# Multi-Agent Based Simulation of the Deterrent Effects of Taxpayer Audits

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As a tool of enforcement, tax audits are thought to have both *direct* and *deterrent* effects on taxpayers. The direct effect is simply the difference between the tax liability as determined by an examiner and the amount voluntarily reported by the taxpayer. In fiscal year (FY) 2003, the direct effect of the 849,000 audits performed on individual income tax returns was a total recommended \$4.6 billion in additional tax, or an average of \$5,400 per audited taxpayer (IRS, 2004).<sup>1</sup>

In contrast, the deterrent effect is an increase in voluntarily reported tax liability due to the existence of a program of taxpayer audits. Several studies aimed at quantifying the magnitude of deterrent effects have reported ambiguous results. Panel studies using state-level data by Dubin, Graetz, and Wilde (1990) and Plumley (1996) find deterrent effects in a range from six to 11 times the direct effect. In contrast, Erard (1992) finds no improvement in compliance for a group of taxpayers who were audited in one year and, by chance, audited again two years later when compared to a control group. A field study of Minnesota taxpayers by Blumenthal, Christian, and Slemrod (1998) found that audits deter evasion by low and middle-income taxpayers but actually increase evasion among high-income taxpayers. Finally, Tauchen, Witte, and Beron (1989), using random taxpayer audit data from the 1969 Taxpayer Compliance Measurement Program (TCMP), find that raising the audit rate had an impact only on high-income wage and salary workers.

These conflicting empirical findings suggest the need for more research into the processes and conditions that promote the diffusion of deterrent effects. However, apart from a smattering of survey and experimental studies in the 1970s and early 1980s and the previously mentioned study by Erard (1992), the tax profession largely has avoided this topic. A factor contributing to the lack of research on this topic is the theoretical view that taxpayers behave *as if* the audit selection process were completely random (Allingham and Sandmo, 1972). With this assumption, each taxpayer's evasion decision is reduced to a simple calculation of maximum utility that depends only on the fraction of taxpayers audited each year and the penalty for evasion.

Alm (1999), strongly objecting to this mechanistic view of taxpayer behavior, states "...it is grossly misleading to represent a complex system by a single, so-called representative agent, who behaves in some average or typical way... This lesson is especially apt for tax compliance, [where] people exhibit a remarkable diversity in their behavior."

Researchers who study the origins of human behavioral diversity have identified several contributing factors, such as genetic variation (Jobling, Hurles, and Tyler-Smith, 2004), cultural conditioning (Nisbett, 2003), ecological

setting (Winterhalder and Smith, 2000), and mental models (Johnson-Laird, 1983). Concerning the latter, humans continuously construct mental models of reality, which include their assumptions, beliefs, experiences, and biases about the world. Since life experiences vary from person to person, even within a culturally homogeneous society, each individual's mental model of a particular phenomenon will be unique in some respects. The variation in mental models among individuals within a population could account for much of the diversity of taxpayer behavior that Alm refers to.<sup>3</sup>

An analogy from the domain of traffic enforcement may help to illustrate this point. Assume you are driving in excess of the speed limit on the interstate when you see a sign stating "Zone Patrolled by Low Flying Aircraft." How do you react? If you immediately slow down to the posted speed limit you must be acting on the belief that you suddenly have come under increased surveillance by crossing an imaginary line on the road. On the other hand, if you look around and fail to spot any "low flying aircraft" do you assume it is safe to continue speeding? The choice you make (slow down or continue speeding) depends, in part, on your mental model of the effectiveness of aerial traffic surveillance as well as other factors such as the behavior of other drivers and, perhaps, whether or not you are running late for an appointment. In the same way, when the IRS announces it will begin conducting more audits each taxpayer's response (assuming they are aware of the new enforcement regime) will reflect their unique preconception of how the IRS works along with any other information deemed relevant. These different perceptions will lead some evaders to reduce or halt their evasion while others will continue to evade as before or increase their evasion. This paper adopts the term *induced* effect to refer to a change in compliance behavior caused only by the awareness of a change in enforcement level (e.g., audit rate or penalty rate).

Apart from induced effects, a program of taxpayer audits also may promote voluntary compliance from *indirect* effects. Two categories of indirect effects have been identified in the literature: *subsequent period* effects and *group* effects. Subsequent period effects refer to an increase in taxpayer compliance following an audit. Erard (1992) examined the reporting behavior of taxpayers who were audited by the IRS and, by chance, were selected for audit again two years later. He hypothesized that taxpayers who were previously audited would exhibit greater compliance in subsequent time periods, either because the audit process teaches taxpayers how to more accurately comply or because beliefs about audit probabilities are conditioned on prior audit experience. However, Erard was unable to confirm the existence of subsequent period effects.

Despite these inconclusive findings, Erard's hypothesis of higher post-audit compliance by taxpayers seems plausible. Psychological research indicates people perceive a higher likelihood of an event if the experience is vivid or more easily recalled (Tversky and Kahneman, 1973; Plous, 1993). Continuing with our traffic analogy, motorists who get ticketed in a "speed trap" are likely to recall the incident for some time and consciously slow down when passing through the same area on subsequent trips.

The speed trap situation is analogous to third-party reporting of income which taxpayers believe (often correctly) the IRS relies on to detect underreporting. Evidence from IRS's TCMP studies shows a positive correlation between voluntary reporting compliance and the share of income subject to withholding and information reporting (IRS, 1996). Therefore, subsequent period effects are more likely to occur when taxpayers are convinced they are under continuous surveillance, such as is apparently the case with information reporting, than when surveillance is infrequent and unpredictable (e.g., a tax audit).

A second form of indirect effects, referred to here as *group* effects, results when an individual's behavior is influenced by the values and norms of his/her peers. Several survey and experimental studies have linked the propensity to evade taxes to social norms that are cultural in origin (Alm, Sanchez, and de Juan, 1995), predominant among certain professional or trade organizations (Geeroms and Wilmots, 1985) or reflect the behavior of one's neighbors (Vogel, 1974; Spicer and Lundstedt, 1976, Scott and Grasmick 1981; Grasmick and Scott, 1982).

Completing our analogy with traffic enforcement, we can recall situations when our own driving behavior was influenced by our fellow motorists. For example, when vehicles are passing you left and right on the interstate do you sometimes accelerate (beyond the posted speed limit) to match their speed? If you were driving behind a hay wagon on a two-lane road in a no passing zone, did you pass anyway? These examples and the above cited research indicate that, at times, what we consider to be acceptable (though illegal) behavior depends on what others around us are doing.

This brief discussion has touched on three characteristics of taxpayers and tax systems that likely influence how audits deter evasion. These are: 1) taxpayers' heterogeneous perceptions of the likelihood of detection and its attendant consequences; 2) existing institutional arrangements, such as information reporting and withholding, which both increase voluntary reporting and reduce the amount of unreported tax that can be detected by examining tax returns; and 3) social norms and other group influences that act to diffuse behaviors throughout a population.

Andreoni, Erard, and Feinstein (1998) note that experts generally agree on the importance of these factors for understanding taxpayer behavior but disagree on how to incorporate them in existing models of evasion.<sup>4</sup>

In recent years, several authors have developed tax evasion models using techniques of multi-agent based simulation (MABS) (Mittone and Patelli, 2000; Davis, Hecht, and Perkins, 2003). This paper takes the view that computational simulation appears to offer the most promising approach to combine the three behavioral and institutional factors identified above with the core elements of established microeconomic theory. In addition, MABS models often provide a visualization capability that allows users to compare and contrast a model's output with their intuition about a problem. The capability to combine both intuition and formal rules of logic helps to produce models that are analytically rigorous yet comprehensible by non-technical users.

This paper describes the development of an agent-based computational model of income tax evasion that assumes individuals behave as utility maximizers but who also exhibit heterogeneous behavior, receive income from sources with different levels of "visibility," and whose behavior is subject to peer influences. It should be emphasized that the model, known as the Tax Compliance Simulator (TCS), does not claim to accurately portray taxpayer behavior. Rather, TCS combines both theoretical models and known empirical relationships into a decision support tool that analysts can use to investigate the possible implications of alternative compliance strategies.

The next section contains an overview of agent-based computation and reviews the existing literature on MABS models of income tax evasion. The third section introduces the TCS model and describes how specific features were implemented, such as the taxpayer agent's <sup>5</sup> reporting decision, the perception of audit risk, and agent lifecycle income. The fourth section presents a hypothetical case study that demonstrates how TCS can be used to estimate the deterrent effects of audits. The last section summarizes main points and describes plans for future development of TCS.

# AGENT-BASED MODELS OF INCOME TAX EVASION<sup>6</sup>

An agent-based model consists of individual agents (persons, households, firms) that are represented as software "objects" having multiple characteristics. These characteristics can be constants (e.g., gender), variable states (e.g., age, weight), or rules of behavior (e.g., utility function, movement). Running such a model proceeds in two stages: setup (or instantiation) and execution. During the setup stage an agent population is created and individual agents are assigned their initial values. Also at this time, the simulation parameters, such as number of iterations to perform and any stopping rules, are defined. As the model executes, agents are allowed to interact and

various statistical and graphic routines monitor what happens. Each run of a simulation generates a "solution" to the problem being modeled. However, it is necessary to rerun the simulation many times in order to check the robustness of the solutions generated by the model. An excellent introduction to the use of MABS models in the social sciences is Epstein and Axtell (1996).

Mittone and Patelli (2000) were the first to develop a MABS model of income tax evasion. Building on the theoretical work of Myles and Naylor (1996), Mittone and Patelli assume the existence of three classes of taxpayers: honest, imitative and free riders. Each taxpayer category has a unique utility function that describes its behavior. Honest taxpayers derive additional utility by conforming to the social norm of compliance (with utility being proportional to the percentage of honest taxpayers in the population). Free riders derive maximum utility from paying as little in taxes as possible. Imitative taxpayers maximize their utility by paying what other taxpayers pay (population mean). All three groups also derive utility from public sector goods and services supported by voluntary and enforced tax contributions. Individual behavior is influenced indirectly by the group via the level of utility derived from public goods and services.

In each time period during the simulation, taxpayer agents must decide whether to evade more, less or the same as in the preceding period. The decision is stochastic, but the choice probabilities depend on whether calculated utility decreased, increased or was unchanged from last time. Decision probabilities are updated each time period based on the change in total utility associated with the previous round's compliance decision.

The authors use their model to examine how aggregate evasion behavior varies with different starting mixes of taxpayers. They find that even when all taxpayers are initially honest, the absence of audits causes revenues eventually to fall to zero (except for the occasional random tax payment). This outcome results as random dips in tax payments induce otherwise compliant taxpayers to reduce their support for public goods, thus, producing a self-reinforcing negative feedback cycle that discourages voluntary tax payments.

When audits are introduced, the additional enforcement revenue increases the quantity of public goods and taxpayers' utility. The tax agency also informs taxpayers about the average amount of tax paid and the proportion of "honest" (fully compliant) taxpayers so that imitative and honest agents can correctly calculate their utility. The authors test two different audit strategies: uniform and tail auditing. Uniform auditing implies a fixed random probability of selection. Tail auditing means audits are performed only on taxpayers who report the least amount of

tax (although the article does not specify the cutoff point used). As one might expect, tail auditing is found to have a weaker deterrent effect than uniform auditing.

Mittone and Patelli programmed their model using SWARM, one of several publicly-available freeware packages designed to promote the development of agent-based applications. Others include: RePast, Ascape, NetLogo and MASON.<sup>7</sup>

Davis, Hecht, and Perkins (2003) construct a MABS model using *Mathematica* software to test the hypothesis that the diffusion of tax evasion exhibits "tipping point" behavior similar to the propagation of a disease epidemic. Tipping point behavior refers to a population that undergoes a sudden transition from one state or condition to another for a small change in the environment. In their model, the authors want to identify the audit rate at which a predominantly honest population starts evading or the reverse case where a group of evaders suddenly begins to comply.

Davis, Hecht, and Perkins also assume the existence of three classes of taxpayers: honest, susceptible and evader. First, they develop a representative agent mathematical model and determine its solutions in equilibrium. They find stable equilibria both at high and low levels of enforcement. However, the transition from one state to the other is both nonlinear and asymmetric. In other words, when the population is initially honest audit rates must fall to some extremely low level to trigger wides pread evasion. Conversely, if the initial population is comprised of evaders, the audit rate must be raised to a different (and higher) level before taxpayers suddenly become honest.

Next, the authors develop a MABS approach to determine if the solution derived analytically using a representative agent model is true for heterogeneous agents as well. In their MABS model, taxpayers start out either as honest or evading. An evading taxpayer reverts to being honest only if audited. Honest taxpayers become susceptible if they observe someone in their social network evade without being audited. The authors do not specify how agents learn about each other's evasion success, but assume information is transmitted through direct observation. Once taxpayers become susceptible, they will evade if either the audit rate or the proportion of their acquaintances that are compliant falls below some pre-determined (random) threshold. Evaders who are audited by the tax agency revert to being honest until the next time they observe an acquaintance evading.

Davis, Hecht, and Perkins find that their simulation results support the hypothesis that tax evasion exhibits tipping point behavior. However, this conclusion remains in doubt due to their model's lack of parallelism with real world conditions. For example, the authors assume only evaders are audited whereas about one in four audited

taxpayers receive a refund or owe no additional tax (IRS, 1996). Also, results from their agent-based simulation show taxpayers becoming 100 percent compliant for audit rates as low as 0.03. This finding is not supported by IRS random audit studies that show little variation in the overall noncompliance rate in the last forty years despite audit rates ranging from less than 0.01 at present to 0.05 during the 1960s (Christian, 1994).

## THE TAX COMPLIANCE SIMULATOR (TCS)

Drawing on these pioneering efforts, Bloomquist (2004a) developed a prototype MABS model of taxpayer compliance behavior known as the Tax Compliance Simulator (TCS). TCS is written in the NetLogo simulation language (Wilensky, 1999). Compared to other agent-based modeling languages that require previous knowledge of C++ or Java, NetLogo is relatively easy to learn and, therefore, well-suited for prototyping. A large collection of sample programs written by an active NetLogo user community also enables new users to learn by example.

TCS allows users to define two distinct taxpayer sub-populations having unique behavioral, income, and tax enforcement characteristics. This option permits greater parallelism with the naturally occurring world where the opportunity to evade may vary considerably from one group of taxpayers to another (e.g., wage earners versus sole proprietors). TCS enables separate estimation of the direct, indirect, and induced effects of taxpayer audits and provides almost limitless flexibility to perform sensitivity testing. Taxpayers are represented as software agents each having 29 potentially unique characteristics including income level, fraction of income visible to the tax authority, age, life span, memory, a static list of acquaintances, perception of enforcement activity, etc.

#### **Taxpayer Reporting Decision**

TCS users can declare a percentage of each taxpayer agent's income to be "visible" to the tax authorities. By default, the model assumes all such income is fully reported. By declaring some fraction of income to be "visible," the user can represent institutional arrangements, like information reporting and withholding, that positively influence the level of reporting compliance. For example, the 1988 TCMP study found taxpayers report over 99 percent of wage and salary income on their income tax returns versus only 67 percent for sole proprietor income (IRS, 1996). However, "visible" income need not be restricted to explicit tracking mechanisms, but could also encompass implicit forms of visibility, such as might be the case for businesses required to obtain a license from state or local governmental authorities (e.g., health care providers, restaurants, and bars). By having to make their presence known to government officials, some business owners might feel compelled to report income they might otherwise not reveal if they operated in complete anonymity. Users can explore the impact of different assumptions

concerning transaction visibility by adjusting two parameters, the percentage of visible income (%Visible) and the standard deviation of visibility (SD%Visible) among taxpayers. The latter parameter determines the level of variation in income visibility among the taxpayer population.

For income that is not "visible," TCS assumes taxpayers adopt the approach of standard microeconomic theory (Allingham and Sandmo, 1972) which says that a risk neutral taxpayer will evade whenever the perceived audit rate (p) and penalty rate (f) take on values that make the following expression true:

[1] 
$$p < \frac{1}{(1+f)}$$
, where  $f \ge 0$ 

Bloomquist (2003) argues that taxpayers with high compliance opportunity costs (high discount rate) are more likely to evade, ceteris paribus, than other taxpayers. In order to account for this behavior, TCS modifies the taxpayer's reporting decision by incorporating variables to account for the time lag between an act of evasion and its detection and the taxpayer's discount rate. A third variable is included that represents an auditor's ability to detect evasion. With these modifications, the taxpayer's income reporting decision becomes:

[2] 
$$p < \frac{1}{(1+g)}$$
, where  $g = (f \times d) / (1+r_i)^t$ 

In expression 2, t = number of time periods between evasion and detection, d = auditor detection rate (0 = d = 1.0), and  $r_i$  = discount rate for taxpayer i ( $r_i \sim N(r, s)$ ,  $r_i$  = 0, with r and s determined by the user). Expression 2 implies that the present value cost of evasion is inversely related as an exponent to the length of time between an act of evasion and its detection. Finally, internal IRS studies find that auditors detect only one of every three dollars of unreported income not covered by information reporting (IRS, 1996). TCS enables a user to vary the auditor's ability to detect evasion (d) to determine how this parameter influences taxpayer behavior.

How much tax is voluntarily reported by the taxpayer is calculated using equation 3 which takes into account reporting of both visible and non-visible income components.

[3] 
$$T_r = t(Y_v + ?Y_{nv})$$
, where  $? = \begin{cases} 1 & \text{if } p \ge \frac{1}{(1+g)} \\ 0 & \text{otherwise} \end{cases}$ 

In equation 3,  $T_r$  is the reported tax amount,  $Y_v$  is "visible" income,  $Y_{nv}$  is non-visible income, and t is the tax rate. The current version of TCS assumes a single, flat tax rate for all reported income. It is anticipated that a future version of TCS will incorporate actual tax rate schedules.

## **Audit Risk Perception**

Andreoni, Erard, and Feinstein (1998), among others, have pointed out that the observed level of compliance is far higher than predicted by expected utility (EU) theory. Given the low audit and penalty rates in most countries, theory suggests virtually all taxpayers should evade the maximum amount. One explanation for higher than expected levels of compliance is the tendency of people to overweight low probability events (Neilson, 2003). Bernasconi (1998) shows that if audit probabilities are transformed using an empirically-derived weighting function based on rank dependent expected utility (RDEU) theory one obtains predicted compliance close to observed levels.

In TCS, users may select either unweighted (EU) or weighted (RDEU) audit probabilities. In the latter case, default values are calculated using a single parameter RDEU transformation function with a shape parameter that is the mean of three independently estimated values for an identically-specified function (Tversky and Kahneman, 1992; Camerer and Ho, 1994; and Wu and Gonzalez, 1999). Figure 1 displays for comparison the default RDEU weighting function used in TCS (solid line), the three weighting functions from which it is derived, and the EU (linear) probability function.

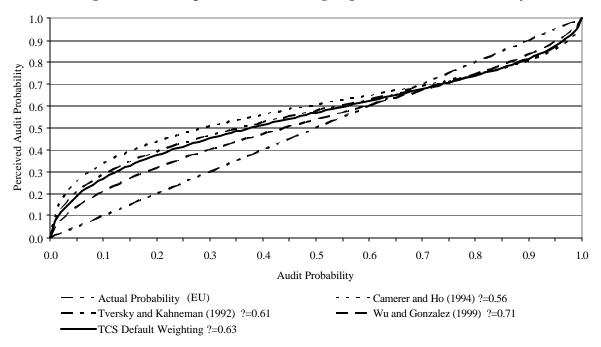


Figure 1. Relationship of EU and RDEU Weighting Functions for Audit Probability

In addition to weighting of audit probabilities, taxpayer agents are allowed to perceive a mean audit rate that is higher or lower than the actual audit rate. This might be an appropriate assumption if it is thought that taxpayers tend to overestimate the true audit probability (Harris, 1988). Whether the actual or a perceived audit rate is assumed, users can specify that all agents base their evasion decisions using the same rate (i.e., "representative" agents) or audit rates drawn from a probability distribution (i.e., "heterogeneous" agents). If heterogeneous agents are used, perceived audit rates are drawn from a normal distribution with a mean of the actual (or perceived) audit rate with a fixed standard deviation (default value = 0.03).

## **Indirect Effects and Social Networks**

TCS has an option to turn indirect effects on or off. When activated, users must specify the range of values that indicate how much audit risk perception increases when an agent is audited or when they learn that someone in their social network has been audited. Two options are available: +Random0-20 and +Random0-N. The first option tells TCS to add a random value in the range of 0 and 20 percentage points to each taxpayer's perceived audit rate when indirect effects are activated. This value is fixed throughout each agent's life span. Specifying the second option requires the user to enter a value between 1 and 100 at set-up time to indicate the maximumvalue for the additional indirect effect. Two other optional parameters related to indirect effects are the NETWORKSIZE and TIMEAFFECTED. The NETWORKSIZE slider (a separate slider for each of the two agent population sub-groups) is used to set the size of each agent's social network. If a value of zero is selected, only subsequent period effects for audited agents are modeled. If NETWORKSIZE is set to some positive and even value (say, six), then each agent's social network consists of exactly six other taxpayers. When one member of the social network is audited, the other members are assumed to hear about it and are subject to indirect effects. The TIMEAFFECTED slider (again, one for each population sub-group) is used to indicate the duration (number of time periods) of indirect effects.

Agent social networks in TCS are configured as toroids containing even-numbered sets of agents. At present, social network size is static during a simulation but can be set to different values for purposes of sensitivity testing. Figure 2 displays social networks for agent number 2 and 10 (labeled with an X) that consist of six nearest neighbors (three on each side and labeled with an n).

Figure 2. Two Social Networks in TCS

Agent	0	1	2	3	4	5	6	7	8	9	10	11
2	n	n	Χ	n	n	n						n
10	n	n						n	n	n	Χ	n

## **Taxpayer Agent Age and Income Characteristics**

The two MABS models of income tax evasion reviewed above used highly simplified taxpayer agents compared to their real-world counterparts. Both Mittone and Patelli (2000) and Davis, Hecht, and Perkins (2003) assume taxpayer agents live forever and have constant incomes. In contrast, taxpayer agents in TCS have finite lifespans with a minimum age of 16 and maximum age of 100. When an agent dies (a randomly determined event occurring after age 65) another agent having characteristics drawn from the same population sub-group as the deceased agent replaces it. In addition, TCS agents' incomes follow a typical earnings lifecycle with a peak occurring between ages 45 and 55. An agent's maximum lifetime earnings are determined by a random draw from a triangular distribution with maximum and mode specified by the user. For every time period, each agent's income is calculated as a percentage of lifetime maximum annual earnings based on the agent's current age. The relationship between an agent's age and maximum lifetime earnings is derived from data compiled by the U.S. Bureau of the Census.<sup>8</sup>

#### **Running a Simulation and Agent Visualization**

The TCS user interface screen (Figure 3) enables users to modify key model parameters using sliders, switches and choice buttons. Simulations can be run in interactive mode with full graphics display or in "batch" mode using a NetLogo option called BehaviorSpace. At first, users may want to run the model in interactive mode with a limited number of agents to set up and validate a simulation then switch to batch mode and a larger number of agents to perform the actual analysis. Users can set a target voluntary compliance rate (VCR) and gradually increment both the audit and penalty rates to identify threshold values that achieve the desired level of compliance (given the model's assumptions about taxpayer behavior). An option is available to seed the random number generator with a system-supplied value or a value supplied by the user. The latter capability is useful to examine output for possible anomalous behavior and to ensure consistency when porting the model to a new computing environment.

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Figure 3. TCS User Interface Screen

By default, agents are displayed as black or white dots (if two population sub-groups are used). Agents subject to indirect effects change shape to an arrow but retain their original color. When audited, agents temporarily change color to yellow.

During an interactive session, agents move from left to right in the graphic display area (the grey region in the center of the screen) as they approach middle age and earn more income and from right to left as they exit their peak earning years. The rightward distance traveled by each agent depends on its pre-assigned maximum annual income, with the highest earning agents moving farthest to the right-hand side of the graphics display area. Also located on the user interface screen is a histogram of the agents' income that is updated each time step.

The vertical dimension (y-axis) of the graphic display area represents voluntary compliance level. The display area has three sections: the bottom section is a zone of zero percent compliance and the top section is a zone of 100 percent compliance. Within these two zones, each agent's y-coordinate is randomly assigned, but relative income

positions (x-coordinates) are maintained. Only in the middle zone does an agent's vertical position indicate its level of voluntary compliance relative to other agents with higher positions denoting greater compliance.

#### SIMULATING THE DETERRENT EFFECTS OF TAXPAYER AUDITS USING TCS

This section presents a hypothetical example using TCS to estimate the deterrent effects of taxpayer audits. The first set of simulations illustrates how different assumptions for audit rate perception (representative agents versus heterogeneous agents) influence the simulation output. This is followed by an analysis of the deterrent effects for taxpayers with different proportions of "visible" income. A third group of simulations explores the relationship between social network size and deterrence. Finally, all three of these influences are combined to assess the relative magnitude of deterrence from induced versus indirect effects.

## Representative vs. Heterogeneous Agents

In this first example, TCS simulates the compliance behavior for a population of 300 taxpayers over 300 time periods for audit rates from 0.01 to 0.10. In one set of simulations, all agents are assumed to perceive the exact same audit rate and base their compliance decisions accordingly. A second set of simulations uses the same parameters settings as the first, but allows agents to perceive audit rates differently according to their mental models of IRS enforcement activity. In both cases, agents overweight the perceived audit rate using the default RDEU transformation. Other assumptions include: a penalty rate three times the amount of taxes evaded and no "visible" income. Figure 4 displays the output from both simulations.

Figure 4 shows that voluntary reporting compliance for representative taxpayer agents is zero for audit rates ranging from 0.01 to 0.08, but leaps to 100 percent for audit rates of 0.09 or higher. This conclusion is supported by Bernasconi (1998) who derives similar analytical results for taxpayers under RDEU axiomatics. The sudden transformation from one state of compliance to another is symptomatic of "tipping point" behavior which is the focus of the paper by Davis, Hecht, and Perkins (2003). However, such an abrupt transition from zero to 100 percent compliance does not correspond to observed taxpayer behavior.

When heterogeneous agents are used, voluntary compliance is seen to rise with each increment in the audit rate although the marginal impact is greatest for audit rates between 0.06 and 0.09. This outcome is intuitively more appealing than the off/on compliance behavior of the representative agent model. Note that while the representative agent model predicts 100 percent compliance when the audit rate equals 0.10, the heterogeneous agent model

predicts that taxpayers will only report \$.70 of each \$1 of tax due. This "tax gap" reflects taxpayers' different mental models of audit risk.

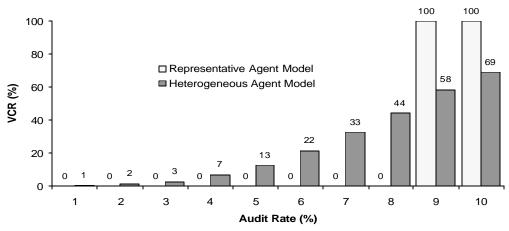


Figure 4. Voluntary Compliance Rate (VCR) by Audit Rate and Agent Type

Simulation parameters: RDEU transformation of audit probabilities (overweighting), 3x penalty rate, no visible income, 300 agents, and 300 time periods.

### **Income Visibility**

The second group of simulations illustrates the deterrent effect of audits when different proportions of income are visible to the tax authority. As previously stated, TCS assumes all "visible" income is fully reported to the tax agency similar to the observed reporting compliance behavior for wage and salary income. Therefore, increasing the percentage of visible income will shift the voluntary compliance rate upward by a constant amount.

Five groups of simulations were run for audit rates ranging from 0.01 to 0.10. In Figure 5 and Table 1, the simulation labeled "0/0" is identical to the previous simulation using heterogeneous agents. In this case, "0/0" refers to zero percent visible income and a standard deviation of zero percentage points. The simulations labeled "50/0" and "90/0" assume all taxpayer agents have exactly 50 percent and 90 percent of their income visible to the tax authorities. The two simulations labeled "50/20" and "90/20" denote where the proportion of visible income assigned to taxpayers is drawn from a normal distribution with mean 0.50 (or 0.90) and a standard deviation of 0.20. This option is included to improve parallelism with real world conditions where the proportion of income subject to information reporting varies from taxpayer to taxpayer.

Table 1 and Figure 5 show that increasing the audit rate improves compliance for all taxpayers but has a much greater marginal impact on taxpayers with no visible income and the smallest impact on taxpayers with 90 percent visible income. For this hypothetical case study, Table 1 shows that raising the audit rate from 0.01 to 0.05 increases

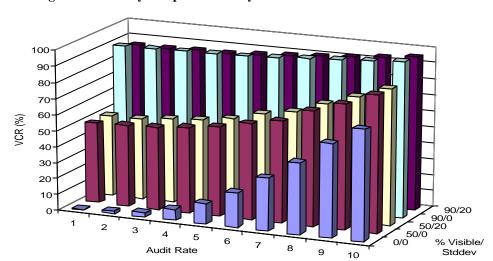


Figure 5. Voluntary Compliance Rate by Audit Rate and Percent Visible Income

Simulation parameters: RDEU transformation of audit probabilities (overweighting), 3x penalty rate, heterogeneous agents, 300 agents, and 300 time periods.

Table 1. Voluntary Compliance Rates by Income Visibility and Audit Rate: Simulation Results

% Visible/	Audit Rate										
Stddev	1	2	3	4	5	6	7	8	9	10	
0/0	1	2	3	7	13	22	33	44	58	69	
50/0	50	51	52	53	56	60	63	72	78	85	
50/20	51	50	52	54	57	61	65	72	78	85	
90/0	90	90	90	91	91	92	93	94	96	97	
90/20	87	86	87	87	88	89	91	92	93	95	

Source: Calculated by author using TCS.

voluntary compliance by 12 percentage points for taxpayers with no visible income but only one point for those with 90 percent visible income. The data in Table 1 also reveal an apparent anomaly where the VCR is seen to fall below the mean visible income level when agent values are drawn from a probability distribution. This phenomenon is evident in the lower audit rates for the simulation labeled "90/20" and is due to the fact that income visibility cannot exceed 100 percent but can be as low as three (or more) standard deviations from the mean in the opposite direction. In this example, an agent three standard deviations from a mean value of 90 would have 30 percent of income visible to tax authorities. Therefore, the disparity between the calculated VCR and mean visible income level will widen with higher levels of visible income.

## Social Network Size

The next simulations look at the impact of social network size on voluntary reporting compliance. In order to perform this analysis in TCS it is necessary to first flip the *IndirectEffects?* switch to the "on" position. This

activates a choice parameter +IEProb[1/2] and two sliders: NETWORKSIZE[1/2] and TIMEAFFECTED[1/2]. For these simulations, each taxpayer's probability of audit was incremented by a random number between 0 and 0.20 (using the +Random0-20 option for +IEProb1) and TIMEAFFECTED1 was assigned a value of 5. These settings imply that when a taxpayer is audited or discovers that someone in his/her social network has been audited, their perception of audit risk increases (by a random number between 0 and 0.20) and that this condition of elevated risk perception lasts for exactly five time periods. In addition, all simulations were executed using heterogeneous agents and assume a mean 50 percent visible income with a standard deviation of 20 percentage points ("50/20"). Finally, separate simulations were executed for agent social networks of size 0 (self only), 4, 8, 12, 16, and 20. The results are displayed graphically in Figure 6 with numerical output shown in Table 2.

From Table 2, we see the expected finding that deterrent effects increase with social network size. However, we also note that the marginal impact is greatest going from a social network size of 0 to 4. This suggests that a taxpayer's audit status need only be known by a small group of close friends (who also then act on the information) in order for sizable indirect effects to be realized.

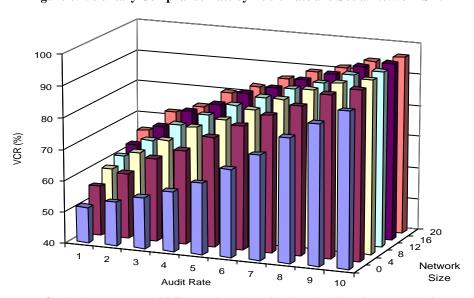


Figure 6. Voluntary Compliance Rate by Audit Rate and Social Network Size

Simulation parameters: RDEU transformation of audit probabilities (overweighting), 3x penalty rate, heterogeneous agents, 300 agents, and 300 time periods, 50% visible income, subsequent period effects last 5 periods.

Table 2. Voluntary Compliance Rates by Social Network Size and Audit Rate: Simulation Results

Social Network	Audit Rate										
Size	1	2	3	4	5	6	7	8	9	10	
Self Only	51	54	56	59	63	68	73	80	85	90	
4	56	61	67	70	75	80	84	87	92	94	
8	59	66	70	75	79	83	87	91	93	95	
12	61	67	73	77	81	84	88	91	94	96	
16	63	70	76	78	83	85	89	91	95	96	
20	66	72	75	80	83	86	89	92	94	96	

Source: Calculated by author using TCS.

## **Summary**

What does this hypothetical example tell us about the relative contributions of induced and indirect effects on compliance behavior? Recall that induced effects are defined as a change in voluntary compliance due to awareness of a change in the population audit rate. Indirect effects include both subsequent period and group effects on individual compliance behavior. In order to obtain a more precise estimate of these impacts, a final group of simulations were run each using 1,000 agents for 1,000 time periods. Table 3 displays the results for audit rates from one to five percent.

Table 3. Voluntary Compliance Rates by Source of Deterrence

Source of	Social	Audit Rate								
Deterrence	Network	1	2	3	4	5				
Induced	N/A	50	51	52	53	56				
Induced and Indirect	Self Only	51	54	56	59	63				
	4	56	61	66	70	75				
	8	59	65	70	75	79				
	12	62	68	73	77	81				
	16	64	70	75	79	82				
	20	65	71	76	79	83				

Source: Calculated by author using TCS.

N/A - not applicable.

The induced effects are shown in the top line of Table 3. Starting with a base VCR of 50 percent due to the reporting of visible income, each one point increase in the audit rate raises voluntary compliance by one point for audit rates up to 0.04 and an additional 3 percentage points going from an audit rate of 0.04 to 0.05. If only induced effects are considered, an increase in the audit rate say, from 0.01 to 0.03, would raise compliance by only two percentage points. On the other hand, an equivalent change in the audit rate would produce a ten percentage point increase in the VCR (from 56 to 66) when both induced and indirect effects for four-person social networks are considered. The difference is even greater if the audit rate is raised from 0.01 to 0.05; in this case the VCR increases

by six percentage points considering only induced effects but 19 percentage points for the combined induced and indirect effects. These hypothetical results suggest tax officials might wish to devote more attention to understanding group influences on compliance behavior. This observation is supported by preliminary findings reported in Alm, Jackson, and McKee (2004) who find that communication among experimental subjects is positively correlated with tax compliance.

#### SUMMARY AND FUTURE RESEARCH

This paper had two main goals. The first was to show how multi-agent based simulation (MABS) models provide a way to incorporate several important characteristics of taxpayers and tax systems typically excluded from analytical models of tax evasion. Such issues as taxpayer behavioral heterogeneity, variation in the visibility of income from multiple sources, and group influences on individuals can be handled easily using tools of agent-based simulation. This paper reviewed two previous MABS models of income tax evasion and provided links to web sites where interested readers can freely download software packages to develop their own MABS applications.

The second goal of the paper was to describe the development of the Tax Compliance Simulator (TCS), a prototype MABS model developed by IRS to estimate the deterrent effects of tax compliance alternatives. Key features of TCS were described including the taxpayer's reporting decision, audit risk perception, social networks, and taxpayer agent age and income characteristics. A hypothetical case study was presented that demonstrated the model's capability to estimate deterrence resulting from different assumptions concerning taxpayers' perceptions of audit probability, the proportion of income visible to tax authorities, and social network size. The simulation results suggest a significant portion of audit-based deterrence could come from group influences on compliance behavior. This finding is supported by the recent experimental work of Alm, Jackson, and McKee (2004).

Future enhancements of TCS will focus on incorporating tax year 2001 random audit data on approximately 46,000 taxpayers from the National Research Program (NRP). The NRP data will be used to define TCS agent characteristics and compliance behavior and will enable IRS researchers to model a variety of compliance scenarios using the latest data available on taxpayer behavior. However, even with this new source of information, we will still lack critical knowledge about the cause and effect relationship between enforcement activity and taxpayer behavior. For the foreseeable future, tax administrators will continue to rely on the scientific tools of research such as field studies and laboratory experiments, and now agent-based computer simulation, to inform their thinking on ways to improve taxpayer compliance.

#### **Notes**

- <sup>1</sup>How much of this recommended amount eventually is paid depends on appeals, audit reconsiderations, and other factors. For example, there were 20,399 returns with \$955 million in unagreed additional tax in FY 2003 (IRS, 2004). However, by convention the direct effect is defined as the examiner-recommended additional tax amount.
- <sup>2</sup>A recent exception is Alm, Jackson, and McKee (2004) who examine the role of communication in framing compliance decisions.
- <sup>3</sup>Alm, Sanchez, and de Juan (1995) find a correlation between tax evasion behavior and culture. However, I believe the concept of mental models provides a more useful theoretical construct to explain observed variation in evasion behavior among individuals within a society.
- <sup>4</sup>Rhoades (1999) develops a mathematical model of tax evasion with multi-component sources of income each with potentially different detection probabilities. However, she does not incorporate heterogeneous taxpayers or group effects in her model.
- <sup>5</sup>In the context of MABS modeling, the terms "taxpayer," "taxpayer agent," and "agent" are used interchangeably throughout the remainder of the paper.
- <sup>6</sup>The material in this section draws heavily on Bloomquist (2004b).
- Links to sites for these and many other software packages for agent-based modeling can be found here:

  <a href="http://wiki.swarm.org/wiki/Tools\_for\_Agent-Based\_Modelling">http://wiki.swarm.org/wiki/Tools\_for\_Agent-Based\_Modelling</a>.
- <sup>8</sup>See <a href="http://www.census.gov/statab/www/">http://www.census.gov/statab/www/</a>.
- <sup>9</sup>The following additional assumptions also apply for all simulations: maximum possible lifetime annual earnings of \$300,000 and modal lifetime annual earnings of \$100,000.
- <sup>10</sup>Bernasconi (1998) finds 100 percent compliance occurs for a penalty rate of 2.10 and an audit rate equal to 0.09. However, he uses an RDEU transformation function with a shape parameter of 0.56 from Camerer and Ho (1994) unlike TCS which uses a shape parameter value of 0.63 that is the mean of three independent estimates (see text). The larger shape parameter value in TCS necessitates a higher penalty before full compliance is reached.
- <sup>11</sup>Executing one simulation with 1,000 agents for 1,000 time periods requires approximately 48 seconds on a Pentium 4 PC with 1 Gb RAM running under Windows XP.

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