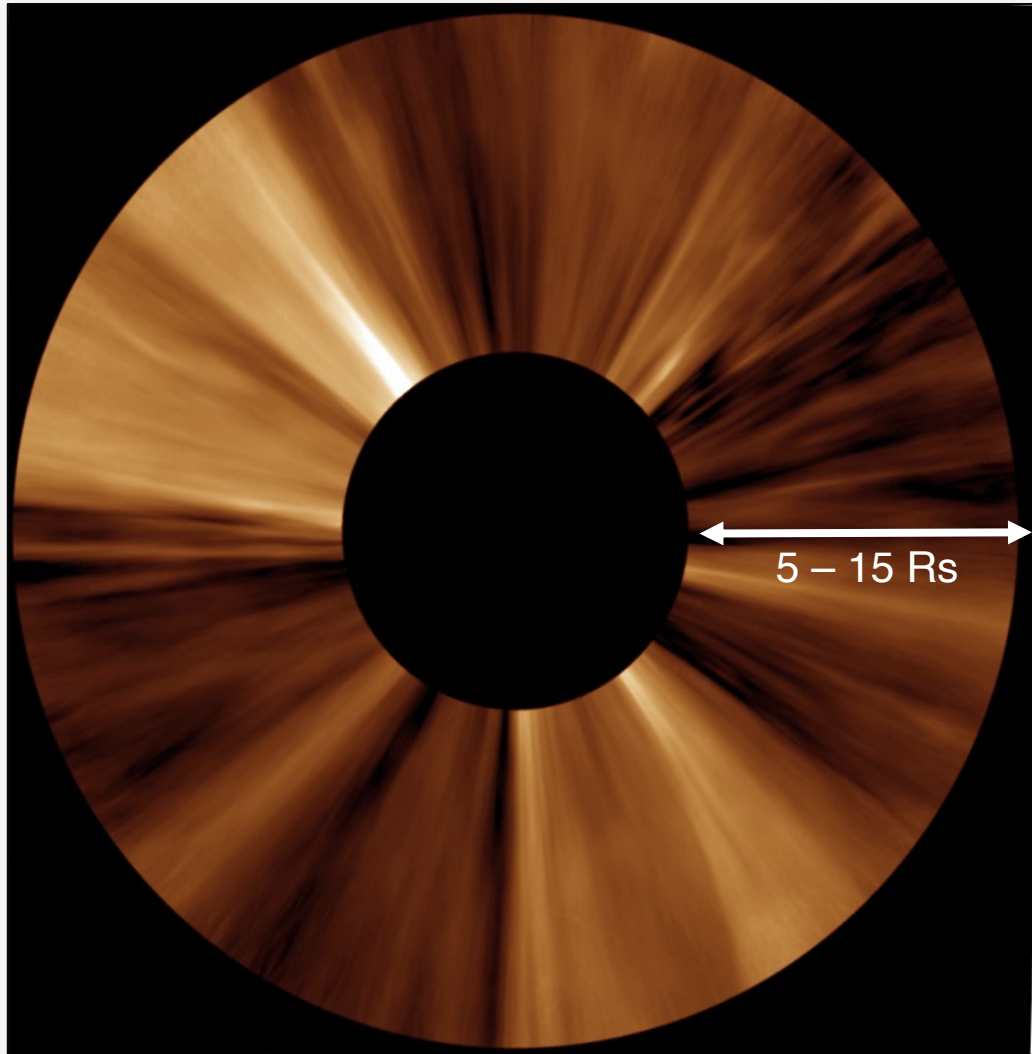


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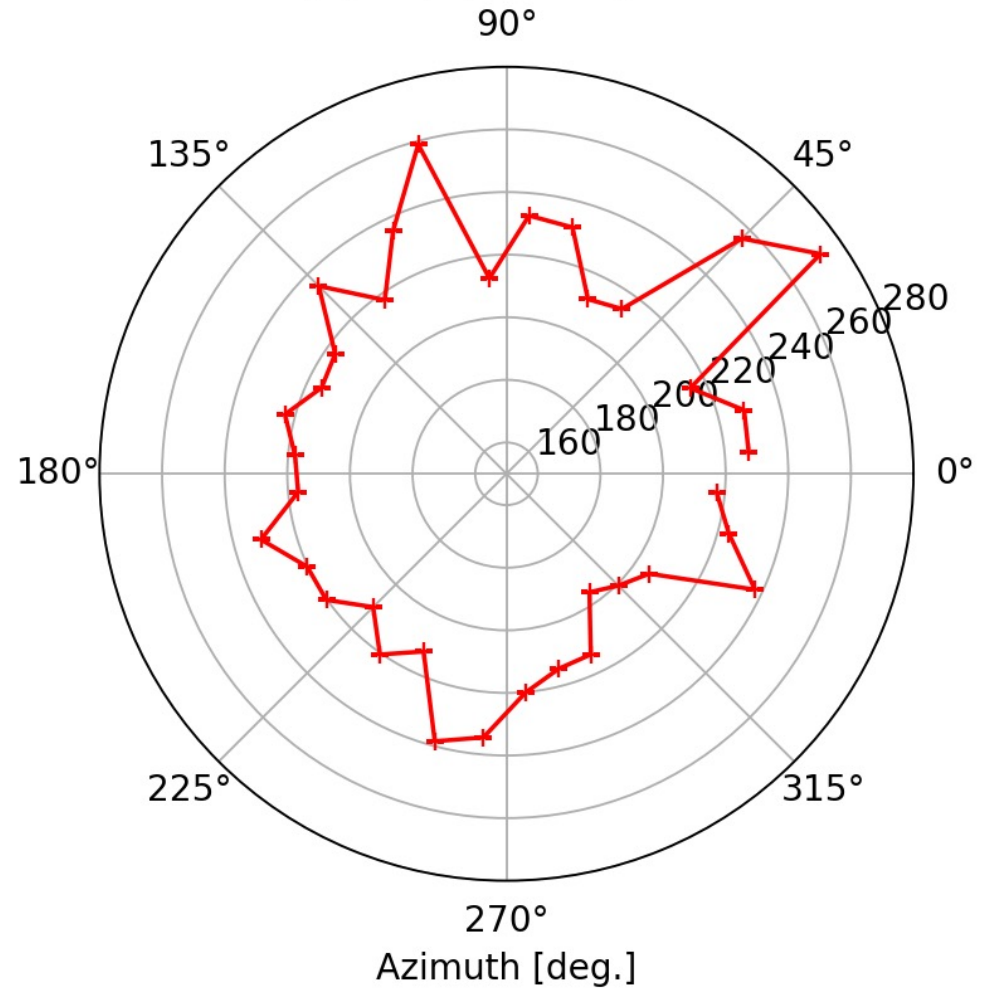


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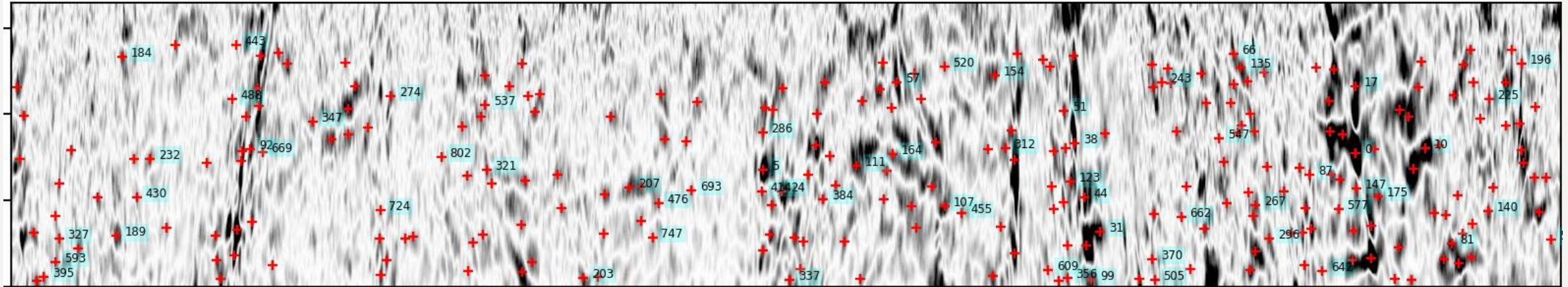


Radial velocity (km/s) averaged over ~6.6 hrs



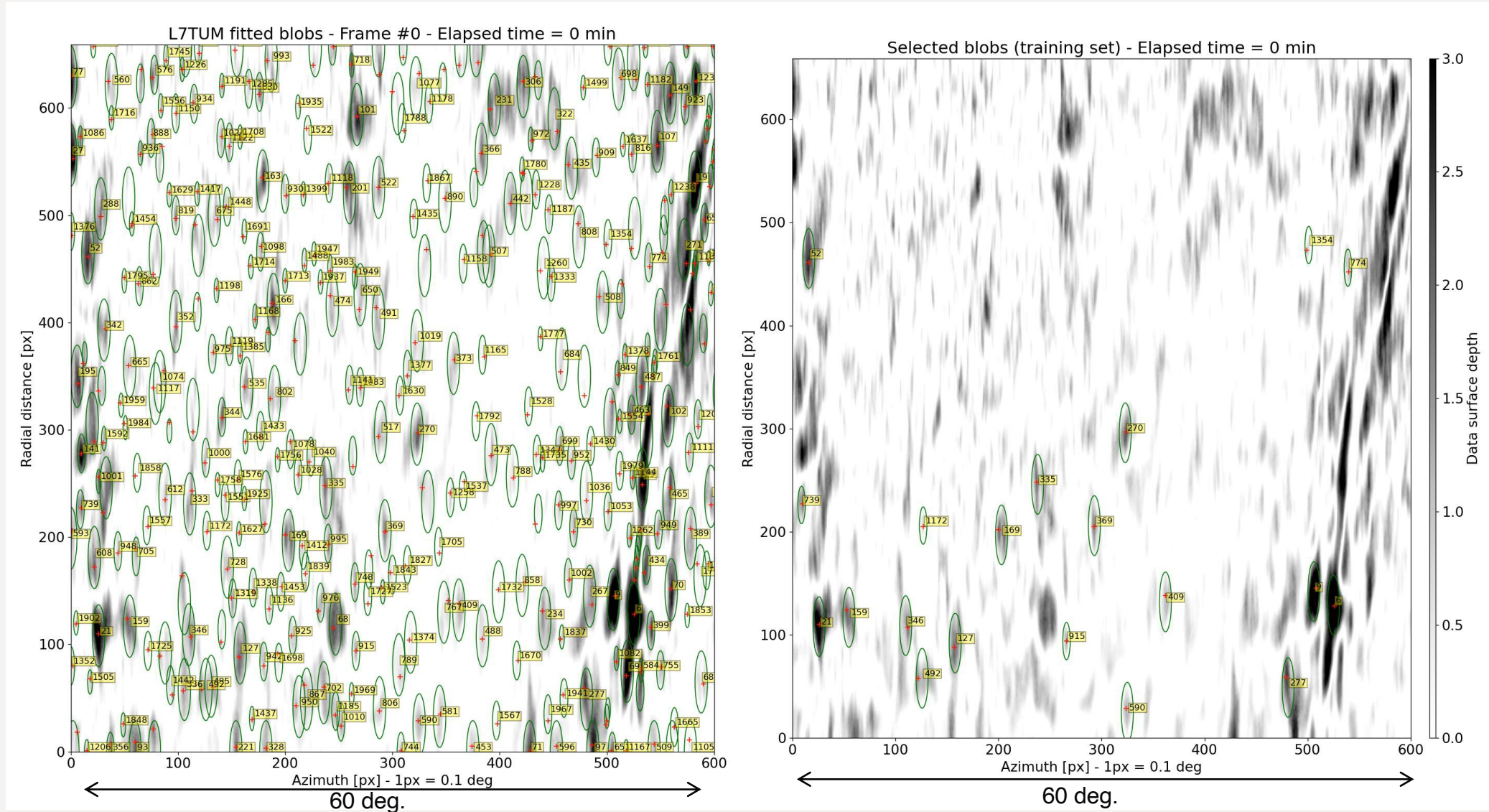
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Caveats: taken as-is, flow field still subject to 3D location uncertainty (optically thin plasma, projection effects, etc...)

Training sets: manually tracked and ellipse-fitted density structures used to fine-tune Magnetic Balltracking



Training sets:

- ✓ **Must provide density & velocity flows used as “ground truth”**
- ✓ **Necessary to tune algorithms, evaluate performance & uncertainties**
- ✓ **Statistically significant for separating Training/Validating/Testing to overcome overfitting**

- **Available:** Manually tracked density structures with quantified uncertainties from STEREO COR2
- **Available:** Synthetic datasets from Valmir Moraes Filho (SynCOM, See talk)

- **Planned:** MHD simulations: jets / jetlets (*Wyper et al. 2022, ApJL 941 L29*)
- **Planned:** GAMERA / CMEs (see talks from Anna Malanushenko and Elena Provornikova)

- input to pipeline for PUNCH-like observations (See Sarah Gibson talk)

CONCLUSION

