

# Realization of Terrestrial Reference Frame for GNSS

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ICG **WG-D**, Oct. 2010

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# OUTLINE

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- Back Ground
- TRF Realization by Multi-techniques combination
  - A-optimal regularization
  - Intra-technique combination
  - Inter-technique combination
- Compass Reference Frame simulation
- Geocenter motion from GPS

# BackGround

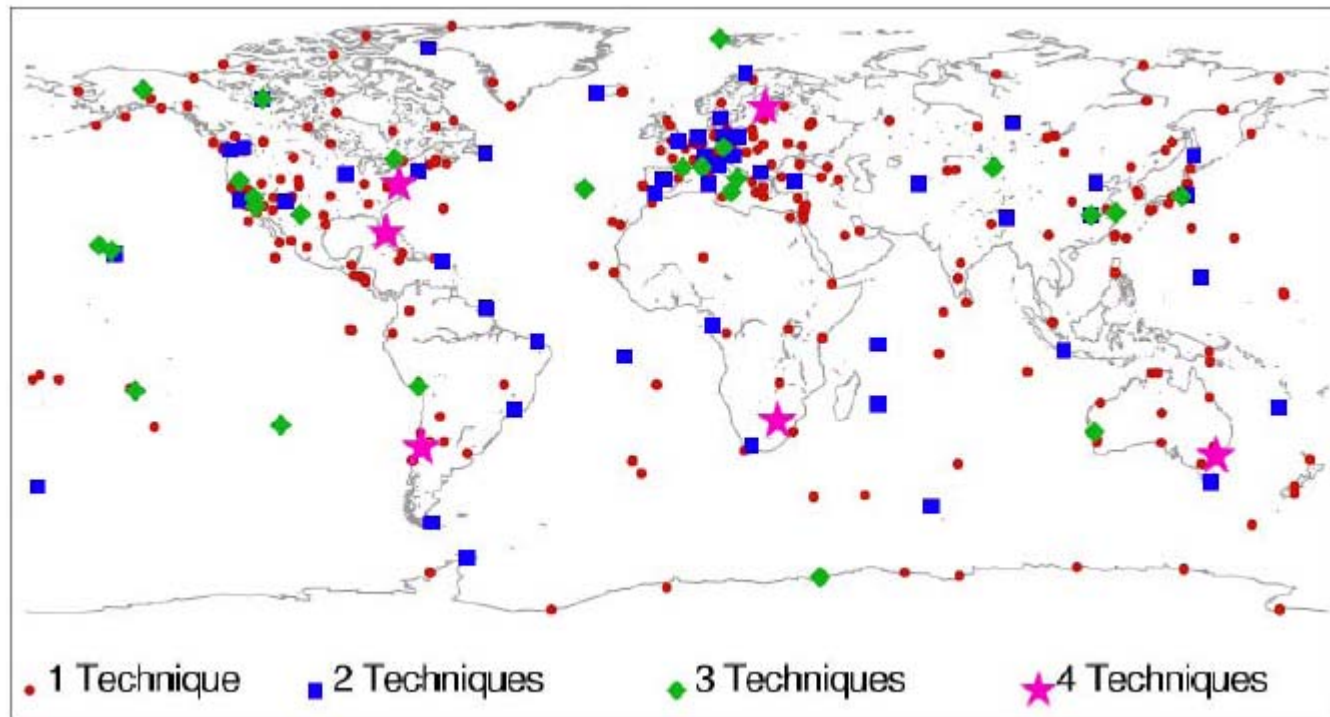
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- ❑ TRF is a basic for GNSS, each system has to develop its TRF
- ❑ TRF is complicate in definition and realization
- ❑ TRF needs data and software support from global or regional area
- ❑ TRF Realization is an important step for GNSS
- ❑ TRF has to meet all kinds of application in deferent levels of precision

# BackGround

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## □ ITRF 2005



# What's TRF

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## □ TRF

Reference Frame: Points with accurate xyz

Inputs:

Points with X Y Z, freedom (observed by GPS, VLBI, SLR)  
aprior information as EOP, some sites' coordinates

Outputs: Points with XYZ and velocity field

Transformation Parameters, EOP

Purpose: determine how these points are consistent with each other, so that they are in a family

## □ Problem in Realization of TRF?

points with freedom, Rank deficiency

# Datum Estimation

- Minimum constraints

$$(N + k^2 B^T B) \hat{x} = b + k^2 B^T c$$

Over-constrained GPS NEQ ???

- A-optimal

$$(N + \lambda \cdot I) \hat{x}$$

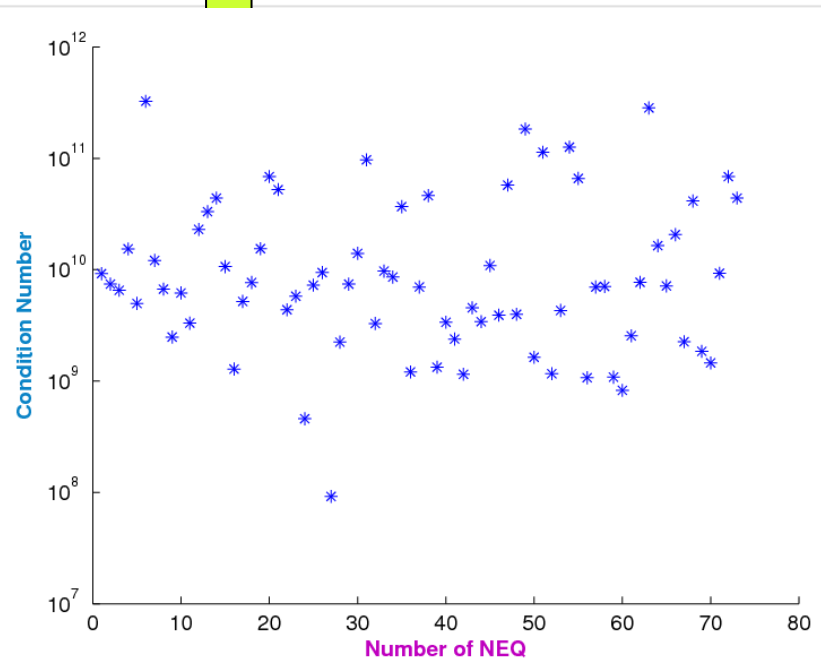


Fig. 1 Condition number of 78 GPS SINEX files

# Regularization parameter

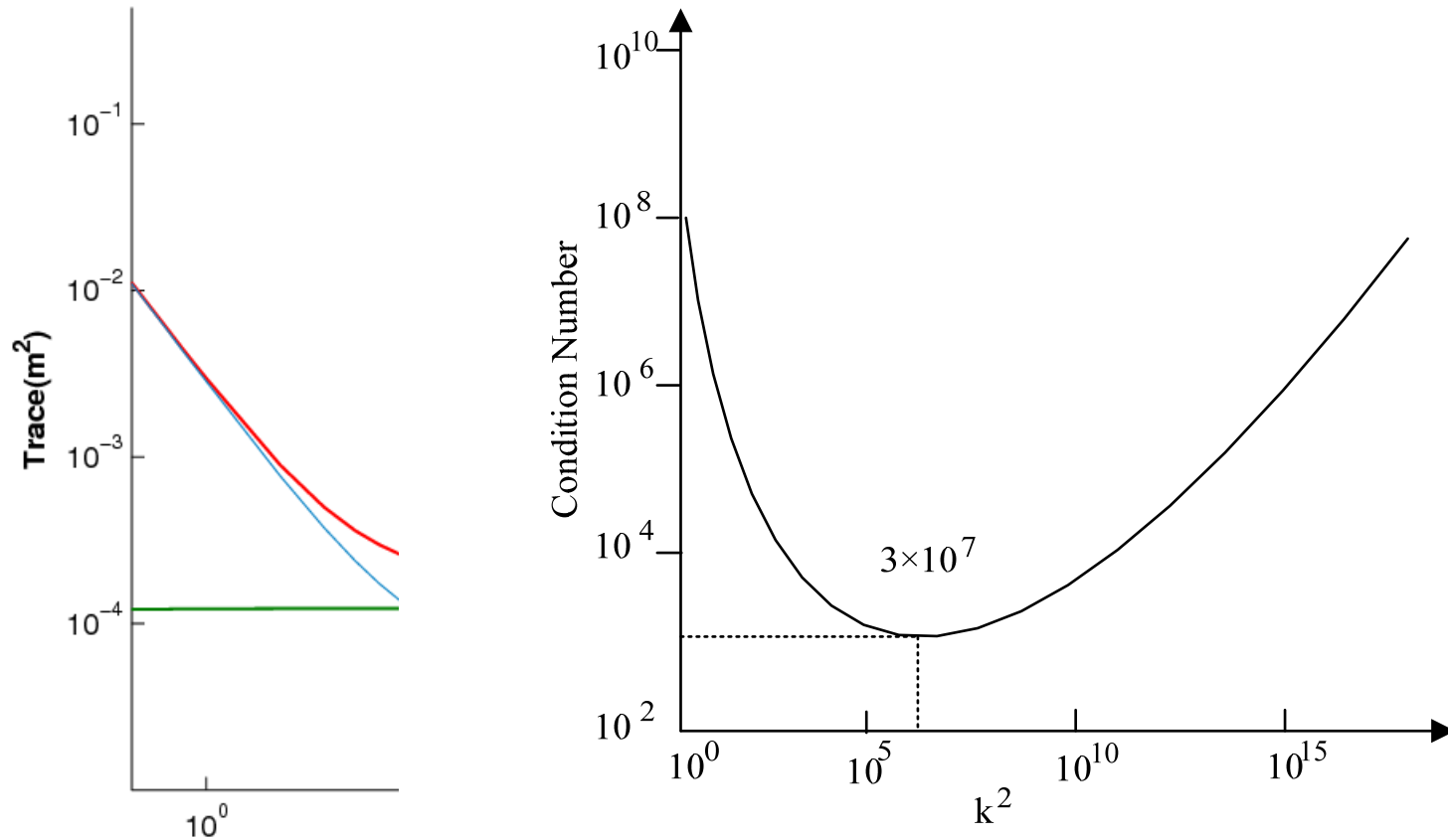
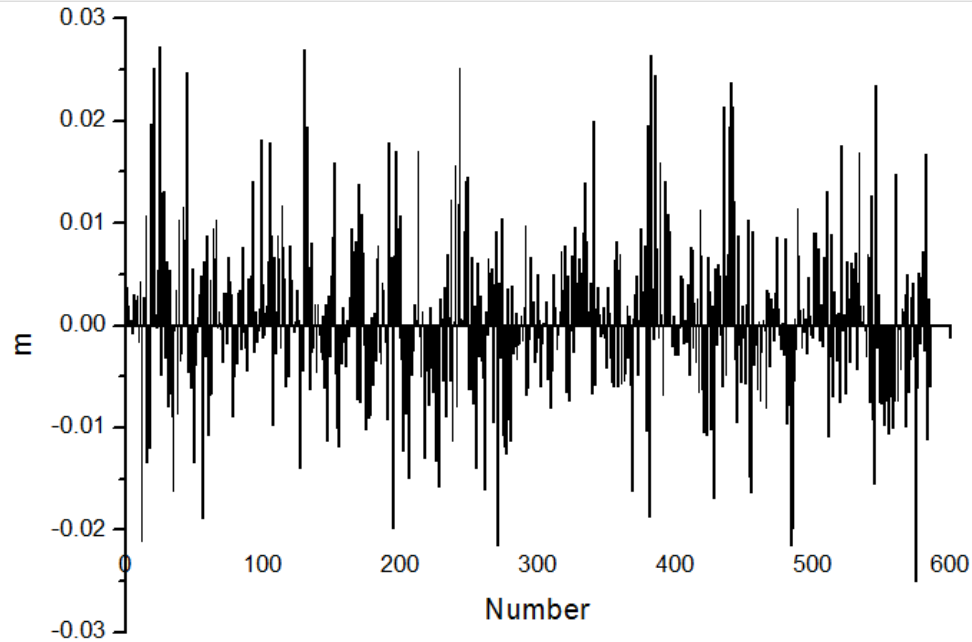


Fig. 3 Stiffness matrix regularization parameters

# Results & Analysis

Fig. 4 Differences when  $k^2=3*10^7, \lambda = 2198.21$

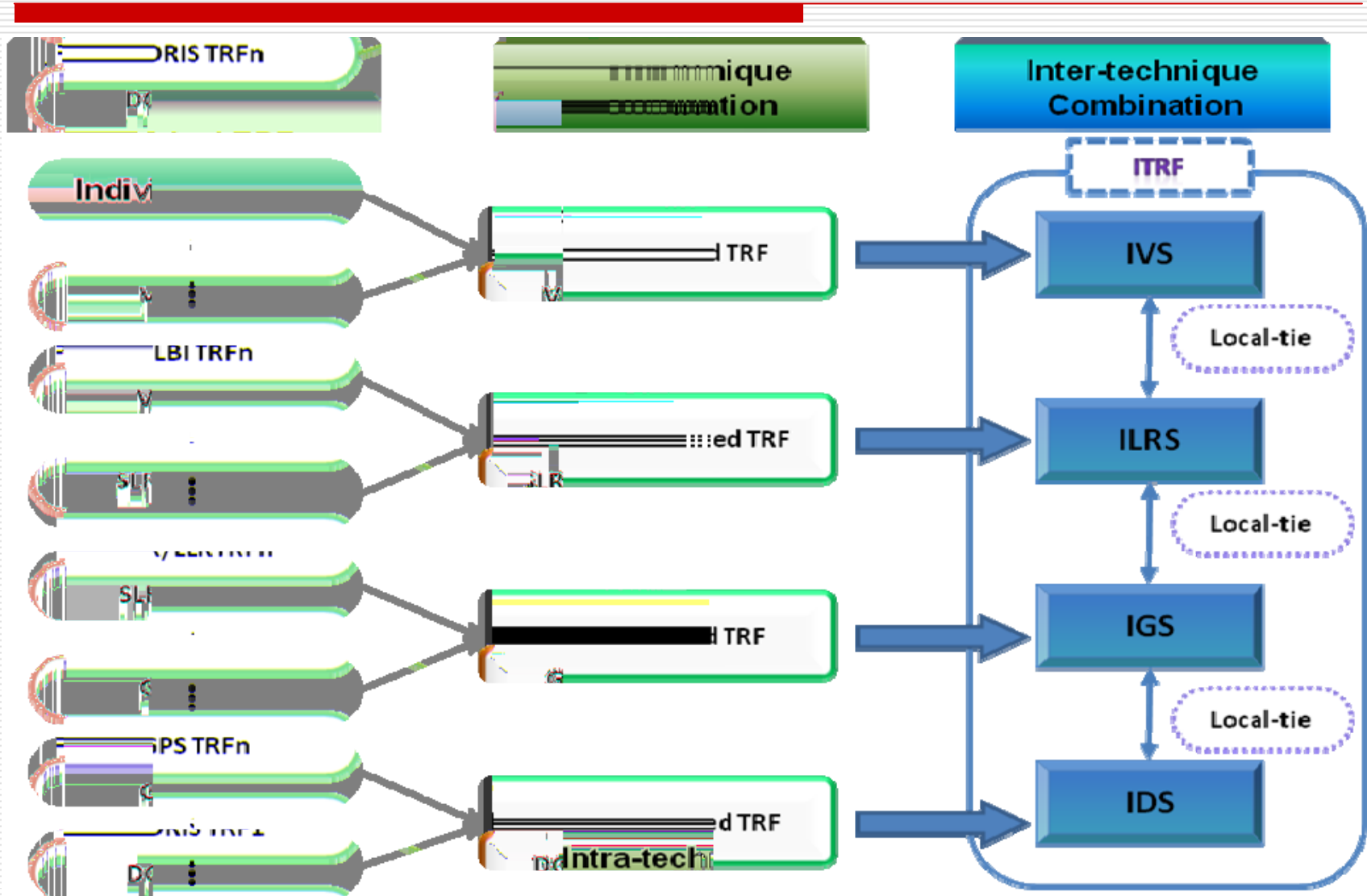


	<b>X</b>	<b>Y</b>	<b>Z</b>
<5mm	22.51%	9.76%	15.23%
5-10mm	72.38%	21.26%	45.99%
10-15mm	5.09%	48.62%	22.16%
15-20mm	0.02%	18.79%	15.62%
20-30mm	0.01%	1.53%	0.98%
>30mm	0.00%	0.05%	0.02%

Coordinate differences between two individual datum constrains are within 3cm, and 98% of them less than 2cm

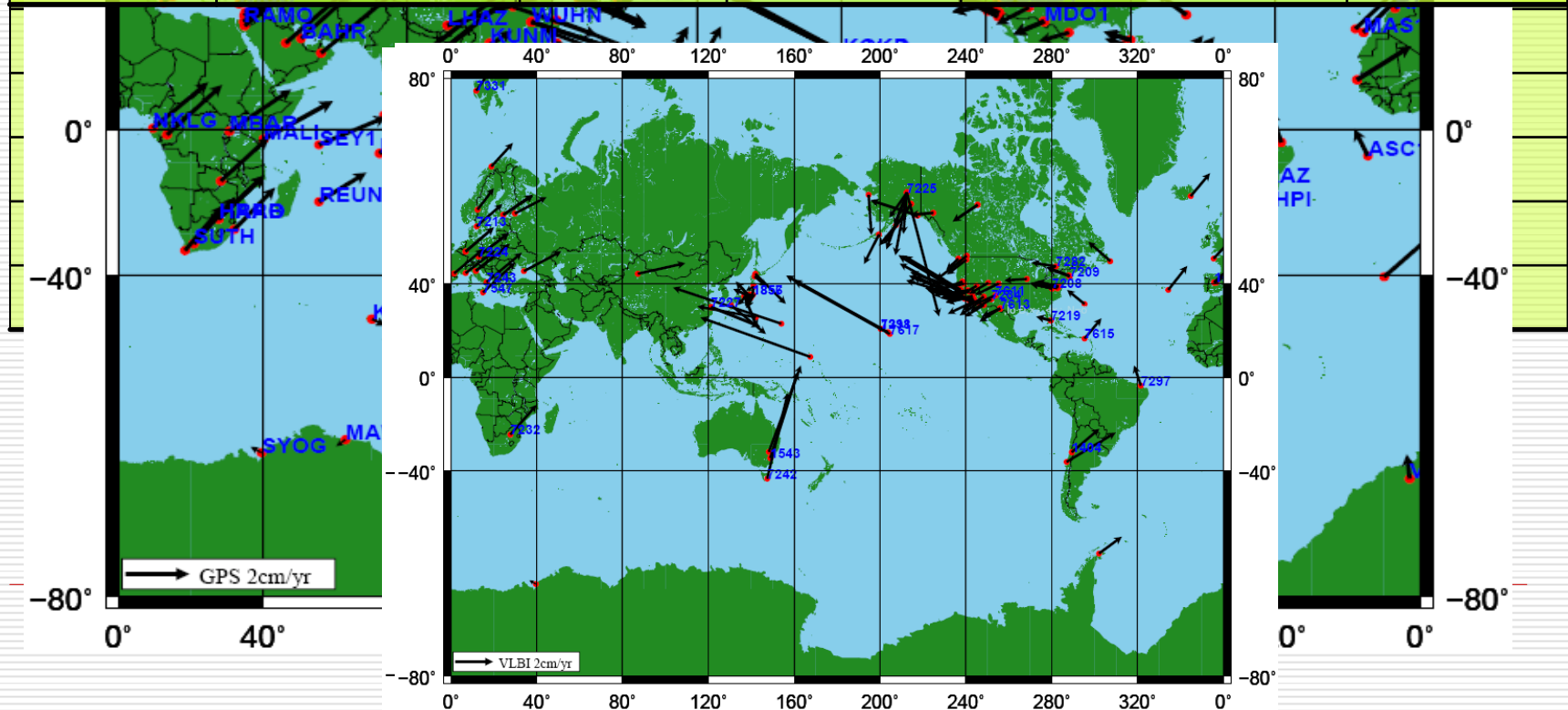


# Combination Strategy

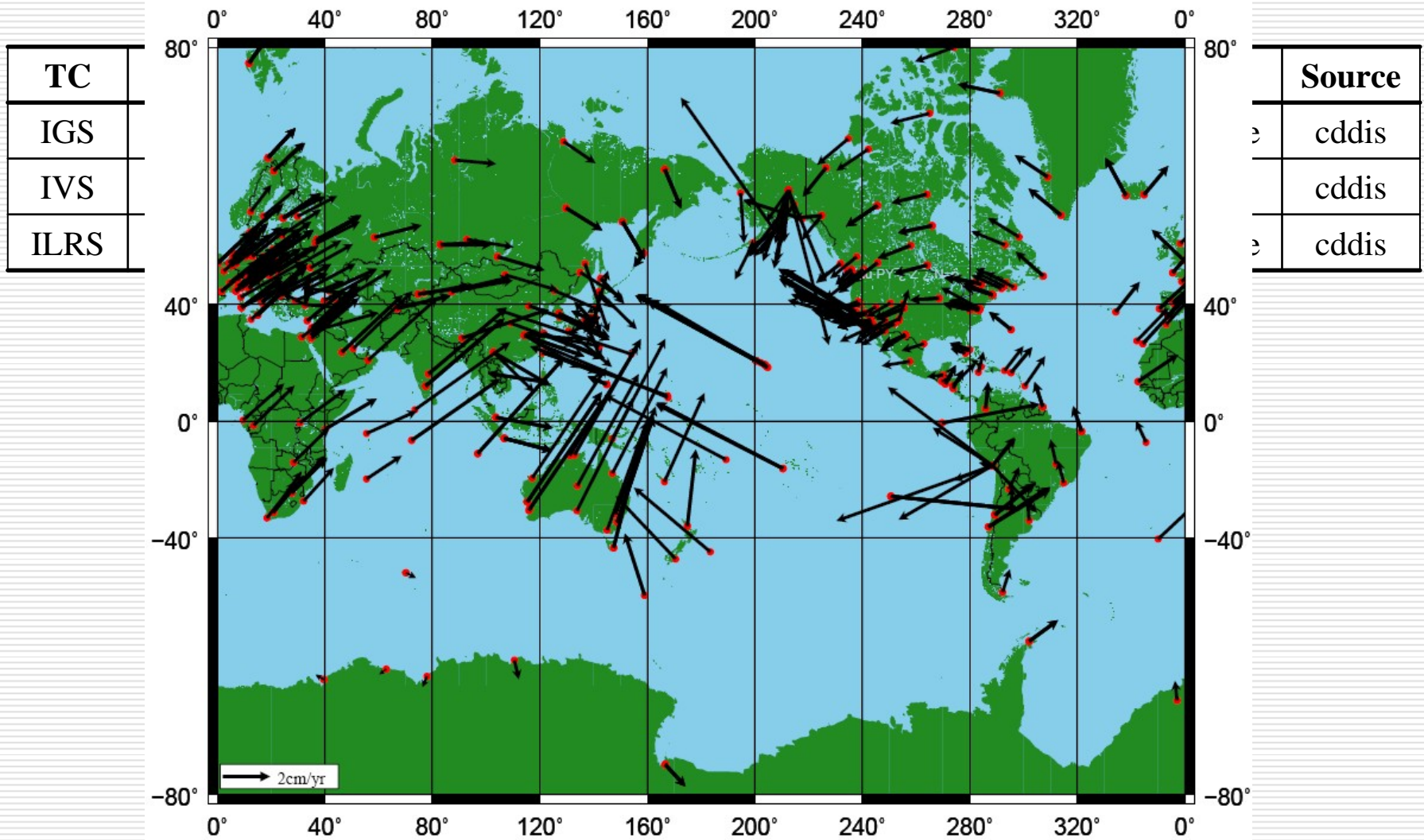


# Intra-~~SEIS~~ GPS Contribution

AC	Data-span	Station	SINEX	Constraints	Source
EASG	1993-2009	18	2.0	Loose constraint	cddis
DGFI	1993-2009	17	2.0	Loose constraint	cddis
GFZ	1993-2009	11	2.0	Loose constraint	cddis
JCET	1993-2009	20	2.0	Loose constraint	cddis
NSGF	1993-2009	15	2.0	Loose constraint	cddis



# Inter-technique Combination



# TRF Simulation Test

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- ❑ Coordinate System Definition
  - ❑ ITRS definition
  - ❑ IERS 2003
- ❑ NetWork
  - ❑ Global distributed permanent stations
- ❑ Simulation data

AC	SINEX files	Data-span
AIUB	28 Weeks	2007-2008
ESA	28 Weeks	2007-2008
GFZ	28 Weeks	2007-2008
Software	PowerADJ-→PANDA	
Remarks: GPS weeks from 1399 to 1402, 1419 to 1422, 1431 to 1434, 1443 to 1446, 1460 to 1463, 1471to 1474, 1483 to 1486		

# Results

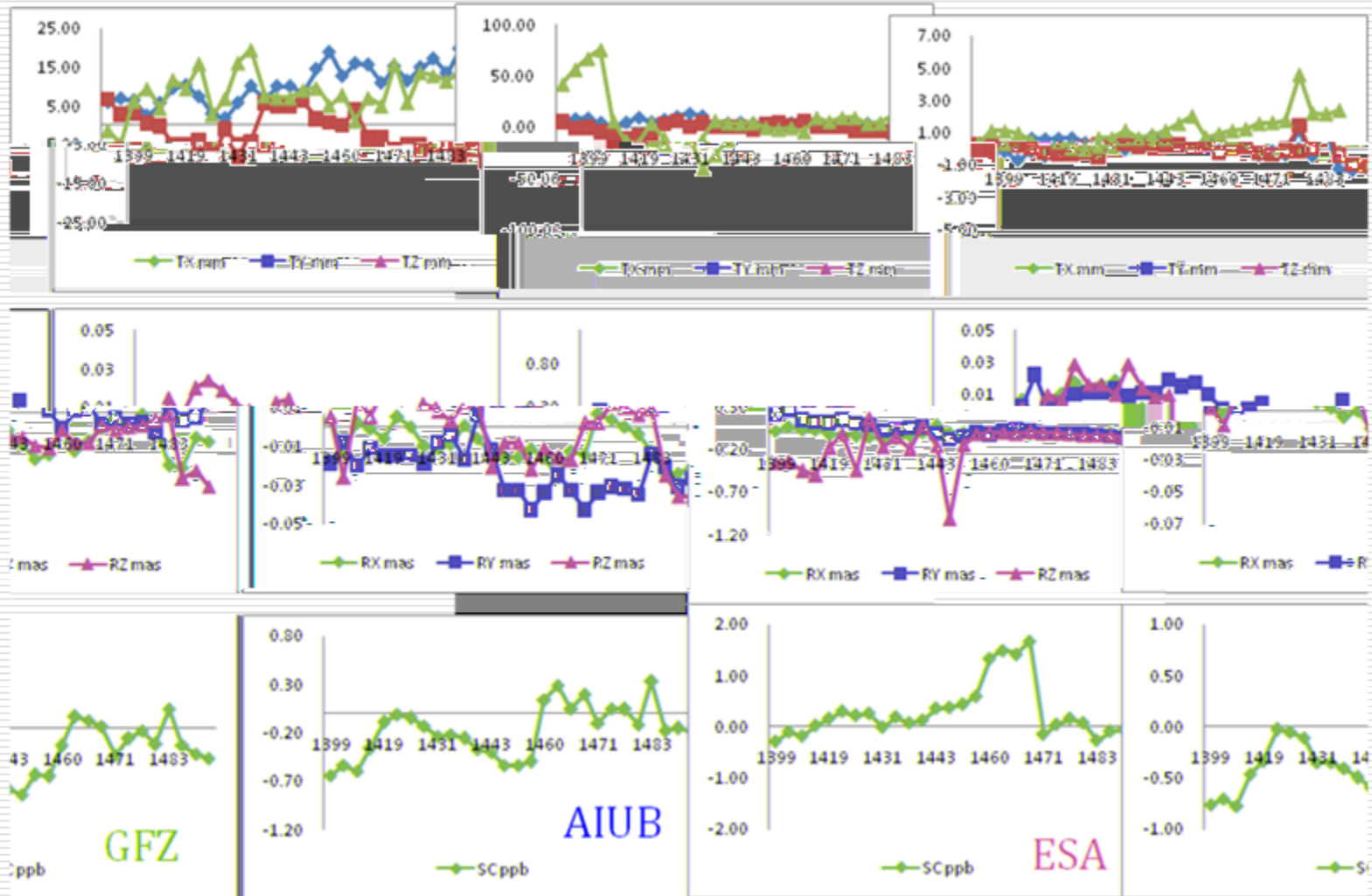
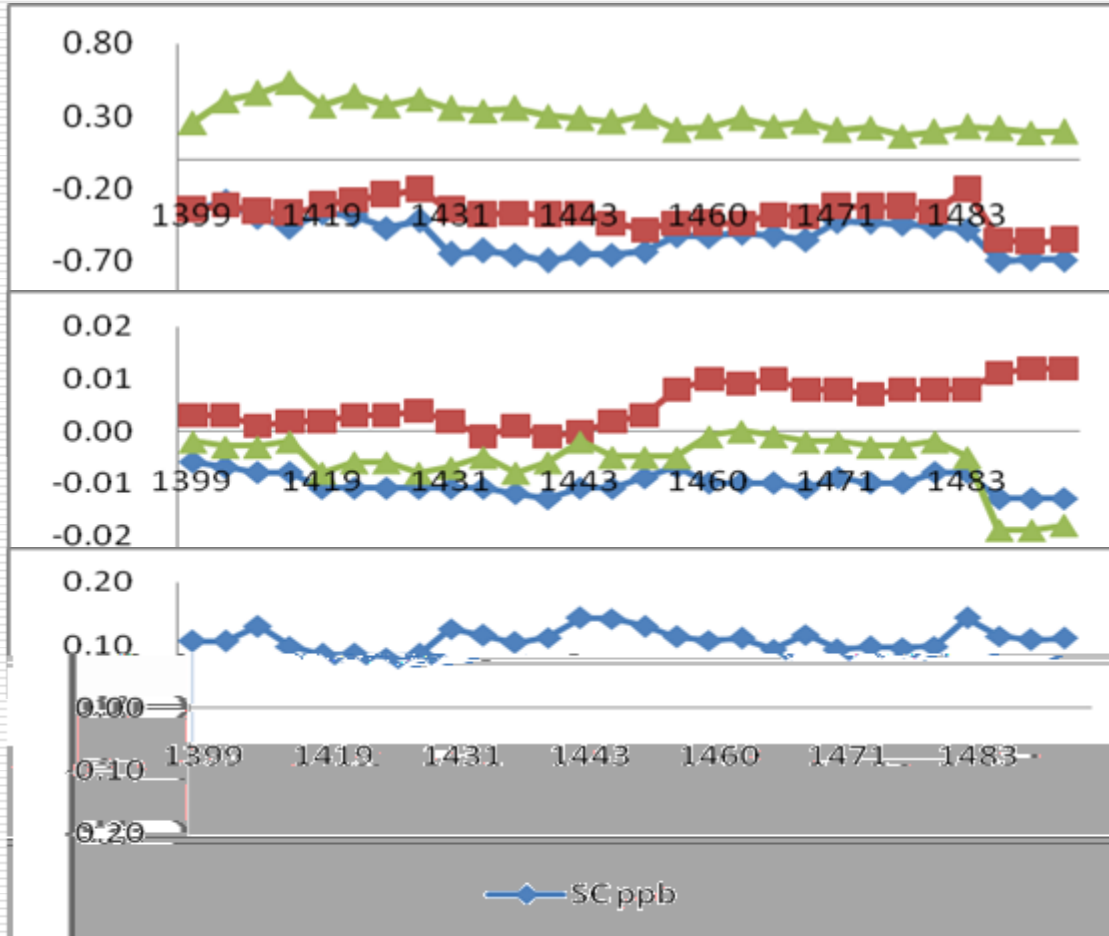


Fig. 5 Transformation parameters of each AC wrt intra-technique combination(WHU)

# Analysis



good consistency wrt  
ITRF2005

Fig. 6 Transformation parameters of WHU wrt ITRF2005



# Why Geocenter Motion?

CM

$$X_{CM}(t) = \frac{\iiint_V x(t) dm}{\iiint_V dm}$$



CF

$$X_{CF}(t) = \frac{\iiint_{\Omega} x(t) dm}{\iiint_{\Omega} dm}$$

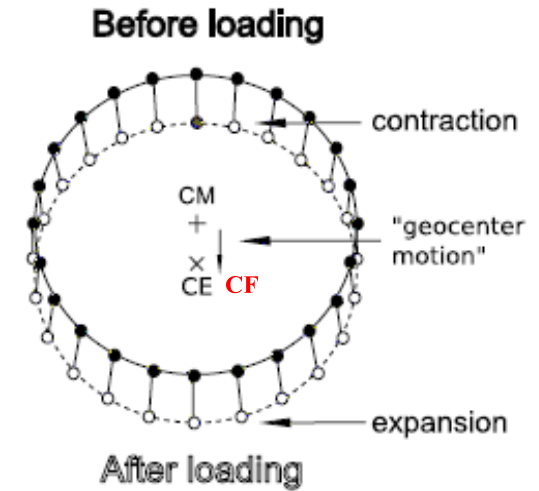
Ideal realization of CF

$$\begin{cases} T(t_0) = 0 \\ \Delta T = 0 \end{cases}$$



Origin of ITRF

$$\begin{cases} T(t_0) = 0 \\ \dot{T} = 0 \end{cases}$$



From Lavallee, 2006

- ❑ No perfect geophysical models available to constrain  $\Delta T = 0$
- ❑  $\Delta T$  : long-term, seasonal, residuals
- ❑  $\dot{T} = 0$  is long-term constraint, and in this case geocenter motion mainly shows seasonal variations

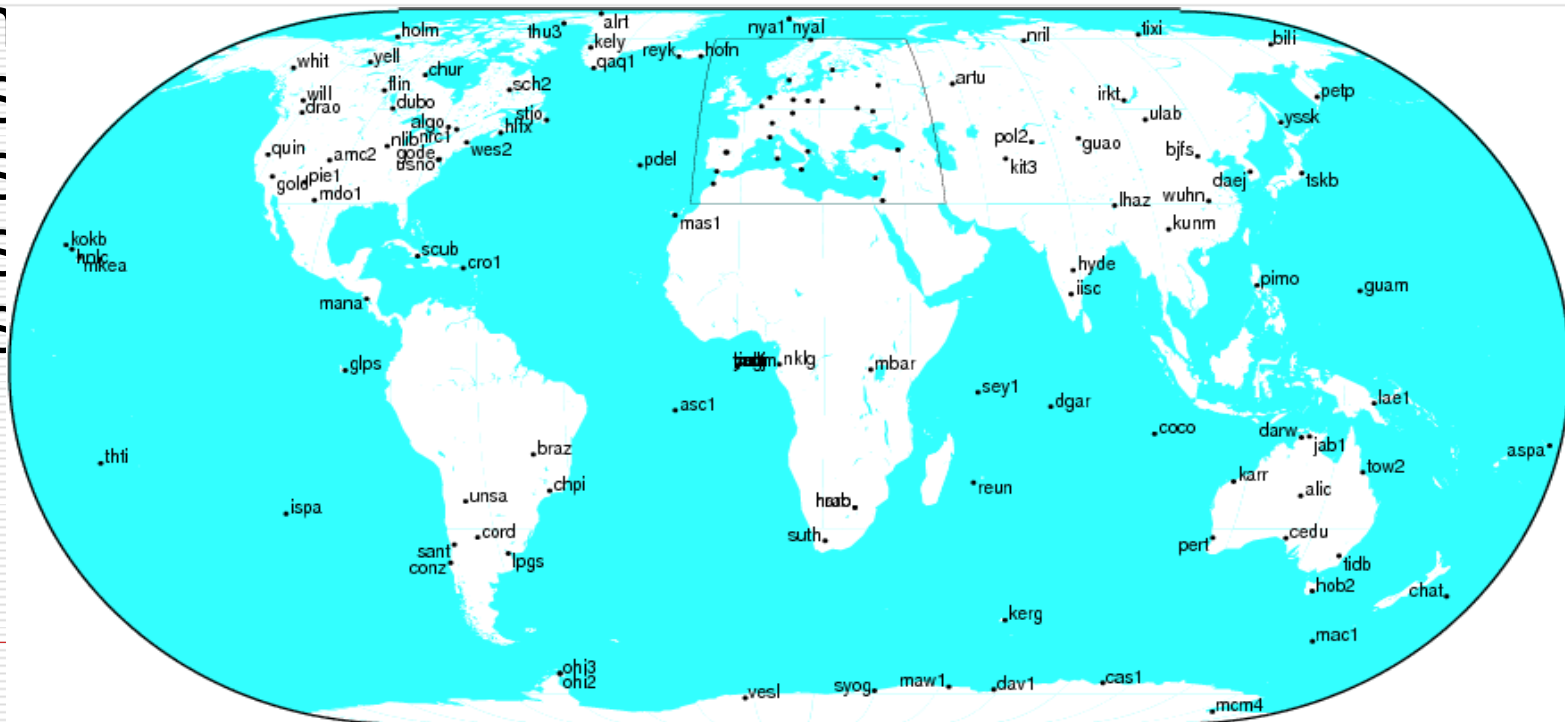
# Degree-one deformation approach

## □ Data and preprocessing

- IGS reprocessed weekly SINEX : 2000.0~2010.0
- Network: 132 reference frame stations of IGS05
- Linear velocity and jumps : IGS05\_repro.snx

## □ Sch

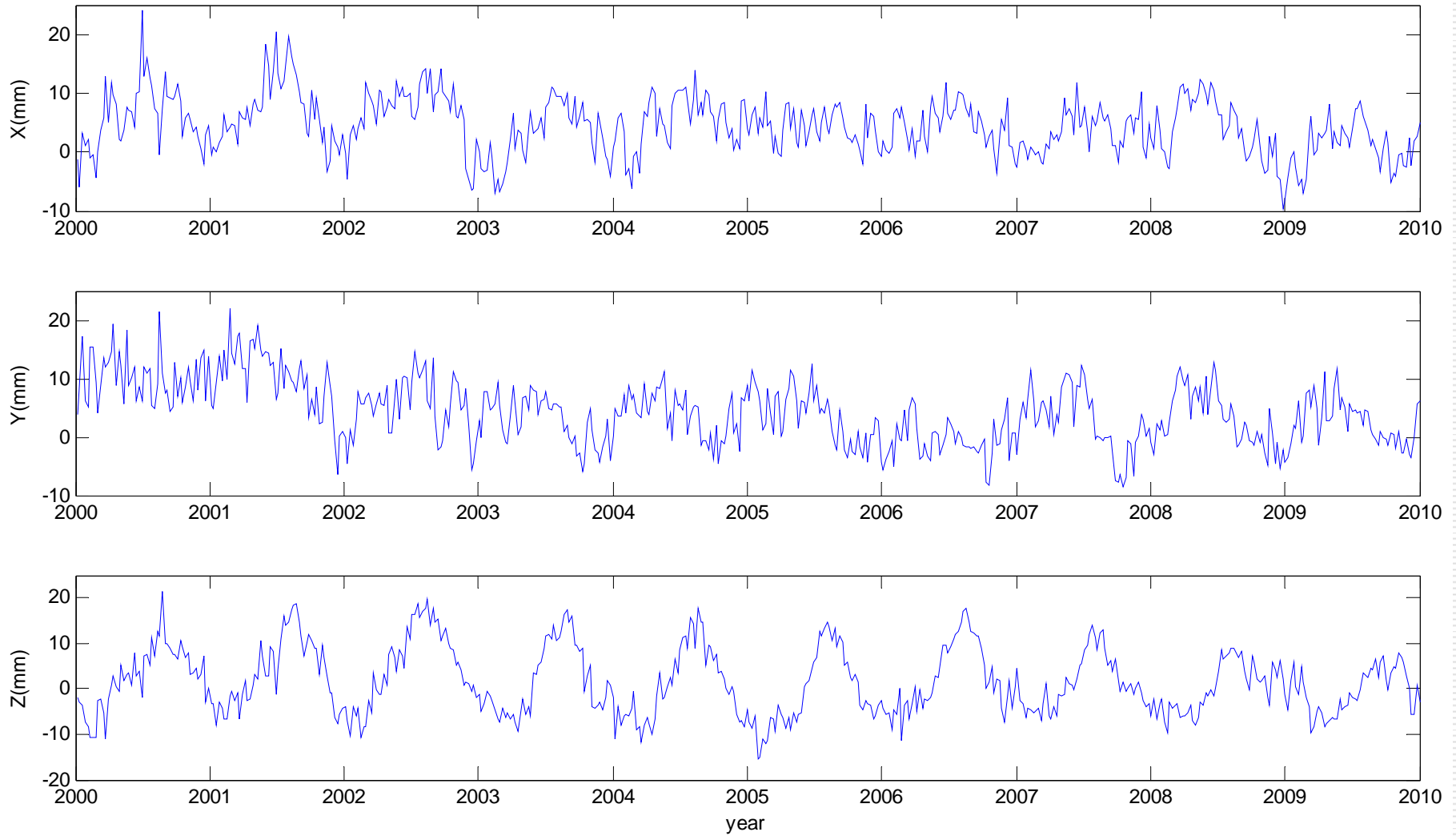
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<http://igs05.jpl.nasa.gov/>



# Results



**Fig. 7 Geocenter motion time series from scheme 2**

# Annual terms analysis

	x		y		z	
	Amplitude,mm	Phase,deg	Amplitude,mm	Phase,deg	Amplitude,mm	Phase,deg
scheme 1	$3.68 \pm 0.2$	$259 \pm 3$	$2.96 \pm 0.1$	$330 \pm 2$	$8.49 \pm 0.2$	$229 \pm 1$
scheme 2	$3.72 \pm 0.2$	$261 \pm 4$	$3.06 \pm 0.1$	$331 \pm 2$	$8.95 \pm 0.2$	$228 \pm 1$
scheme 3	$3.56 \pm 0.2$	$261 \pm 4$	$3.18 \pm 0.1$	$334 \pm 2$	$8.52 \pm 0.2$	$228 \pm 1$
scheme 4	$3.58 \pm 0.2$	$262 \pm 4$	$3.12 \pm 0.1$	$336 \pm 2$	$8.96 \pm 0.2$	$228 \pm 1$
scheme 2 <sup>b</sup>	$3.92 \pm 0.3$	$256 \pm 4$	$2.45 \pm 0.2$	$327 \pm 2$	$9.86 \pm 0.2$	$230 \pm 1$
igl	$1.93 \pm 0.2$	$89 \pm 6$	$2.49 \pm 0.1$	$144 \pm 3$	$1.98 \pm 0.3$	$294 \pm 8$
Lavallee,2006 <sup>c</sup>	$3.57 \pm 0.3$	$219 \pm 5$	$2.44 \pm 0.3$	$289 \pm 7$	$9.93 \pm 0.3$	$240 \pm 1$
Dong,2003 <sup>d</sup>	$2.1 \pm 0.3$	$224 \pm 7$	$3.3 \pm 0.3$	$297 \pm 6$	$7.1 \pm 0.3$	$232 \pm 3$
SLR <sup>e</sup>	2.60	229	3.00	320	3.55	231

## Comparison with other GPS results

### Comparison between four schemes

- ✓ Amplitude in X and Y direction agree with Lavallee, but the phase is different up to 40 degrees
- ✓ Degree-two mass load has limited effects on the annual terms, only at the land and phase in Y direction, and phase in Z direction show good consistency with SLR, but amplitude in Z direction show large differences
- ✓ The phase of scheme 2<sup>b</sup> are clearly smaller than scheme 2 in X and Y direction, encouraging to guess that phase in X and Y direction is likely not stable and that in earlier stage may be smaller

# Discussions

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- ❑ TRF Realization with GNSS, data processing technique development for Multi-GNSS era, need steps forward
- ❑ TRF alignment to international standard, need push through more application projects for GNSS performance refining, IGS as an successful experience, we need make it forward.
- ❑ We realized the estimation of geocenter motion, annual amplitude and phase of by degree-one approach is consistent with those published
- ❑ Geocenter motion is the basic problem for TRF realization for high precision applications
- ❑ Multi-space technology is important to realize TRF for GNSS

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THANK YOU !!!