

**Table S30. Fraction of local heritability observed in simulation (normal allelic effect sizes, imputed SNPs tested).**

Low-frequency un-typed causal variants:										
# casuals	$h_{\text{GWAS}}^2$	$h_{\text{GWAS,joint}}^2$	Gain	$h_g^2$	Gain	$h_{\text{gLDS}}^2$	Gain	$h_{\text{gLDAK}}^2$	Gain	$P(h_{\text{gLDS}}^2 \text{ vs. } h_{\text{gLDAK}}^2)$
1	1.01	1.04 (0.03)	1.03	0.65 (0.07)	<b>0.64</b>	1.11 (0.11)	1.10	0.89 (0.08)	0.88	$1.2 \times 10^{-01}$
2	0.82	0.86 (0.03)	1.05	0.58 (0.06)	<b>0.70</b>	1.00 (0.10)	1.22	1.03 (0.07)	<b>1.26</b>	$8.1 \times 10^{-01}$
3	0.71	0.68 (0.03)	0.96	0.57 (0.05)	<b>0.80</b>	1.00 (0.11)	<b>1.41</b>	0.94 (0.09)	<b>1.33</b>	$7.0 \times 10^{-01}$
5	0.56	0.60 (0.03)	1.07	0.69 (0.06)	<b>1.23</b>	0.74 (0.10)	1.33	1.02 (0.08)	<b>1.82</b>	$3.2 \times 10^{-02}$
10	0.38	0.47 (0.03)	<b>1.24</b>	0.71 (0.07)	<b>1.88</b>	0.93 (0.11)	<b>2.46</b>	0.92 (0.10)	<b>2.42</b>	$9.2 \times 10^{-01}$
Average	0.70	0.73 (0.10)	1.04	0.64 (0.10)	0.91	0.96 (0.10)	1.37	0.96 (0.10)	1.37	

  

Common un-typed causal variants:										
# casuals	$h_{\text{GWAS}}^2$	$h_{\text{GWAS,joint}}^2$	Gain	$h_g^2$	Gain	$h_{\text{gLDS}}^2$	Gain	$h_{\text{gLDAK}}^2$	Gain	$P(h_{\text{gLDS}}^2 \text{ vs. } h_{\text{gLDAK}}^2)$
1	1.00	1.00 (0.03)	1.00	0.70 (0.07)	<b>0.70</b>	0.88 (0.11)	0.88	1.00 (0.10)	1.00	$4.5 \times 10^{-01}$
2	0.82	0.81 (0.03)	0.98	0.71 (0.06)	0.86	0.88 (0.11)	1.07	0.98 (0.09)	1.20	$4.6 \times 10^{-01}$
3	0.71	0.74 (0.03)	1.05	0.65 (0.06)	0.91	0.90 (0.09)	<b>1.27</b>	0.99 (0.09)	<b>1.39</b>	$4.9 \times 10^{-01}$
5	0.56	0.64 (0.02)	<b>1.14</b>	0.74 (0.06)	<b>1.33</b>	0.77 (0.11)	1.38	0.97 (0.07)	<b>1.74</b>	$1.1 \times 10^{-01}$
10	0.37	0.45 (0.02)	<b>1.21</b>	0.77 (0.05)	<b>2.07</b>	0.87 (0.09)	<b>2.35</b>	1.00 (0.09)	<b>2.70</b>	$3.1 \times 10^{-01}$
Average	0.69	0.73 (0.09)	1.05	0.71 (0.09)	1.03	0.86 (0.09)	1.25	0.99 (0.09)	1.43	