

Seki and Graphs

Thomas Wolf
Brock University,
St. Catharines, Ontario, Canada,
twolf@brocku.ca

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Outline

Introduction

Equivalence of Positions

Basic Seki

Generating All Basic Seki

Complicating a Seki

Challenges

More than 2 Liberties per Chain

Local and Global Seki

References

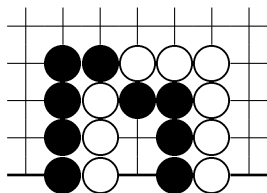
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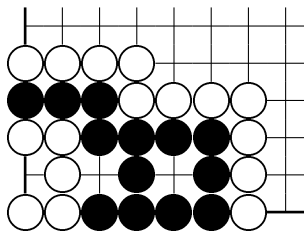
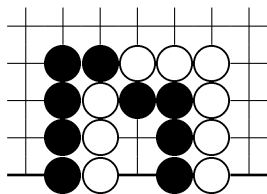
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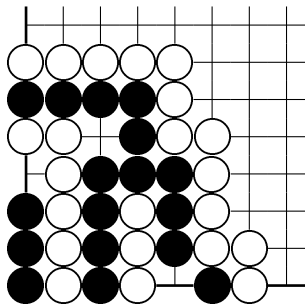
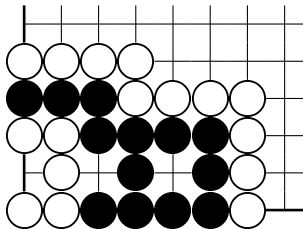
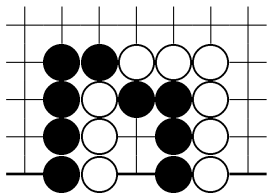
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- ▶ introduction of cuts

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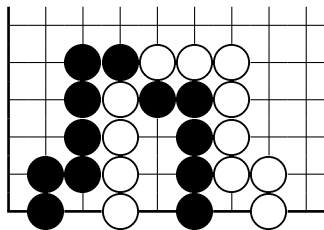
More than 2 Liberties per Chain

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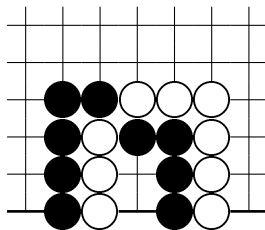
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Non-terminal Positions

We are only interested in terminal positions.



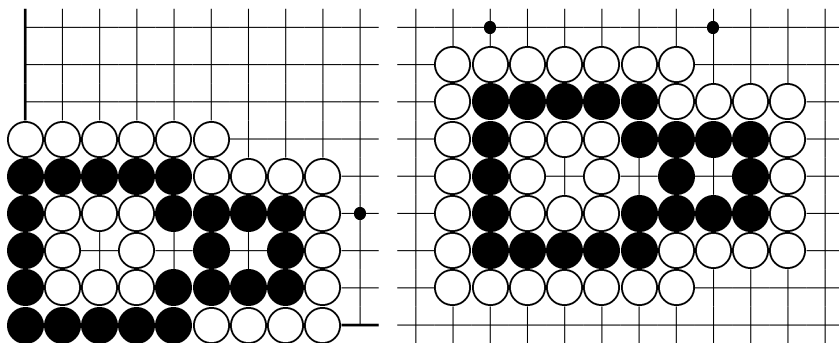
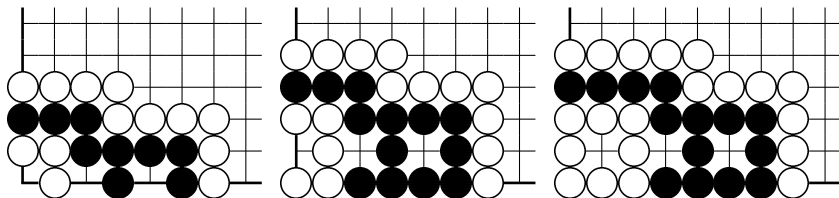
Non-terminal seki



Terminal seki

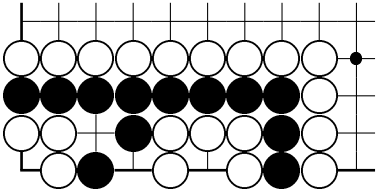
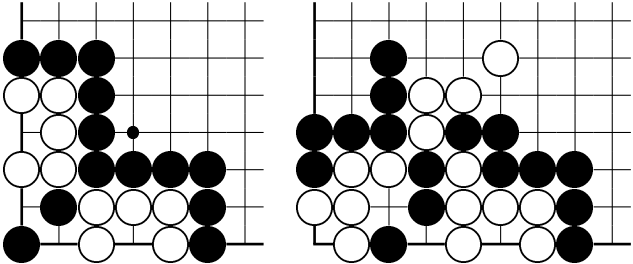
Shift and Deformation

All of these positions are equivalent.



Introducing Cross Cuts II

The following positions differ even more but are still equivalent.



Common Fate Graphs

What is the essence of a seki position?

Commonly used in Go: the *Common Fate Graph* (CFG):

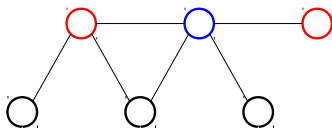
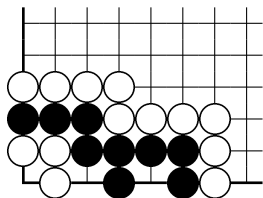


Figure: The corresponding CFG

Circles: red: white chain, blue: black chain, black: liberty

Lines: neighbourhood relations

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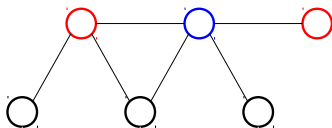
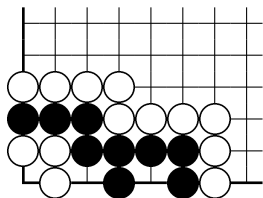


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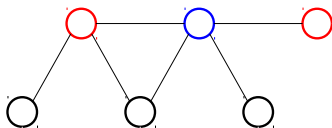
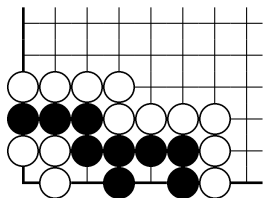


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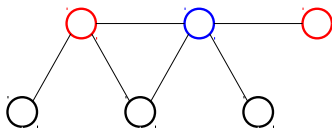
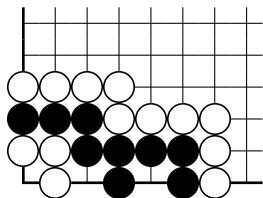


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But the choice of graph depends on the type of seki to be considered.

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Positions are terminal, i.e. a move taking an opponent liberty
gets instantly captured.

Basic Seki Graphs

This special class of seki allows more compact graphs:

Basic Seki Graphs (BSG). Example:

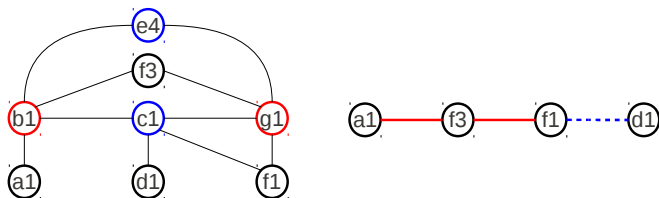
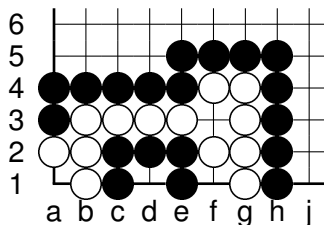


Figure: The 2 corresponding graphs: CFG and BSG

Properties of Basic Seki Graphs I

Necessary properties for graphs to represent basic seki:

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- ▶ There has to be at least one red and one blue edge (otherwise life, not seki).
- ▶ If two edges of same colour, say red, end in a shared node, say M , then both red edges must have their other end in the same other node, say N (otherwise White can move on M and give atari without being captured).

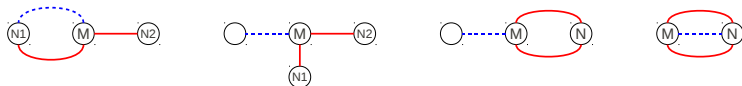


Figure: Two forbidden and two admissible graphs

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- ▶ If two nodes are linked to each other by edges of different colour then these two nodes are all the nodes of the graph (consequence of previous statement, rightmost figure).

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- ▶ If a node has edges of only one colour then these edges may reach only two other nodes (otherwise a move on M creates a chain with 3 liberties).

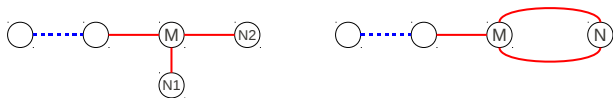


Figure: A forbidden and an admissible graph

Summary on Basic Seki

Main conclusions:

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- ▶ *Therefore Basic Seki consist either of a linear or a circular sequence of liberties where two neighbouring liberties are connected by only chains of one colour.*
- ▶ *The case of only 2 liberties connected by black and white chains can be seen as the smallest circular sequence.*

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⇒ Generating all sequences of such number encodings will generate all Basic Seki.

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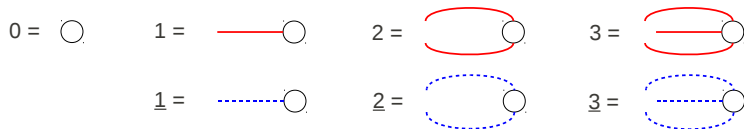


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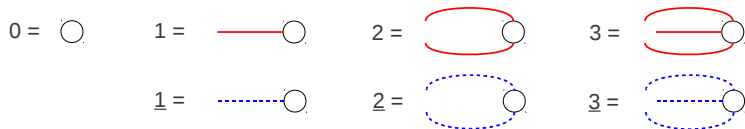


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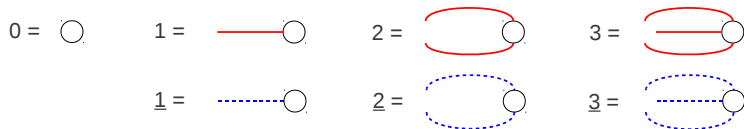


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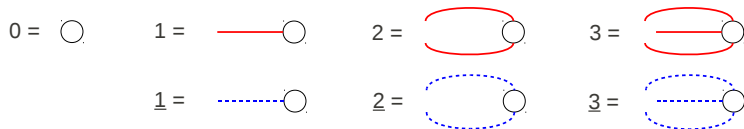


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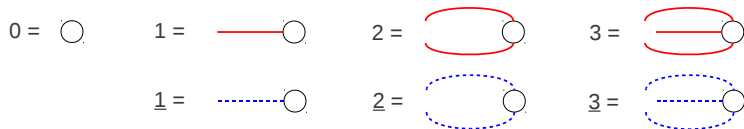
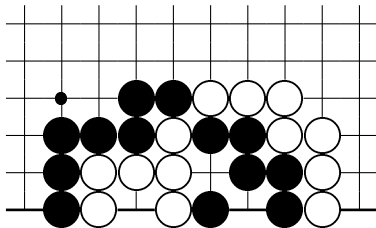


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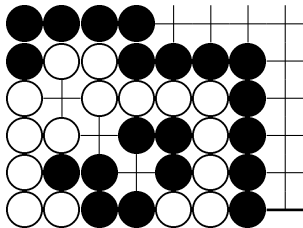
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- ▶ two seki attached on board to one seki → ... + ...

Examples of linear Seki I



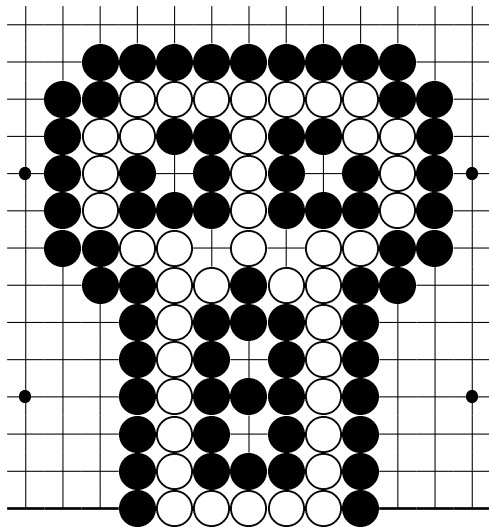
encoding: 012

Examples of linear Seki II



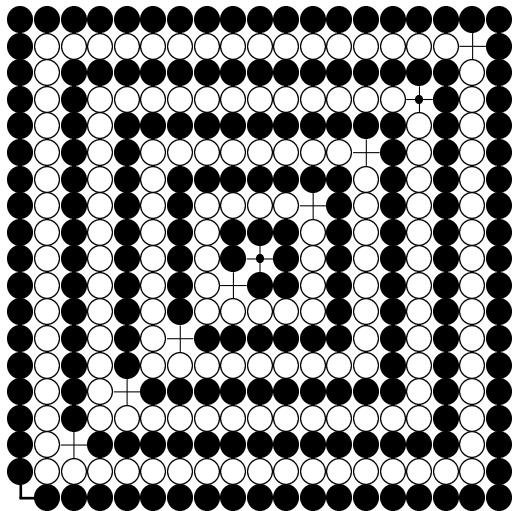
encoding: 0222

Examples of linear Seki III



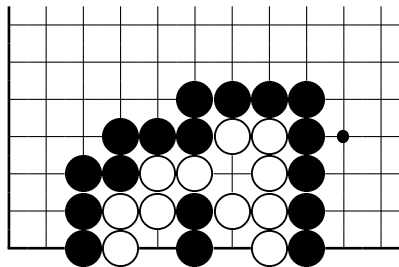
"The Scream" with encoding: 0121

Examples of linear Seki IV



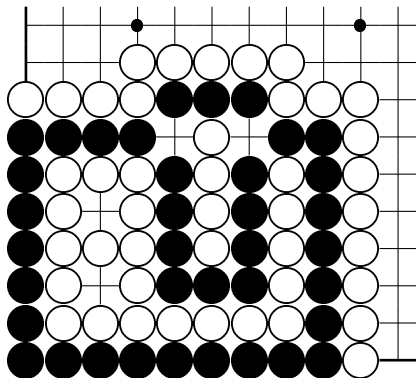
"The Onion" with encoding: $0\underline{1}1\underline{1}1\underline{1}1\underline{1}1\underline{1}1 = 0\underline{1}(\underline{1}1)^4$
looks circular but is linear.

Examples of circular Seki I



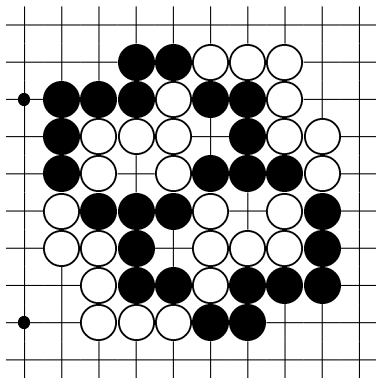
encoding: 111

Examples of circular Seki II



encoding: 31

Examples of circular Seki III



encoding: $\underline{1111} = (\underline{11})^2$

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 - ▶ avoid identical circular basic seki (inversion, colour switch, cyclic permutation, e.g. $2\underline{1}1 = \underline{1}12 = 12\underline{1} = \dots$)

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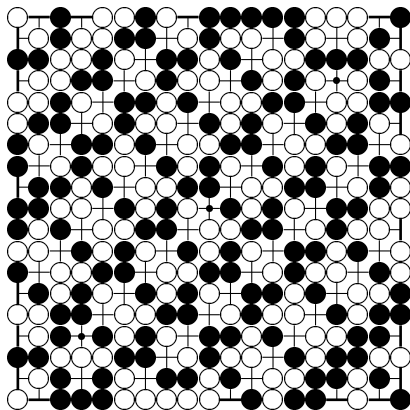
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Attaching Seki



A full board seki of G. Hungerink

The BSG of the whole board consists of three disconnected sub graphs and has the encoding

$$\underline{1211} + 0(\underline{22})^4 \underline{1}(\underline{22})^6 \underline{11211}(\underline{22})^6 \underline{11211}(\underline{22})^6 \underline{1}(\underline{22})^4 + \underline{11211}.$$

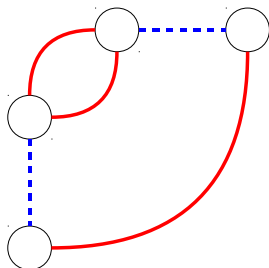
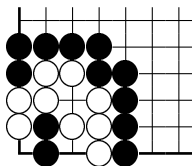


Figure: The upper left corner and the colour switched lower right corner of the board as BSG with encoding 1211.

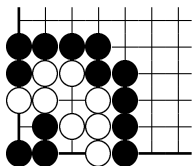
Cutting off a Stone I



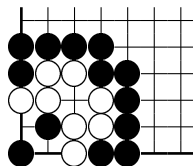
Figure: The change of BSG



encoding: 111

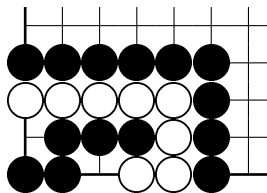


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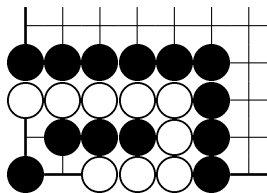


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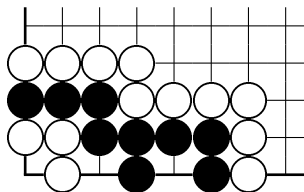
Cutting off a Stone II



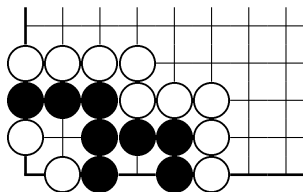
encoding: 11



encoding: 21



encoding: 011



encoding: 021

Creating an Eye I

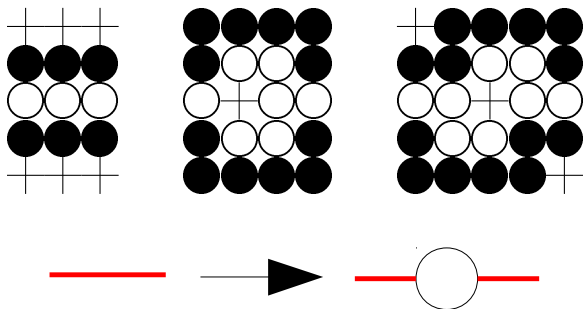
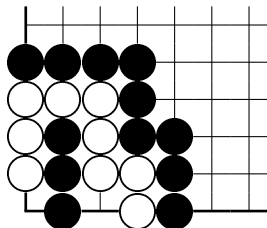
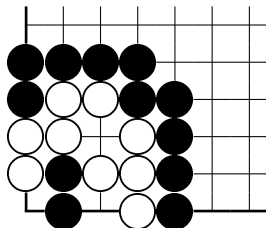


Figure: The change of CFG

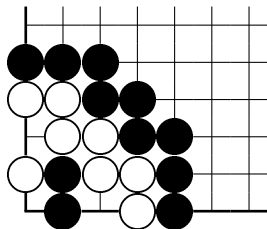
Creating an Eye II



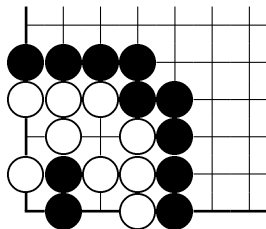
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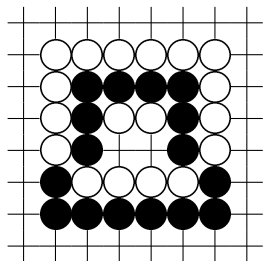


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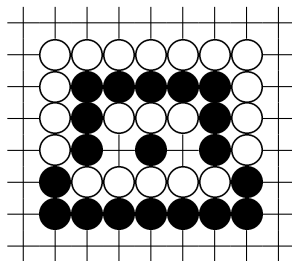


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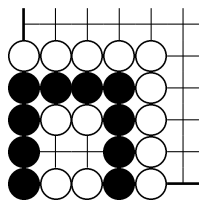
Bamboo Joints in Basic Seki I



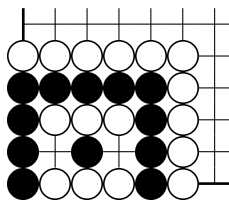
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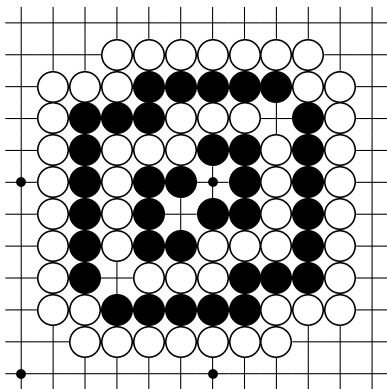
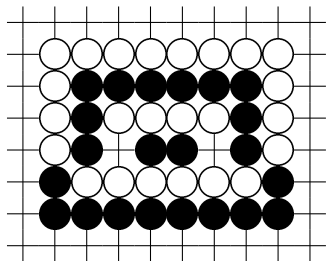


encoding 21



encoding: 22

Bamboo Joints in Basic Seki II



Both seki have the encoding $2\bar{2}$ but different sequences of black and white stones around liberties (WBWB and WWBB).

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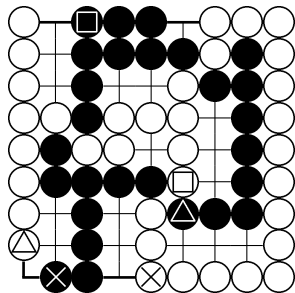
Moves are made by decreasing an A_{ij} by 1.

Problem: For a given computer determined seki matrix a Go position may not exist, e.g. not for:

$$\begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix}.$$

Work of Vladimir Gurvich II

Example:



$i \setminus j$				s_i^W
	0	3	3	6
	3	3	1	7
	3	1	2	6
s_j^B	6	7	6	

Table: The liberty matrix

Lemma: (giving sufficient conditions for Black to capture)

Even when playing second, Black captures if there is a row i such that $s_j^B - A_{ij} \geq s_i^W$ for every column j and $s_j^B > s_i^W$ if $A_{ij} = 0$.

Seki with > 2 Liberties per Chain

We need new graphs where

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⇒ *We are looking for bi-partite planar graphs!*

Bi-partite planar 3-regular Graphs

Sensei's Library [4]:

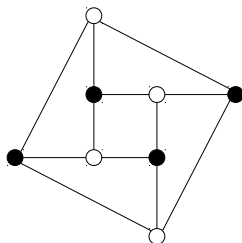
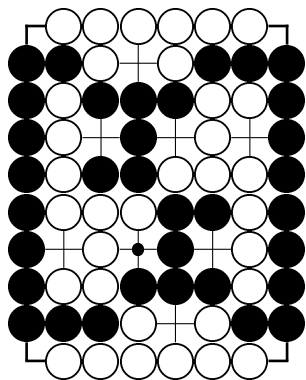


Figure: The corresponding Graph

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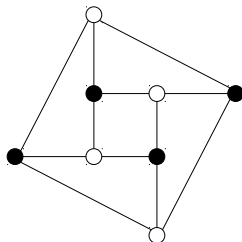
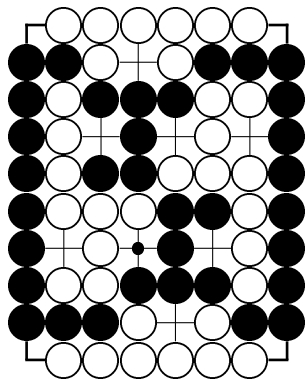


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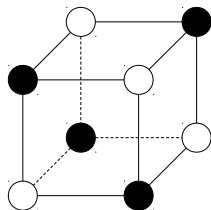


Figure: The same Graph

Planar Graphs and their Dual

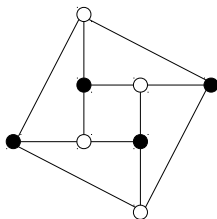
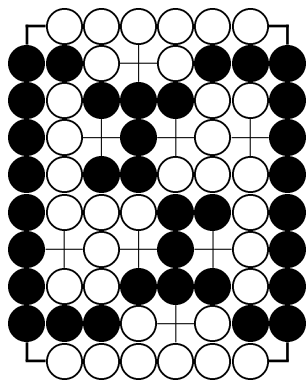


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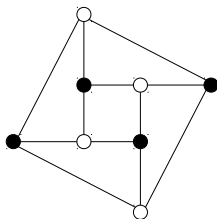
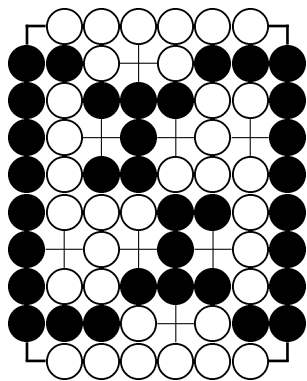


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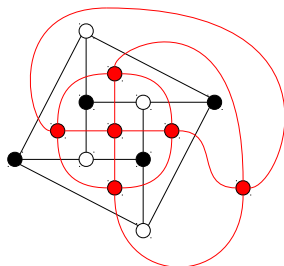


Figure: with it's dual Graph

The Cube and the Octagon

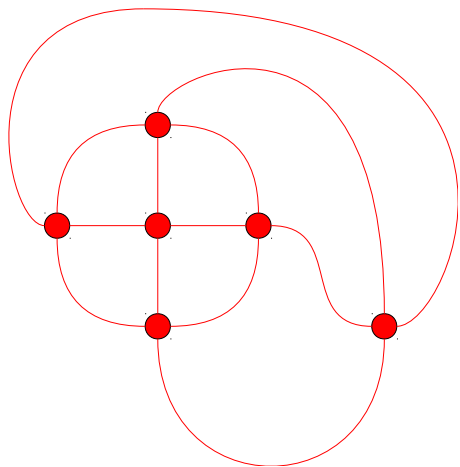


Figure: The dual Graph of a Cube

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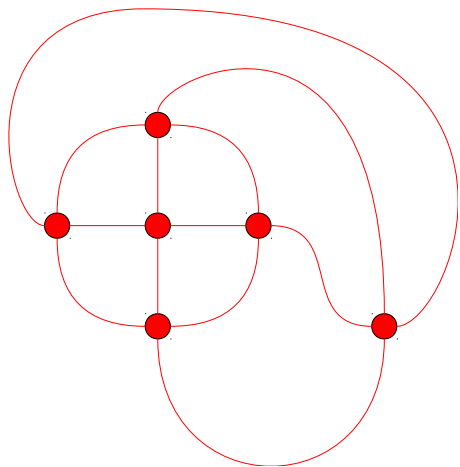


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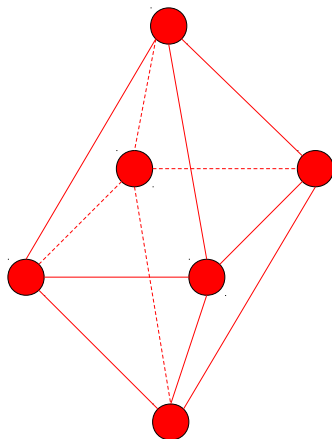


Figure: is an Octagon

Generating more bi-partite planar 3-regular Graphs I

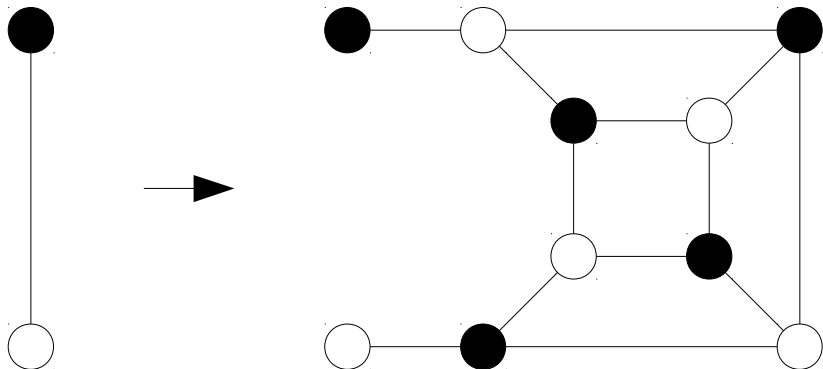
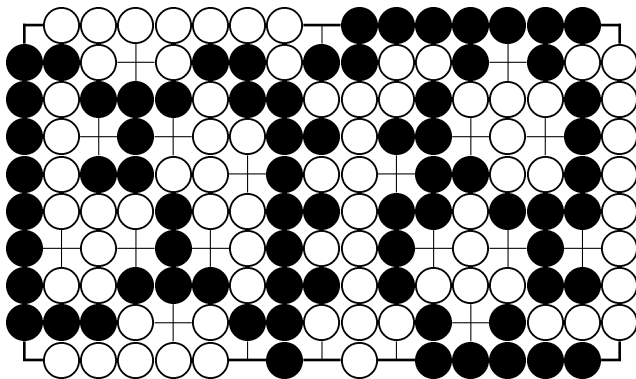


Figure: This replacement of any edge generates each time a new graph and thus a new seki.

Generating more bi-partite planar 3-regular Graphs II



The position resulting from the complication step.

Higher regular Graphs

How about sekis of this type with chains having each 4 or more liberties?

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But, bi-partite planar 3-regular graphs are perfect matchings.

⇒ opportunity to generate higher regular graphs with multi-edges. (i.e. seki with pairs of chains sharing more than 1 liberty).

Again a bi-partite planar 3-regular Graph

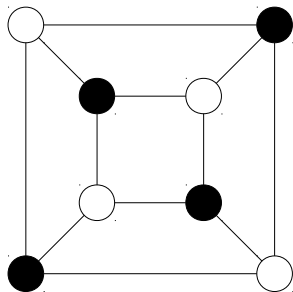
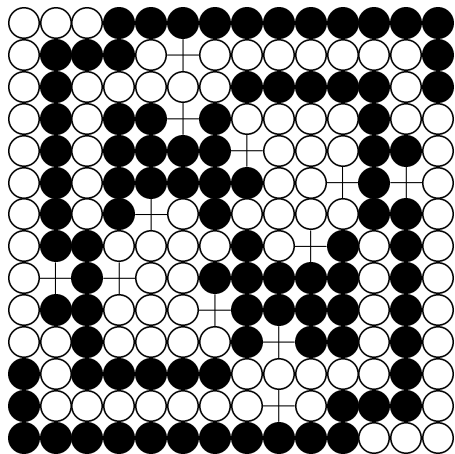


Figure: A cubical graph

A bi-partite planar 4-regular Graph

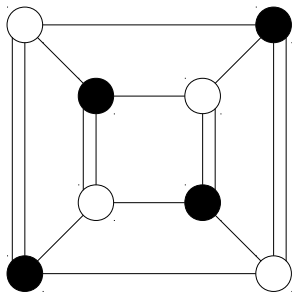
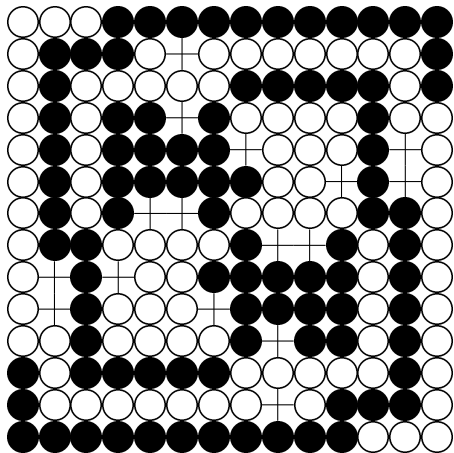


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A bi-partite planar 5-regular Graph

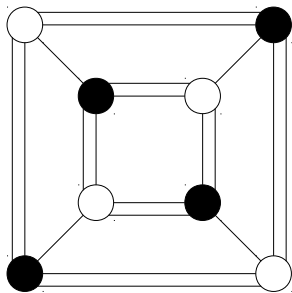
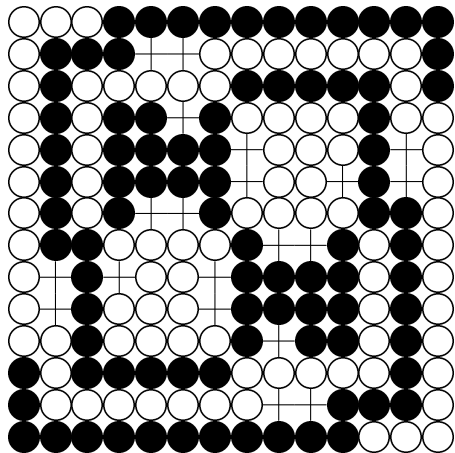


Figure: A cubical graph

A bi-partite planar 6-regular Graph

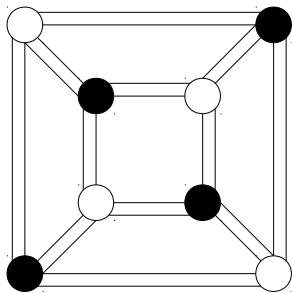
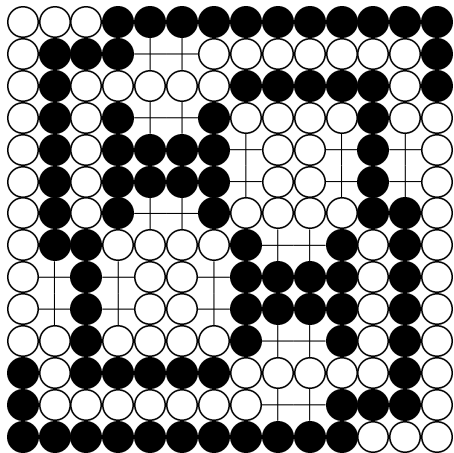


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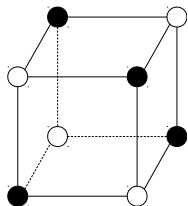
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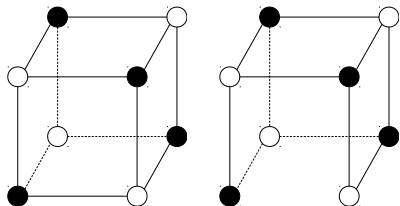
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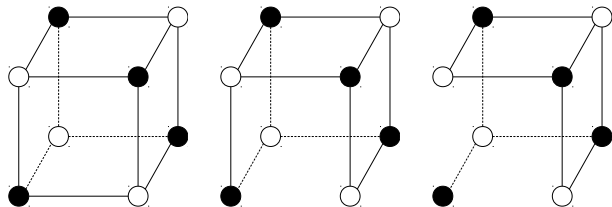
'Local Seki' versus 'global Seki'



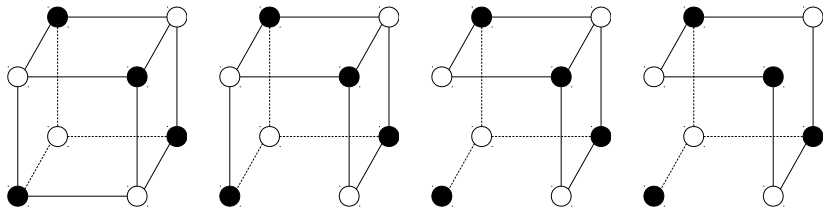
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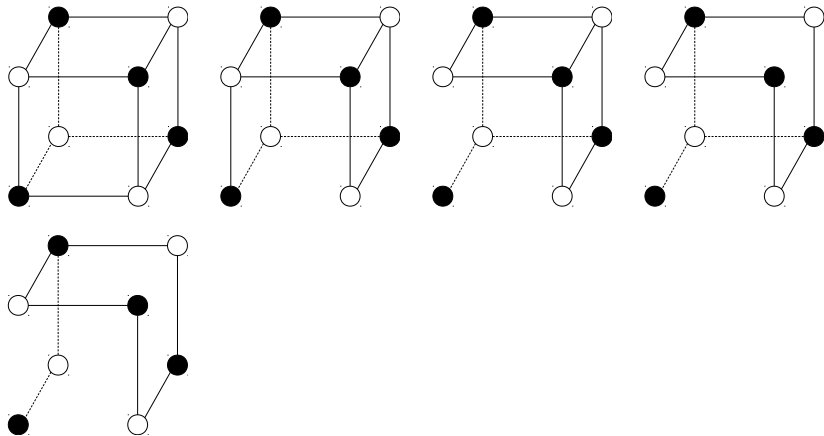
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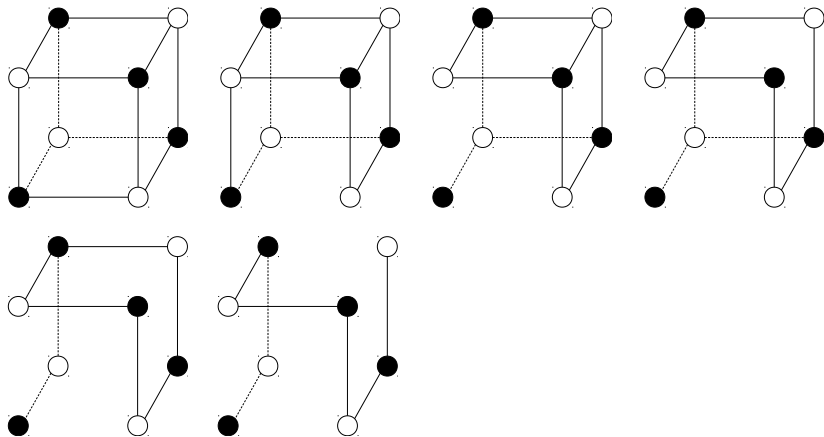
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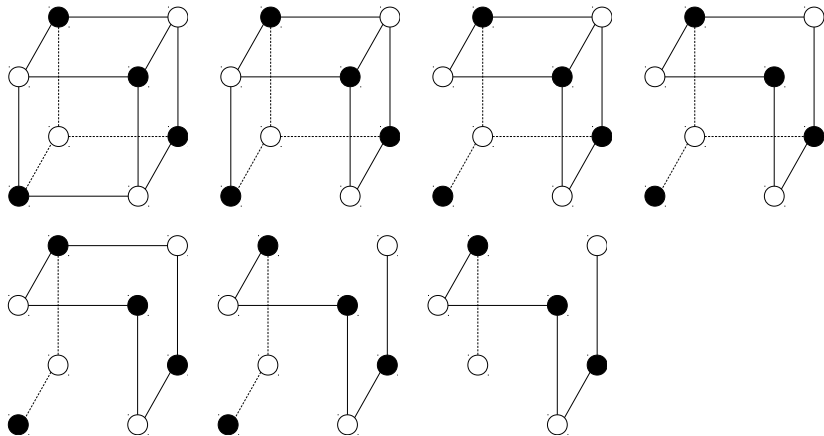
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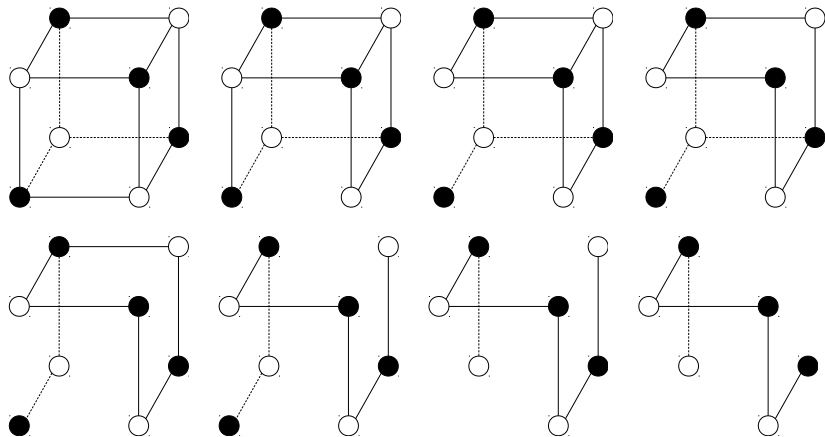


Figure: Global instability of Cubical Seki

⇒ Each attacking chain is captured (i.e. is a local seki) but in return an opponent chain can be captured (i.e. no global seki).

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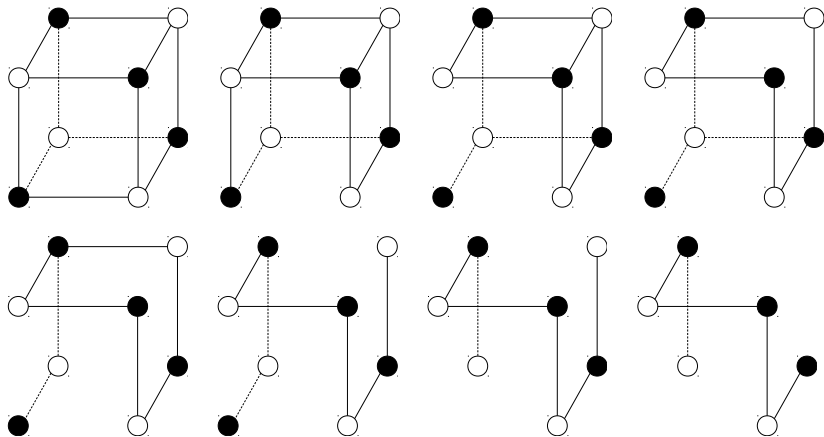
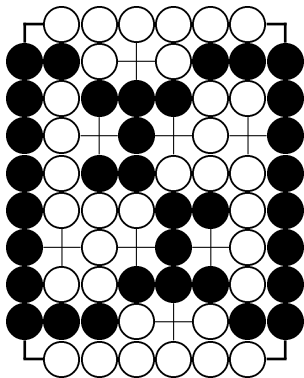


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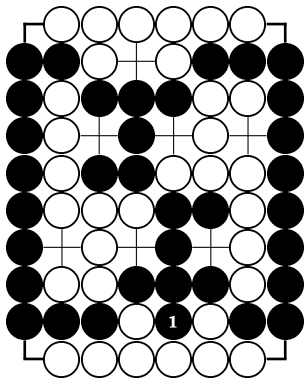
- ⇒ Each attacking chain is captured (i.e. is a local seki) but in return an opponent chain can be captured (i.e. no global seki).
- ⇒ Sacrifice a small chain and catch a big one ⇒ no “real” seki.

A Sacrifice in a Local Seki



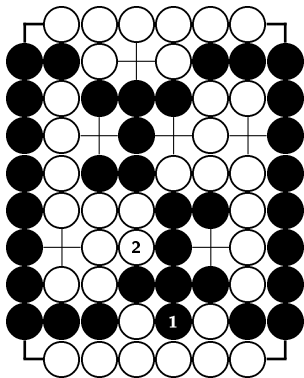
Black to play and sacrifice a small chain to catch a bigger one.

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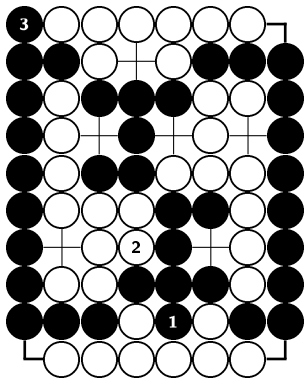
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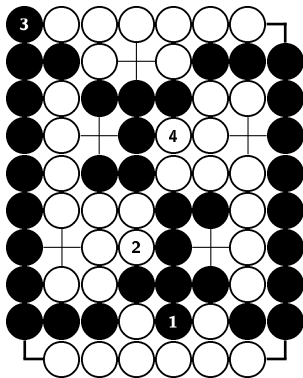
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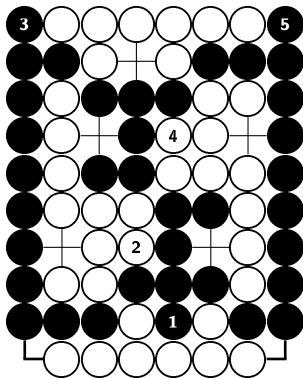
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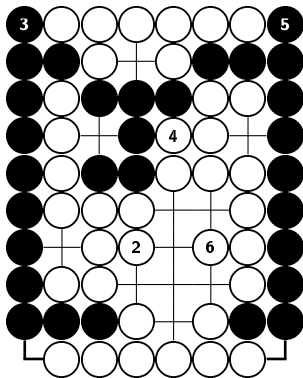
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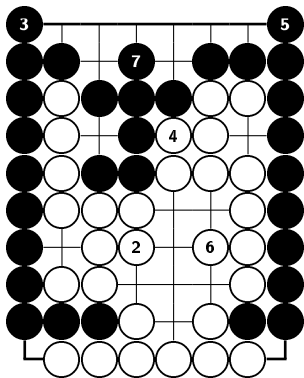
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The End

Thank you!