

	IXPE	Ver. 2.0
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Quick Start Data Analysis Guide

Prepared by: IXPE General Observer Facility NASA, Marshall Space Flight Center

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Abstract

This document describes the Imaging X-ray Polarimeter Explorer as an aid to potential observers to propose, conduct and analyze science observations from IXPE.

Revision History

Revision	Author	Date	Change
v1.0	IXPE GOF	03 May 2023	Initial Release
v2.0	IXPE GOF	09 Feb 2024	added ixpecalcarf

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1 What is IXPE

The IXPE (Imaging X-ray Polarimetry Explorer) observatory is a NASA Small Explorer mission, in collaboration with the Italian Space Agency (ASI), providing polarimetric imaging and spectral capabilities in the 2–8 keV energy range [1]. IXPE was launched on 2021 Dec 9 into a 600-km-altitude, nearly equatorial, 96.6-minute-period circular orbit. Its 2-year baseline science mission began 2022 Jan 11 after a brief commissioning and calibration phase. IXPE began Cycle 1 of its General Observer (GO) program 2024 Feb 03. All baseline mission science data are publicly available through NASA's High Energy Astrophysics Science Archive Research Center (HEASARC). Cycle 1 science data have up to a six-month proprietary period from the time the data is first available to an observation's Principal Investigator.

The purpose of this document is to help the science community to perform basic spectro-polarization analysis of IXPE observations using publicly-available tools, to navigate the IXPE data archive and calibration database (CALDB), and to assess technical feasibility when preparing proposals through the GO program.

1.1 What does IXPE Measure

IXPE consists of three identical, co-aligned, focusing X-ray mirror assembly-detector pairs (aka telescopes) that simultaneously observe astrophysical targets. IXPE detects X-rays in the energy range 2-8 keV through photoelectric absorption in a gas. The energy, location, and time of arrival of each detected event is registered providing spectrometry, imaging, and timing measurements for an ensemble of events. In addition, IXPE works on the principle that photoionization results in an (inner shell) electron emitted preferentially parallel to the direction of the electric field vector, i.e., the polarization direction, of the incident X-ray photon. Specifically, the photoelectron angular distribution is modulated $\propto \cos^2(\phi - \phi_0)$ where ϕ is the photoelectron ejection azimuthal angle and ϕ_0 is the incident X-ray electric field vector (which is itself perpendicular to the incident photon direction of motion).

IXPE detectors are similar to classic proportional counters in that they use a gas medium to absorb incident X-rays and an applied voltage to cause the resulting electron charge cloud to drift toward an anode readout. However, IXPE's novel design [2] includes a Gas Electron Multiplier, to provide charge gain while preserving the track shape, and a finely pixellated anode (a custom ASIC readout) to *image* the photoelectron track in the readout plane perpendicular to the incident X-ray direction. The shape of, and charge distribution in, these photoelectron tracks are analyzed in ground processing to determine the location and initial photoelectron direction of each event [3,4].

1.2 How Does IXPE Operate

IXPE nominally executes a small circular dither pattern as it points toward an astrophysical target and continues in this orientation until an observation segment is complete. Very bright targets may require two or more segments separated in time to allow stored data to be telemetered. Targets can be observed continuously for a minimum duration of ~ 57 min each orbit depending on the target's inclination to the ecliptic plane. Science observations pause during Earth occultations of the target (and during brief passages through the South Atlantic Anomaly). The IXPE solar panels are fixed perpendicular to the primary axis of the observatory and must point within 25° of the Sun; thus, target visibility is generally restricted to an ~ 50 -day window twice per year.

The IXPE science program begins with a set of celestial targets and durations of observations (at a minimum). The Science Operations Center (SOC) at NASA/MSFC then turns these into scheduled programs of spacecraft actions to be executed by the Mission Operations Center (MOC) at the Laboratory for Atmospheric and Space Physics (LASP) of the University of Colorado. The MOC sends commands to, and receives data from, the observatory primarily through the ASI-provided ground station at Malindi, Kenya. The SOC then ensures the resulting data are fully recovered, processed, and validated. The processed data are delivered to the High Energy Astrophysics Science Archive Research Center (HEASARC) at NASA/GSFC where they are made available to the science community.

1.3 What are IXPE's Performance Parameters

Table 1 lists several IXPE physical parameters of interest to end-users. The three $15 \times 15 \text{ mm}^2$ IXPE focal plane detector units (DUs) are clocked 120° from each other to help eliminate any systematic effects in polarization sensitivity. With telescope focal lengths of ~4000 mm, the plate scale is approximately 1 mm = 51.6''. The pixel size is 50 μ m or 2.6''. Full, official descriptions of the IXPE observatory and instrumentation are available on the MSFC IXPE website as IXPE-SOC-DOC-011A_UG-Observatory.pdf and IXPE-SOC-DOC-008A_UG-Instrument.pdf respectively.

Table 1: IXPE System Performance.

Mirror Angular Resolution	$\leq 30''$ HPD
Effective Field of View	$12.9' \times 12.9'(300 \text{ pixel} \times 300 \text{ pixel})$
Operational Energy Range	2-8 keV
Energy Resolution	0.57 keV at 2 keV ($\propto \sqrt{E}$)
Timing	100 μ s absolute time accuracy

IXPE is sensitive to photons up to ~ 10 keV. However, the modulation response drops steeply below 2 keV due to the near-circularity of the photoelectron tracks and the quantum efficiency of the detectors (and the effective area of the mirror assemblies) decrease significantly above 8 keV. Therefore, the recommended or operational IXPE energy range is 2-8 keV.

2 How Do I Plan Science Observations with IXPE

There are publicly-available tools for estimating source counting rates, polarization sensitivity, and target accessibility that can aid IXPE observation planning. There are also on-line listings of targets observed in the past and targets planned to be observed in the near future. These tools are briefly introduced here with more details in the following subsections.

- PIMMS, the Portable Interactive Multi-Mission Simulator, is a widely used tool for estimating source count rates for high-energy observatories. For IXPE, PIMMS also calculates the sensitivity to polarization (§2.2).
- *viewing* is a simple on-line tool that can be used to determine when an astronomical position or target can be viewed by IXPE.
- The IXPE Long Term Plan and As-Run Target List are available on-line; see also §3. These lists can be useful to check if your favorite source will be or has been observed by IXPE. Note that some objects have been observed several times and/or their observation has been segmented.

In addition, *ixpeobssim* is a versatile and extensive Python-based simulation and analysis framework specifically developed for IXPE [5]. *ixpeobssim* was developed and continues to be maintained to help IXPE end users but it is not an official NASA nor ASI product. In addition to functionality equivalent to *Xselect* (§4) for IXPE data reduction and *XSPEC* (§6) for spectro-photometric analysis, *ixpeobssim* is designed to produce realistic, high-fidelity, simulated observation products in the same form and format as standard IXPE event lists. The myriad details of *ixpeobssim* are beyond the scope of this Quick Start guide. Instead, the interested reader is encouraged to consult the extensive documentation and examples available through the *ixpeobssim* website.

2.1 What is Minimal Detectable Polarization

IXPE's unique contribution to high-energy astrophysics is its ability to determine the net polarization angle (also called the position angle) of an X-ray source and the degree of polarization (also called the polarization fraction; sometimes expressed as a percentage). The standard sensitivity metric for X-ray polarimetry is the Minimum Detectable Polarization at 99% confidence level, MDP₉₉, defined (e.g., [6]) as:

$$MDP_{99} = \frac{4.29}{\langle \mu \rangle C_S} \left[\frac{C_S + C_B}{T} \right]^{1/2} \approx \frac{4.29}{\langle \mu \rangle \sqrt{N}}$$
(1)

where C_S and C_B are the source and background count rates, T is the observation exposure time and $\langle \mu \rangle$ is the source-count-weighted modulation factor. The rightmost expression holds when $C_S \gg C_B$ and the total number of detected counts $N \to C_S \times T$. The modulation factor is the amplitude of the \cos^2 distribution of the photoelectron (azimuthal) ejection directions from a 100% polarized source as measured by an instrument (while the position angle corresponds to the angle of the distribution peak). Optimal sensitivity to polarization is achieved when $\langle \mu \rangle \to 1$. In general, and for the IXPE detectors specifically, $\langle \mu \rangle$ is a function of energy (see also Fig. 2, §5).

By this definition, the MDP₉₉ is the smallest polarization fraction that can be measured at a 99% confidence level. Eq. 1 shows that measuring polarization requires a large number of events: To measure, say, an MDP₉₉ of 1% for a nominal value $\mu = 0.5$ and in the absence of any background noise requires 736,000 counts. For most astronomical sources, then, measurements of polarization will require long observations. A graphic depiction of attainable MDP₉₉ for various power law spectra against source flux in the IXPE 2–8 keV operational band is shown in Fig. 1.



Figure 1: Lines at constant observing time in the MDP₉₉ vs. flux space, for simple power-law spectra with different indices, Γ . One mCrab in the 2-8 keV range is ~ 2.1×10^{-11} erg cm⁻² s⁻¹

2.2 How Do I Estimate Polarization Sensitivity Using PIMMS

For IXPE, PIMMS returns the estimated MDP₉₉ levels, or the exposure time necessary to reach a desired MDP₉₉ level, in addition to the IXPE counting rate given a spectral model and source flux (or count rate from any of many other X-ray missions) over a user-prescribed energy range. Specifically, PIMMS returns the total (three telescopes combined) source count rate, C_S , that can be used to calculate the sensitivity to variations in the source energy spectrum or light curve. PIMMS also returns the *effective* count rate, C_E , and the *modulated* count rate, C_M , defined such that the modulation factor over the output energy range is $\langle \mu \rangle = C_M/C_E$.

Analysis shows a statistically better measure of the polarization can be made by weighting events by how well polarization can be measured (§4.1). Therefore, PIMMS uses C_E , defined as the sum of the weighted counts per unit time, instead of C_S for computing MDP₉₉ from Eq. 1.

For IXPE, PIMMS calculates MDP₉₉ for a 10 ks and a 100 ks observation. The MDP₉₉ for any other integration time, T can then be calculated by scaling by $1/\sqrt{T}$ (see Eq. 1). Alternatively, PIMMS

accepts a user-defined MDP_{99} level (as a percentage) and returns the exposure time needed to reach that value for the given input model.

PIMMS assumes source polarization properties are independent of energy. This may not be true for many astrophysical sources of interest and PIMMS may need to be queried for carefully-selected output energy ranges. In particular, the default output PIMMS energy range for IXPE is 0.5-10 keV which is most useful for estimating the total source count rate that must be telemetered. The operational energy range, 2-8 keV, should be used to estimate the IXPE sensitivity to polarization. Also, many astrophysical sources may have both a non-thermal (potentially polarized) spectral component and an unpolarized thermal or emission line component. For planning purposes, the 3-6 or 4-6 keV energy range may be appropriate, for example, if a non-thermal continuum between potentially strong thermal emission lines of Si and Fe is expected.

As always, PIMMS does not account for spectral energy broadening, source variability, nor vignetting (decrease in the energy-dependent effective area with off-axis angle) but assumes a steady, on-axis, point-like source. Thus PIMMS should be used with care (and rarely alone) when preparing proposals for spectrally-complex, extended, or time-variable sources.

3 How Do I Get Archived IXPE Data Products

The IXPE data archive is maintained by the High Energy Astrophysics Science Archive (HEASARC) at the GSFC. Unless noted otherwise, all data files are in the Flexible Image Transport System (FITS) format and follow all the relevant FITS standards and conventions. The IXPE Master Catalog, is a database table of all IXPE observations archived at the HEASARC. To display the catalog,

- 1. Select the 'Browse this table...' link in the upper left corner of the Master Catalog page to access the search form.
- 2. Use the default query settings (that is, do not put an entry in the 'Object Name or Coordinates' field) to see the complete catalog,
- 3. Select 'Start Search' at the bottom of the search form.

The search will return the full table of planned and observed targets. Data are publicly available if the 'public_date' field is set to a time in the past. Data can be retrieved by:

- 1. Selecting rows (unique Observation Sequence Numbers) of interest from the results table,
- 2. Selecting desired data from the Data Products list (e.g., IXPE Level 2 Data (ixpe.obs.l2)), and
- 3. Choosing a retrieval option (e.g., Preview and Retrieve).

Note that a given target may have multiple table entries corresponding to separate observations of the same target. Also note that IXPE data files, especially Level 1 and housekeeping files, can be very large; in general, only the Level 2 data are needed for scientific analysis. Thus, selecting the 'Preview and Retrieve' retrieval option is recommended. This option gives you another chance to view and select precisely what datasets are available (and their size).

Some observations performed early in the mission had some processing issues that are captured in an ascii-formatted README file associated with the archived science data and retrievable using the following sequence:

- 1. Selecting rows (unique Observation Sequence Numbers) of interest from the results table,
- 2. Selecting 'IXPE All Data for the Observation (ixpe.obs)' from the Data Products list,
- 3. Choosing Preview and Retrieve,
- 4. Clicking on the 'DIRECTORY' link in the 'IXPE All Data for the Observation' in the Preview results table, and

5. selecting the README file (if it exists) in the resulting directory listing.

Users should always check for a README file.

Alternatively, data search and retrieval can start at the main HEASARC Browse search form by entering an object name (or coordinates or time interval), selecting the IXPE mission, and then initiating a search of available archival data. Data can then be selected and retrieved as outlined above.

3.1 What Do The Level 2 Event Lists Contain

The IXPE Level 2 science event data files contain the filtered and calibrated data used for scientific analysis. Level 2 event data file names are of the form $ixpePPnnnpp_detD_evt2_vxx.fits$ where PPnnnpp is the eight-digit Observation Sequence Number consisting of a 2-digit mission year identifier, PP, a 4-digit target ID, nnnn, and a 2-digit segment number, pp, all of which are zero-padded. D is the detector unit number (1, 2, or 3); and xx is a zero-padded 2-digit processing version number. (Typically, only the latest processing version data is available in the archive.)

The IXPE Level 2 binary table EVENTS extension contains the columns listed in Table 2 (in addition to trigger identification and status flags) where TIME is the event timestamp, PI is the calibrated (gain-

No.	Column Name	Format	Units	TLMIN	TLMAX
2	TIME	D	s		
5	PI	J	chan	1	374
6	W_MOM	Ε			
7	Х	Ε	$pixel^*$	1	600
8	Υ	Ε	$pixel^*$	1	600
9	Q	D			
10	U	D			

Table 2: IXPE Level 2 EVENT Extension Table Column Names and Numbers.

*Pixels are $2.6'' \times 2.6''$

corrected) "Pulse Invariant" event energy channel (ranging from 0 to 374 corresponding to mid-bin energies from 0.02 keV to 14.98 keV with uniform, 40 eV, binsize), and X and Y are the sky positions converted from the detector coordinate positions to the J2000 tangent plane centered on the targeted pointing (as encapsulated in their associated WCS keywords). W_MOM, Q, and U are the (pseudo-)Stokes parameters for the event ($\S4.1$) used to determine the spectro-polarimetric properties of an ensemble of events. All but the Stokes parameters are standard event table columns commonly used in high energy astronomy.

Table 3: Selected IXPE Level 2 EVENTS Extension Header Keywords.

Keyword	Sample Value	Keyword Comment
MJDREFI	57754	start mission MJD (integer part)
MJDREFF	0.00080074074074	start mission MJD (fractional part)
DEADAPP	Т	Flag indicating if dead time correction has been applied
DEADC	0.921	The ratio of LIVETIME/ONTIME values
LIVETIME	85062.977847	[s] Sum of LIVETIME column for valid GTI
ONTIME	92363.433994	[s] Engineering-defined exposure time
RA_OBJ	83.633040	Right Ascension of target in J2000
DEC_OBJ	22.01449	Declination of target in J2000

Table 3 lists several EVENTS extension header keywords of importance. These include MJDREFI and MJDREFF, the integer and fractional parts, respectively, of the Modified Julian Date reference time needed to convert TIME column values to absolute time; LIVETIME, the sum of the valid Good Time Intervals (corrected for deadtime), equivalent to the time on target or exposure time; and the target J2000 coordinates, RA_OBJ, DEC_OBJ, in decimal degrees.

A complete listing of all table columns and header keywords for all FITS file extensions for all publicly-released IXPE data files are contained in the official IXPE data formats documentation.

4 How Do I Extract Spectro-polarimetric Data with *Xselect*

The command-line FTOOLS program, *Xselect*, can be used to extract PHA spectra from IXPE Level 2 event lists as detailed below (§4.2). The main HEASoft page contains links to select and download *Xselect* and other general-use FTOOLS software, mission-specific tools for IXPE (also documented in IXPE-SOC-DOC-009D_UG-Software.pdf), and/or the *XANADU* data analysis package containing *XSPEC* as well as detailed installation instructions. See also the online *Xselect* User's Guide.

4.1 How are IXPE Level 2 Events Weighted

IXPE is an imaging spectro-polarimeter that registers individual events. As with other event list data, observers can select (filter) events by energy, celestial coordinates, time, and phase in the usual way. IXPE observers can also apply weighting to events extracted from IXPE Level 2 event lists using *Xselect*. Weighting is based on the capability of the electron track characterization algorithm to correctly reconstruct the original photoelectron direction. This capability depends on the morphology of individual tracks; a long straight track terminating in a high surface density charge region (Bragg peak) is more likely to yield a correct photoelectron location and direction than a short track or one suffering a large-angle Coulomb scattering near the initiation point and is assigned a higher weight. IXPE scientists have found [4] the optimal weight, w_k , for the k^{th} event is a power of the ellipticity, α , of its electron track:

$$w_k = \alpha^{0.75}.$$

IXPE Level 2 data files record this weight in column W_MOM along with the Stokes parameters $Q \equiv 2\cos(2\phi)$ and $U \equiv 2\sin(2\phi)$ related to the photoelectron ejection angle, ϕ , measured, per IAU convention, counterclockwise from celestial North.

The implementation of the weighting method for spectro-polarimetric analysis is as follows. Consider a set of $k_j = 1, ..., N_j$ polarization measurements (events) within some energy bin, j, (e.g., as given by the j^{th} PI channel). The Stokes parameters for the set of events are defined as:

$$I_j = \mathcal{E}\sum_{k=1}^{N_j} w_k = \mathcal{E}\sum_{k=1}^{N_j} \text{ W_MOM}_k \qquad Q_j = \mathcal{E}\sum_{k=1}^{N_j} w_k \mathbf{Q}_k \qquad U_j = \mathcal{E}\sum_{k=1}^{N_j} w_k \mathbf{U}_k.$$

There are two variants of the weighting currently available when extracting IXPE data with *Xselect*: SIMPLE weighting following Kislat et al. ([7]) in which case $\mathcal{E} = 1/T$ and NEFF weighting, following Baldini et al. ([5]), in which case $\mathcal{E} = (1/T)(\sum_{k=1}^{N} w_k / \sum_{k=1}^{N} (w_k)^2) \equiv (1/TI)N_{\text{eff}}$ where N_{eff} is the effective number of events. Here, T is the observation exposure time. For no weighting, $w_k \equiv 1$ for all k, and the above expressions reduce to the familiar formulae:

$$I_j = \frac{N_j}{T} \qquad Q_j = \frac{1}{T} \sum_{k=1}^{N_j} \mathbf{Q}_k \qquad U_j = \frac{1}{T} \sum_{k=1}^{N_j} \mathbf{U}_k.$$

Appropriate instrument response files are available for both SIMPLE and NEFF weighting and for unweighted data analysis (\S 5).

4.2 A Walk Through *Xselect*

Xselect, under HEASoft version 6.30.1 and later, allows users to extract the Stokes I, Q and U spectra from IXPE Level 2 event lists. The IXPE observation of the blazar Mrk 501 obtained in 2022 July, Observation Sequence Number 01004701, will be used as an example. The Level 2 event lists are retrieved from the IXPE archive following the steps outlined in §3 as a single tarfile then extracted onto disk as:

> ls -l -rw-r--r- 1 owner group 3827598 Jul 27 11:07 ixpe01004701_det1_evt2_v01.fits.gz -rw-r--r- 1 owner group 3781526 Jul 27 11:07 ixpe01004701_det2_evt2_v01.fits.gz -rw-r--r- 1 owner group 3620924 Jul 27 11:07 ixpe01004701_det3_evt2_v01.fits.gz

Given a source and background 'region file' for DU1 generated by, e.g., the data visualization application DS9, here called *src.reg* and *bkg.reg*, respectively,¹ then the *Xselect* steps required to extract the source and background spectra are simply:

```
> xselect prefix=mrk501
xsel> read event "./ixpe01004701_det1_evt2_v01.fits.gz"
xsel> filter region "src.reg"
xsel> extract SPEC stokes=NEFF
xsel> save spec ixpe_det1_src_
xsel> clear region
xsel> filter region "bkg.reg"
xsel> extract SPEC stokes=NEFF
xsel> save spec ixpe_det1_bkg_
```

If a prefix is not specified at the command line, then the user will be prompted for a session name. Also, at startup, the default_mission may not be set to IXPE but the read event command will recognize the data as IXPE data and prompt the user to reset the mission. The above *Xselect* commands result in six files being generated:

```
> ls -l *.pha
-rw-r--r-- 1 owner group 63360 date ixpe_det1_src_I.pha
-rw-r--r-- 1 owner group 63360 date ixpe_det1_src_Q.pha
-rw-r--r-- 1 owner group 63360 date ixpe_det1_src_U.pha
-rw-r--r-- 1 owner group 63360 date ixpe_det1_bkg_I.pha
-rw-r--r-- 1 owner group 63360 date ixpe_det1_bkg_Q.pha
-rw-r--r-- 1 owner group 63360 date ixpe_det1_bkg_U.pha
```

Note that the data visualization application (specified by, e.g., pset xselect imagedisp=ds9) can be spawned within *Xselect* itself with the command

xsel> plot image

although the region file(s) need to be read in with the filter region command within *Xselect* in order to be applied to the event list. Note also that the region filters should either be in WCS or Physical coordinates. Regions created in Image coordinates will not work correctly if image binning is not 1.

The additional "stokes" argument supplied to the extract SPEC command for IXPE observations can be any one of:

xsel> extract SPECT stokes=NEFF
xsel> extract SPECT stokes=SIMPLE
xsel> extract SPECT stokes=UNWEIGHTED
xsel> extract SPECT stokes=NONE

¹The contents of *src.reg* are the single line circle(16:53:51.766,+39:45:44.41,60.0"), and those of *bkg.reg* are the two lines circle(16:53:51.766,+39:45:44.41,252.0") and -circle(16:53:51.766,+39:45:44.41,132.0"). The standard $60^{\mathcal{M}}$ source region size corresponds to roughly the 95% encircled energy fraction for an on-axis source.

These control the applied weighting scheme; NEFF or SIMPLE as described in §4.1 or UNWEIGHTED that sets all the weights to unity, while NONE extracts only the single, unweighted I (counts) spectrum. Similar commands to the above should be executed also for DU2 and DU3.²

$\mathbf{5}$ How Do I Get Calibrated Instrument Response Files

Spectro-polarimetric analysis of IXPE data using XSPEC requires Instrument Response Files to be associated with each spectrum. Some files are maintained in the IXPE calibration database (CALDB) system indexed and maintained by the HEASARC. Unless noted otherwise, all CALDB files are in the Flexible Image Transport System (FITS) format and follow all the relevant FITS standards and conventions. The full CALDB should be retrieved from the IXPE calibration database files page or from the CALDB supported-missions page and installed as explained in the general CALDB download and installation instructions.

Table 4: IXPE Calibration Database Files for Spectro-polarimetric Analysis*

ixpe_d1_20170101_02.rmf ixpe_d1_20170101_alpha075_02.rmf ixpe_d1_20170101_alpha075simple_02.rmf ixpe_d2_20170101_02.rmf ixpe_d2_20170101_alpha075_02.rmf ixpe_d2_20170101_alpha075simple_02.rmf ixpe_d3_20170101_02.rmf ixpe_d3_20170101_alpha075_02.rmf ixpe_d3_20170101_alpha075simple_02.rmf *File versions effective as of February 2024 are listed.

Each IXPE detector and mirror assembly has a set of associated calibration files. Specifically, there are sets of three Redistribution Matrix Files³ (RMF) for each Detector Unit as listed in Table 4: One is intended for use in unweighted data analysis and is assigned a name of the form $ixpe_dD_20170101_VV.rmf$ where D is the DU number and VV is the CALDB file version number (20170101 indicates the response file is applicable to data taken after 2017 Jan 01). The other two are used when weighting events by either the NEFF or SIMPLE weighting method $(\S4.1)$. These have names of the form ixpe_dD_20170101_alpha075_VV.rmf and ixpe_dD_20170101_alpha075SIMPLE_VV.rmf, respectively.

Spectro-polarimetric analysis of IXPE data also requires an Ancillary Response File (ARF) and a Modulation Response File (MRF) for each DU defined as the product of the energy-dependent modulation factor, $\mu(E)$, and the ARF: MRF $(E) = ARF(E) \times \mu(E)$. Previously, versions of these files were provided in the CALDB along with RMFs. As of the release of HEASoft version 6.33 (c. 2024 Feb), ARFs and MRFs are created using the mission-specific FTOOL inpecalcarf.

The *ixpecalcarf* tool builds an observation-specific ARF or MRF that correctly accounts for off-axis vignetting, a finite source extraction radius, and dither motion. The tool first makes an on-axis response from components stored in the IXPE CALDB. Corrections are then made using additional CALDB data, pointing information from spacecraft attitude housekeeping data, and the observation's time exposure information from the Level 2 event list GTI (good time interval) binary table extension.

A Walk Through *ixpecalcarf* 5.1

It is assumed at this point that Stokes I, Q and U spectra have been extracted from an IXPE Level 2 event list as outlined in §4.2, that the corresponding Level 1 spacecraft attitude data file for the observation is in hand, and that the IXPE CALDB has been properly installed. Continuing with the observation of the blazar Mrk 501, Observation Sequence Number 01004701, as an example, the following command line generates an MRF for the source Stokes Q spectrum, ixpe_det1_src_Q.pha, extracted from detector DU1 using Xselect:

 $^{^{2}}$ In general, the region files should be independently defined for each telescope; in this example, the source location has the same celestial coordinates within $0.25^{\ell\ell}$ for all three detectors so the same region files can be used for all three detector units.

 $^{^{3}}$ The instrument responses are defined on 275 energy bins corresponding to mid-bin energies of 0.02 to 10.98 keV (40 eV bins) whereas there are 375 PI channels; i.e., the RMFs are not square matrices.

```
> ixpecalcarf \
evtfile=ixpe01004701_det1_evt2_v01.fits.gz \
attfile=ixpe01004701_det1_att_v01.fits.gz \
arfout=ixpe_det1_src_Q.mrf \
specfile=none radius=1.0 weight=1 resptype=mrf
```

Here, as in §4.2, the input Level 2 event list is evtfile=ixpe01004701_det1_evt2_v01.fits. The spacecraft attitude file, part of the engineering housekeeping file suite retrievable from the "hk" subdirectory in the data archive (§3) is attfile=ixpe01004701_det1_att_v02.fits.gz.⁴ The resulting Response File is appropriate for an observation in which IXPE has been pointed so that the sky location of the target is at the center of the detector, and a 1.0' source extraction region radius (radius=1.0), and NEFF weighting method (weight=1) have been used to extract the spectrum file. (Other weighting options are weight=0 for UNWEIGHTED and weight=2 for SIMPLE). The name of the output Response File is arfout=ixpe_det1_src_Q.mrf and the type of response file is a modulation response file (resptype=mrf). Specifying specfile=none in this example prevents *ixpecalcarf* from modifying any spectral files.

A similar *ixpecalcarf* command can be used to generate an ARF for Stokes I spectra by setting **resptype=arf**. The Stokes Q MRF can also be used for the Stokes U MRF. Finally, the *ixpecalcarf* tool should be applied likewise for the three DU2 and three DU3 Stokes spectra.

There are several additional *ixpecalcarf* parameters that can be set including other ways of defining the response file type and output filename; it is recommended the user read the full *ixpecalcarf* documentation that is also accessible through the fhelp command-line FTOOL utility.

The final step before spectro-polarimetric analysis is to insure the keywords RESPFILE and AN-CRFILE are assigned the correct instrument response files for each Stokes spectrum using the FTOOL fthedit. The RESPFILE keyword should point to the appropriate CALDB RMF. and the ANCRFILE keyword should be set to the corresponding *ixpecalcarf* output as follows. For the Stokes I spectrum:

```
> fthedit ixpe_det1_src_I.pha keyword=RESPFILE operation=add \
value=" '$CALDB/data/ixpe/gpd/cpf/rmf/ixpe_d1_20170101_alpha075_02.rmf'" longstring=YES
> fthedit ixpe_det1_src_I.pha keyword=ANCRFILE operation=add \
value=" 'ixpe_det1_src_I.arf" longstring=YES
```

The operation=add parameter will add the keyword RESPFILE or modify the keyword if it already exists. Note the reference to the environment variable CALDB. For the Q and U spectra, the RESPFILE is the same as for the I spectrum but the correct ANCRFILE is the Modulated Response File:

```
> fthedit ixpe_det1_src_Q.pha keyword=RESPFILE operation=add \
value=" '$CALDB/data/ixpe/gpd/cpf/rmf/ixpe_d1_20170101_alpha075_02.rmf'" longstring=YES
> fthedit ixpe_det1_src_Q.pha keyword=ANCRFILE operation=add \
value=" 'ixpe_det1_src_Q.mrf'" longstring=YES
> fthedit ixpe_det1_src_U.pha keyword=RESPFILE operation=add \
```

```
value=" '$CALDB/data/ixpe/gpd/cpf/rmf/ixpe_d1_20170101_alpha075_02.rmf'" longstring=YES > fthedit ixpe_det1_src_U.pha keyword=ANCRFILE operation=add \
```

```
value=" 'ixpe_det1_src_Q.mrf'" longstring=YES
```

Of course, PHA file edits similar to the above should be applied also to all spectra corresponding to all three DUs. Note that, in a typical *XSPEC* implementation ($\S6$), properly-scaled background spectra are simply subtracted from the observed spectrum to obtain the source spectrum so that instrument response files are not needed for the background spectra.

Figure 2 displays a non-dithered, on-axis, NEFF-weighted ARF and an unweighted ARF for DU1 and the modulation factor for that detector. Note how the modulation factor is increased if events are weighted but that the effective number of events, and hence the system effective area, decreases. The net effect is a greater polarization sensitivity for weighted analysis. PIMMS uses the NEFF weighting to calculate MDP₉₉ (§2.2).

 $^{^{4}}$ These input files are expected to be in the local working directory in this example; otherwise, full path names should be given or soft links made. Note also the usage of the backslash line continuation character in this example.



Figure 2: Top: On-axis NEFF-weighted and unweighted IXPE ancillary response and modulation response for detector unit DU1.Bottom: Corresponding modulation factor, $\mu(E)$.

6 How Do I Fit Stokes Spectra with XSPEC

The XANADU data analysis package containing XSPEC is available for download from the main HEA-Soft page. XSPEC, version 12.12.1 and later, allows users to analyze the Stokes I, Q and U spectra from IXPE observations.

Having extracted source and background spectra for all three telescopes using *Xselect* according to $\S 4.2$, we now have eighteen PHA files with instrument response files assigned to each. It is recommended that the spectra are simultaneously fit with the same model but with some model parameters allowed to vary between telescopes. Thus, the *I*, *Q*, and *U* set of spectra for each detector are grouped (such that a single set of model fit parameters are applied to all group members):

```
> xspec
xspec> data 1:1 ixpe_det1_src_I.pha
xspec> data 1:2 ixpe_det1_src_Q.pha
xspec> data 1:3 ixpe_det1_src_U.pha
xspec> data 2:4 ixpe_det2_src_I.pha
xspec> data 2:5 ixpe_det2_src_Q.pha
xspec> data 2:6 ixpe_det2_src_U.pha
xspec> data 3:7 ixpe_det3_src_I.pha
xspec> data 3:8 ixpe_det3_src_Q.pha
xspec> data 3:9 ixpe_det3_src_U.pha
and backgrounds assigned:<sup>5</sup>
xspec> backgrnd 1 ixpe_det1_bkg_I.pha
```

⁵Note *Xselect* automatically adds a BACKSCAL and an EXPOSURE keyword to extracted spectra so that XSPEC can properly normalize the background.

```
xspec> backgrnd 2 ixpe_det1_bkg_Q.pha
xspec> backgrnd 3 ixpe_det1_bkg_U.pha
xspec> backgrnd 4 ixpe_det2_bkg_I.pha
xspec> backgrnd 5 ixpe_det2_bkg_Q.pha
xspec> backgrnd 6 ixpe_det2_bkg_U.pha
xspec> backgrnd 7 ixpe_det3_bkg_I.pha
xspec> backgrnd 8 ixpe_det3_bkg_Q.pha
xspec> backgrnd 9 ixpe_det3_bkg_U.pha
```

XSPEC contains several simple multiplicative energy-dependent polarization models. These are

- *polconst* for constant (energy independent) polarization degree and angle,
- *pollin* for polarization with a linear energy dependence, and
- *polpow* for polarization with a powerlaw energy dependence.

For example, for the constant polarization model used here, there are two fit parameters denoted A, the polarization fraction, and ψ , the polarization angle in degrees, such that the model multiplicative factors are $A\cos(2*\psi_{\rm rad})$ for the Q spectrum and $A\sin(2*\psi_{\rm rad})$ for U where $\psi_{\rm rad}$ is ψ in units of radians. The full description of all three multiplicative models are given in the *XSPEC* manual.

The model to be applied to the Mrk 501 spectra is a simple absorbed power law restricted (as per recommendation) to the 2-8 keV energy range.

```
xspec> ignore *:0.0-2.0 8.0-**
xspec> model constant*tbabs(polconst*powerlaw)
```

Note that the multiplicative polconst component applies only to the powerlaw portion of the model by design. The initial model parameters are set such that Data Group 2 and 3 parameters are tied to those of Data Group 1 with the exception of the constant which is allowed to vary for Groups 2 and 3 (== 1 for Group 1). Fitting the model to the data results in:

```
_____
```

```
Model constant<1>*TBabs<2>(polconst<3>*powerlaw<4>) Source No.: 1 Active/On
Model Model Component Parameter Unit
                                            Value
par
     comp
                           Data group: 1
            constant
                                            1.00000
   1
        1
                       factor
                                                         frozen
   2
        2
            TBabs
                                  10^22
                                            0.646199
                                                         +/- 0.103537
                       nH
   З
        З
            polconst
                                            7.45137E-02 +/- 1.80681E-02
                       Α
                       psi
                                  deg
                                                         +/- 6.99991
   4
        З
            polconst
                                            -47.4491
                                                         +/- 5.02693E-02
   5
            powerlaw
                                            2.75111
        4
                       PhoIndex
                                                              7.93573E-03
   6
        4
            powerlaw
                       norm
                                            0.106061
                                                         +/-
                           Data group: 2
   7
                                                         +/- 9.46462E-03
        1
            constant
                       factor
                                            0.955110
        2
            TBabs
                                   10^22
                                            0.646199
   8
                       nH
                                                         = p2
                                            7.45137E-02 = p3
   9
        3
            polconst
                       Α
  10
        З
            polconst
                                  deg
                                            -47.4491
                                                         = p4
                       psi
                                                         = p5
        4
            powerlaw
                       PhoIndex
                                            2.75111
  11
  12
        4
            powerlaw
                       norm
                                            0.106061
                                                         = p6
                           Data group: 3
  13
        1
                                            0.907673
                                                         +/- 9.00732E-03
            constant
                       factor
                       nH
                                  10^22
  14
        2
            TBabs
                                            0.646199
                                                         = p2
  15
        3
            polconst
                                            7.45137E-02 = p3
                       Α
```

16	3	polconst	psi	deg	-47.4491	= p4					
17	4	powerlaw	PhoIndex		2.75111	= p5					
18	4	powerlaw	norm		0.106061	= p6					
Fit st	atist	cic : Chi-S	Squared		144.82	using	149 bins,	spectrum	1,	group	1
		Chi-S	Squared		159.07	using	149 bins,	spectrum	2,	group	1
		Chi-S	Squared		119.97	using	149 bins,	spectrum	З,	group	1
		Chi-S	Squared		147.30	using	149 bins,	spectrum	4,	group	2
		Chi-S	Squared		118.64	using	149 bins,	spectrum	5,	group	2
		Chi-S	Squared		147.13	using	149 bins,	spectrum	6,	group	2
		Chi-S	Squared		147.98	using	149 bins,	spectrum	7,	group	3
		Chi-S	Squared		174.30	using	149 bins,	spectrum	8,	group	3
		Chi-S	Squared		154.01	using	149 bins,	spectrum	9,	group	3
Total	fit s	statistic	-		1313.23	with 1	334 d.o.f	•			
Test s	tatis	stic : Chi-S	Squared		1313.23	using	1341 bins				
Null	hypot	hesis proba	ability of	6.52e-01	with 1334 deg	rees of f	reedom				

6.1 How Do I Interpret the *XSPEC* Fit Results

It is advised that IXPE observers and potential proposers become familiar with the recommended practices for statistical treatment of IXPE results as addressed in the memo "Note on IXPE Statistics" [8].

There are two parameters of interest in our example. These are given by the polarization fraction, A, and polarization angle, ψ , model parameters of the **polconst** component. The *XSPEC* error (or uncertain) command can be used to deduce confidence intervals for these parameters. In particular, the 99% confidence intervals for one parameter of interest are:

where, e.g., for parameter 3, the output values are the parameter number, the 99% lower and upper limits, and (in parentheses) the lower and upper limits relative to the best fit value A = 0.0745 (7.45%). Similarly, the 1- σ uncertainty on parameter 3 is:

```
XSPEC12>error 1.0 3
Parameter Confidence Range (1)
3 0.0564509 0.0925801 (-0.0180629,0.0180664)
```

Of particular interest is the 2-D error contour for the polarization fraction and polarization angle. The following commands can be used to visualize this:

XSPEC12> steppar 1 0.00 0.21 41 2 -90 0 36 XSPEC12> plot contour ,,4 1.386, 4.61 9.21 13.81

where the first command generates a fit-statistic grid and the second draws contours at 50, 90, 99, and 99.9% confidence levels for 2D errors (χ_2^2) as shown in Figure 3.

Note that the detection is deemed "highly probable" (confidence C > 99.9%) as $A/\sigma = 4.123 > \sqrt{-2\ln(1-C)}$ where $\sigma = 0.01807$ as given by *XSPEC* above. Finally, we can use PIMMS to estimate MDP₉₉ as in § 2.2. First, use *XSPEC* to determine the (model) flux on the 2-8 keV energy range:



Figure 3: XSPEC-generated χ^2 image in (A,ψ) space where A is the polarization fraction and ψ the polarization angle for the blazar Mrk 501 obtained in 2022 July, Observation Sequence Number 01004701, with best fit values (0.0745, -47.45°) at $\chi^2_{1334} = 1313.23$ (denoted by the small cross). Contour levels are shown for confidence levels of 50, 90, 99, and 99.9% for two parameters of interest. Some plotting parameters were modified for added clarity.

```
XSPEC12> flux 2.0 8.0
Data Group Number: 1
Model Flux 0.014517 photons (7.9123e-11 ergs/cm<sup>2</sup>/s) range (2.0000 - 8.0000 keV)
Data Group Number: 2
Model Flux 0.013865 photons (7.5571e-11 ergs/cm<sup>2</sup>/s) range (2.0000 - 8.0000 keV)
Data Group Number: 3
Model Flux 0.013176 photons (7.1818e-11 ergs/cm<sup>2</sup>/s) range (2.0000 - 8.0000 keV)
```

Then enter the appropriate parameters (power law model with Galactic hydrogen column density $n_{\rm H}/10^{22} = 0.646$, photon index $\Gamma = 2.75$, and flux (average of three detectors) 7.55×10^{-11} erg cm⁻² s⁻¹ in the 2-8 keV range). PIMMS returns MDP₉₉ of 5.62% for a 100 ks exposure. Scaling by the actual mean of exposure time of 97243 s gives an MDP₉₉ of 5.70% meaning that, for an *unpolarized* source with these physical parameters, an IXPE observation will return a value A > 0.057 only 1% of the time. This is consistent with the highly probable detection deduced here of a polarization fraction of 7.45 ± 1.8%.

7 References

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